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## Studies of miscibility and phase behavior in blends of two random copolymers/

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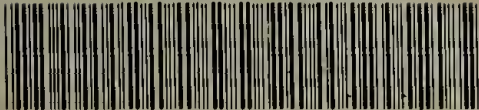
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STUDIES OF MISCIBILITY AND PHASE BEHAVIOR IN BLENDS  
OF TWO RANDOM COPOLYMERS

A Dissertation Presented

by

Heung Sup Kang

submitted to the Graduate School of the  
University of Massachusetts in partial fulfillment  
of the requirements for the degree of

DOCTOR OF PHILOSOPHY

September 1987

Department of Polymer Science and Engineering

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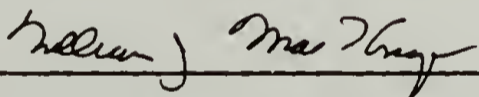
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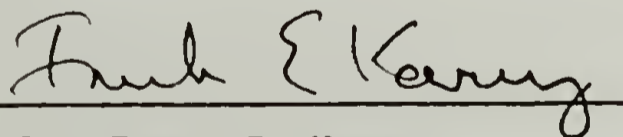
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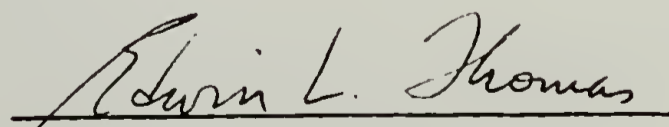
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This thesis is dedicated to my wife, Kyung, and to my two sons, Jin and Hyun, for their understanding and patience during the course of this work.

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## ABSTRACT

### STUDIES OF MISCIBILITY AND PHASE BEHAVIOR IN BLENDS OF TWO RANDOM COPOLYMERS

September 1987

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Miscibility and phase behavior in blends of random copolymers have been studied primarily by differential scanning calorimetry (DSC), optical microscopy, dynamic mechanical measurements and temperature plane and frequency plane dielectric measurements. A series of random copolymers comprising phenylsulfonyl group substituted phenylene oxide repeat units (SPPPO copolymers) was prepared by a Friedel-Crafts sulfonylation reaction of poly(2,6-dimethyl-1,4-phenylene oxide) (PPO) and characterized by elemental analysis, gel permeation chromatography, IR,  $^1\text{H}$ -NMR, DSC, thermogravimetric analysis, dynamic mechanical and dielectric measurements.

The SPPO copolymers were blended with poly(styrene-co-acrylonitrile) (SAN), poly(styrene-co-p(o)-fluorostyrene) and poly(styrene-co-methyl acrylate) (SMA); all systems are of the type  $(A_{1-x}B_x)_{n_1} / (C_{1-y}D_y)_{n_2}$ . SMA copolymers were prepared by free radical solution polymerization. Monomer sequence distributions in SAN copolymers were studied by dielectric relaxation and  $T_g$  measurements. The copolymers exhibited similar dielectric relaxation spectra reflecting small differences in the conformational characteristics and random natures of the copolymers.

Miscibility regimes for each system have been determined at 290°C and displayed in a Cartesian coordinate system and all segmental interaction parameters ( $\chi_{ij}$ 's) involved have been estimated using a mean field treatment. All the blend systems except those containing SMA copolymers display wide miscible regions even though all the  $\chi_{ij}$ 's are positive except  $\chi_{st,po}$ . The experimental miscibility-immiscibility boundaries have been analyzed geometrically and are in reasonably good agreement with calculated boundaries.

Normalized dielectric loss curves of the blends containing SAN copolymers, which were obtained from frequency plane dielectric relaxation measurements, are much broader than those of the pure SAN copolymer, indicating the occurrence of composition fluctuations within the miscible blends. The role of repulsive interactions in

inducing miscibility in blends of poly(p-fluorostyrene) with SPP0 copolymers without any specific interactions has been identified and all the critical phenomena observed in this work are of an LCST type.

## TABLE OF CONTENTS

ACKNOWLEDGEMENTS .....	v
ABSTRACT .....	vi
LIST OF TABLES .....	xii
LIST OF FIGURES .....	xiii

### Chapter

I. INTRODUCTION .....	1
A. Theory of Polymer-Polymer Miscibility .....	3
B. Mean Field Treatment .....	11
C. Experimental Methods for Probing Polymer-Polymer Miscibility .....	14
D. Review of Previous Studies of Copolymer Blends ....	18
References .....	23
II. PREPARATION AND PROPERTIES OF SULFONYLATED POLY(2,6- DIMETHYL-1,4-PHENYLENE OXIDE) COPOLYMERS .....	27
A. Experimental Section .....	28
B. Results and Discussion .....	33
References .....	61

III. MISCIBILITY IN BLENDS OF SULFONYLATED POLY(2,6-DIMETHYL-	
---	--

1,4-PHENYLENE OXIDE) (SPPO) COPOLYMERS AND IN BLENDS OF POLYSTYRENE/SPPO COPOLYMERS .....	64
A. Experimental Section .....	65
B. Results and Discussion .....	67
i) Blends of SPPO Copolymers .....	67
ii) Blends of Polystyrene with SPPO Copolymers ....	82
References .....	99
 IV. MONOMER SEQUENCE DISTRIBUTIONS IN POLY(STYRENE-CO- ACRYLONITRILE) .....	101
A. Experimental Section .....	102
B. Results and Discussion .....	103
References .....	127
 V. MISCIBILITY IN BLENDS OF POLY(STYRENE-CO-ACRYLONITRILE) WITH SPPO COPOLYMERS .....	129
A. Experimental Section .....	129
B. Results and Discussion .....	131
References .....	162
 VI. MISCIBILITY IN BLENDS OF POLY(STYRENE-CO-P(O)-FLUORO- STYRENE) AND POLY(STYRENE-CO-METHYL ACRYLATE) WITH SPPO COPOLYMERS .....	163
A. Experimental Section .....	163
B. Results and Discussion .....	166
i) Blends of Poly(styrene-co-p-fluorostyrene)	

with SPPO Copolymers .....	166
ii) Blends of Poly(styrene-co-o-fluorostyrene)	
with SPPO Copolymers .....	178
iii) Blends of Poly(styrene-co-methyl acrylate)	
with SPPO Copolymers .....	182
References .....	190
VII. CONCLUSIONS .....	191
A. Geometric Analysis of the Miscibility-Immiscibility	
Boundary .....	191
B. Summary of Results .....	195
C. Suggestions for Future Work .....	196
BIBLIOGRAPHY .....	198
APPENDIX I   MISCIBILITY DIAGRAM COMPUTER PROGRAM .....	206

## LIST OF TABLES

2.1 Molecular Weights of Sulfonylated Poly(2,6-dimethyl-1,4-phenylene oxide) Copolymers .....	35
2.2 Properties of Sulfonylated Poly(2,6-dimethyl-1,4-phenylene oxide) Copolymers .....	43
3.1 Mean degree of Sulfonylation Dependence of $\chi_{CD}$ .....	80
3.2 Transition Width and Calculated $\chi_{blend}$ Values .....	93
4.1 Compositions and Properties of Poly(styrene-co-acrylonitrile) .....	104
4.2 Dielectric Parameters for Poly(styrene-co-acrylonitrile).	110
5.1 Dielectric Parameters for SAN 5 and Its Blends with SPP0 12 .....	156
6.1 Molecular Weights of Poly(styrene-co-p(o)- fluorostyrene)	165
6.2 Compositions and Molecular Weights of Poly(styrene-co-methyl acrylate) .....	167
7.1 Coefficients of x, y and xy for Geometric Analysis .....	193

## LIST OF FIGURES

1.1. Temperature dependence of the interaction parameter .....	9
2.1. Schematic diagram of the modification reaction of PPO ....	30
2.2. Degree of sulfonylation vs. theoretical degree of sulfonylation. The numbers 27, 54 and 120 indicate reaction times in hours .....	34
2.3. Density of SPPO copolymers vs. degree of sulfonylation ...	37
2.4. IR spectra of PPO (solid line) and sulfonylated PPO, degree of sulfonylation: 41.0 mole % (broken line) .....	38
2.5. $^1\text{H}$ -NMR spectrum of PPO .....	39
2.6. $^1\text{H}$ -NMR spectrum of sulfonylated PPO; degree of sulfonylation: 35.2 mole % .....	40
2.7. $^1\text{H}$ -NMR spectrum of sulfonylated PPO; degree of sulfonylation: 80.2 mole % .....	41
2.8. Glass transition temperature vs. degree of sulfonylation .	44
2.9. $\Delta C_p$ 's of SPPO copolymers vs. degree of sulfonylation .....	46
2.10. Thermogravimetric analysis of PPO and some modified PPO's .....	48
2.11. Temperatures of indicated weight loss in sulfonylated PPO during heating at $10^\circ\text{C min}^{-1}$ .....	49
2.12. Temperature dependences of mechanical $E'$ , $E''$ and $\tan \delta$	

for PPO at 10 Hz .....	50
2.13. Temperature dependences of mechanical $E'$ , $E''$ and $\tan \delta$	
for dry SPP0 39 at 10 Hz .....	51
2.14. Temperature dependences of mechanical $E'$ , $E''$ and $\tan \delta$	
for wet SPP0 39 at 10 Hz .....	52
2.15. Temperature dependences of dielectric $\epsilon''$ for dry	
SPP0 39 at 50 KHz .....	56
2.16. Frequency dependences of mechanical $\tan \delta$ curves	
for dry SPP0 39 .....	59
2.17. Arrhenius plot of relaxation maxima vs. frequency	
for PPO, SPP0 12 and SPP0 39 .....	60
3.1. DSC thermogram for SPP0 12/34 (50/50 wt % blend) .....	68
3.2. DSC thermogram for SPP0 12/39 (50/50 wt % blend) .....	69
3.3. DSC thermogram for SPP0 47/75 (50/50 wt % blend) .....	70
3.4. DSC thermogram for PPO/SPP0 24 (50/50 wt % blend) .....	71
3.5. DSC thermogram for SPP0 72/90 (50/50 wt % blend).	
Dotted line indicates pure constituents separated by	
aluminum foil. ....	72
3.6. DSC thermogram for SPP0 54/75 (50/50 wt % blend) .....	73
3.7. Optical micrographs for 50/50 wt % blends : .....	75
(a) SPP0 12/34; (b) SPP0 30/54; (c) SPP0 30/55;	
(d) SPP0 12/39; (e) SPP0 47/75; (f) SPP0 12/44	
3.8 $\Delta T_g$ vs. $\Delta$ degree of sulfonylation. Filled and open	
symbols represent one phase and two phase systems,	

respectively. The data represented by triangles were obtained by DSC and optical microscopy. The data represented by circles were obtained by DSC only. The data represented by squares were obtained by optical microscopy only. ....	76
3.9. Isothermal miscibility diagram of 50/50 wt % blends of SPP0 .....	78
3.10. Mean degree of sulfonylation dependence of $\chi_{CD}$ at 290 °C .	81
3.11. DSC thermograms of PS-115, SPP0 12 and blends : .....	84
(A) pure PS-115; (B) 25 wt % SPP0 12; (C) 50 wt % SPP0 12; (D) 70 wt % SPP0 12; (E) 85 wt % SPP0 12; (F) pure SPP0 12	
3.12. Dependence of $T_g$ 's on the weight fraction of SPP0 12 for the PS-115/SPP0 12 blends. Dashed lines represent the Couchman equation, and dotted lines represent the Fox equation with $k=0.66$ . ....	85
3.13. Width of the glass transition and $\Delta C_p$ 's for the PS-115/SPP0 12 blends as a function of blend composition .....	87
3.14. Width of the glass transition and inward shift in $T_g$ for PS-115/SPP0 blends vs. degree of sulfonylation. Widths and inward shifts of the two phase blends are indicated for the PS rich phase. ....	91
3.15. Width of the glass transition for PS-115/SPP0 blends vs. $\chi_{blend}$ .....	94
3.16. DSC thermograms of blends of SPP0 34 and PS of different	

molecular weights annealed at the indicated temperatures.	96
3.17. Phase diagram for blends of PS/SPP0 34 .....	97
4.1. Frequency dependence of dielectric constant, $\epsilon'$ , for SAN 32 .....	105
4.2. Frequency dependence of dielectric loss factor, $\epsilon''$ , for SAN 32 .....	106
4.3. Argand diagram for SAN 32 in the $\alpha$ relaxation region .....	107
4.4. Density of copolymers as a function of AN content .....	109
4.5. Effective dipole moments of copolymers .....	111
4.6. Composition dependence of the correlation parameter, g, for SAN copolymers .....	113
4.7. Temperature dependence of dielectric loss factor, $\epsilon''$ , for SAN 76 .....	115
4.8. Dielectric loss factor $\epsilon''$ as a function of reciprocal temperature at 50 KHz for SAN 76 .....	116
4.9. Frequency dependence of the normalized dielectric loss for SAN 32 .....	118
4.10. Composition dependence of the half width of the dielectric loss for SAN copolymers. The point shown by the open circle was obtained from ref. 17 .....	119
4.11. $T_g$ 's determined experimentally and predicted by con- sidering sequence distribution and the fraction of S-AN dyads calculated vs. mole % AN content .....	125
5.1. DSC thermograms of SAN 26, SPP0 54 and blends :	

(A) Pure SAN 26; (B) 25 % SPP0 54; (C) 50 % SPP0 54;	
(D) 70 % SPP0 54; (E) 85 % SPP0 54; (F) Pure SPP0 54. ....	132
5.2. $T_g$ 's vs. composition for SAN 26/SPP0 54 blends.	
Dashed lines represent the Couchman equation and dotted	
lines represent the Fox equation with $k=0.4$ . ....	134
5.3. $T_g$ 's vs. composition for SAN 5/SPP0 12 blends .....	135
5.4. Miscibility domain for 50/50 wt % blends of SAN copolymers	
with SPP0 copolymers at 290°C .....	136
5.5. Specific volume vs. blend composition expressed as weight	
fraction SPP0. Dashed lines indicate specific volume	
calculated from the additivity relationship. ....	139
5.6. Dynamic mechanical $\tan\delta$ as a function of temperature	
for SAN 18, SPP0 39 and 50/50 wt % SAN 18/SPP0 39	
blends at 1 Hz .....	141
5.7. Dielectric $\tan \delta$ as a function of temperature for	
SAN 5, SPP0 12 and 50/50 wt % SAN 5/SPP0 12 blends .....	143
5.8. (a) Dielectric constant vs. frequency for SAN 5 .....	145
(b) loss factor for SAN 5; (c) Dielectric constant vs.	
frequency for 90/10 wt % SAN 5/SPP0 12 blends; (d) Loss	
factor for 90/10 wt % SAN 5/SPP0 12 blends; (e) Dielectric	
constant vs. frequency for 80/20 wt % SAN 5/SPP0 12	
blends; (f) Loss factor for 80/20 wt % SAN 5/SPP0 12	
blends; (g) Dielectric constant vs. frequency for	
65/35 wt % SAN 5/SPP0 12 blends; (h) Loss factor for	
65/35 wt % SAN 5/SPP0 12 blends. ....	152

5.9. (a) Argand diagram for SAN 5; (b) Argand diagrams for the blends of SAN 5/SPPO 12 of varying compositions. ....	153
5.10. Normalized dielectric loss factor curves for SAN 5 and its blends .....	155
5.11. Fourier transform infrared spectrum of SAN 5 .....	158
5.12. Fourier transform infrared spectrum of 50/50 wt % blend of SAN 5/SPPO 12 .....	159
5.13. Arrhenius plots for SAN 5 and its blends .....	161
6.1. DSC thermograms of P(S-pFS, 77), SPPO 34 and blends : (A) pure P(S-pFS, 77); (B) 25 wt % SPPO 34; (C) 50 wt % SPPO 34; (D) 70 wt % SPPO 34; (D) 85 wt % SPPO 34; (F) pure SPPO 34. ....	168
6.2. Composition dependences of $T_g$ 's for the P(S-pFS, 77)/ SPPO 34 blends .....	170
6.3. $T_g$ 's for blends of P(S-pFS, 77)/SPPO copolymers .....	171
6.4. Miscibility domain for 50/50 wt % blends of P(S-pFS)/ SPPO copolymers at 290 °C .....	172
6.5. DSC thermograms for PpFS/SPPO 34 (50/50 wt % blend) .....	174
6.6. Miscibility of PpFS with SPPO copolymers. The insides of the curves represent the miscibility regions. ....	175
6.7. Phase diagram for blends of PpFS/SPPO 34 .....	176
6.8. Composition dependences of $T_g$ 's for blends of PoFS/PPPO ...	179
6.9. Composition dependences of $T_g$ 's for blends of P(S-oFS, 80)/SPPO 12 .....	180

6.10. Miscibility domain for 50/50 wt % blends of P(S-oFS)/ SPP0 copolymers at 290 °C .....	181
6.11. SMA copolymer vs. feed composition .....	183
6.12. T <sub>g</sub> 's of SMA copolymers .....	185
6.13. DSC thermogram for 50/50 wt % blend of SMA 15/SMA 34 ....	186
6.14. Miscibility diagram for 50/50 wt % blends of SMA copolymers .....	187
6.15. Miscibility domain for 50/50 wt % blends of SMA copolymers with SPP0 copolymers at 290 °C .....	188
7.1. Comparison of calculated and experimental miscibility domains .....	194

## CHAPTER I

### INTRODUCTION

The study of miscibility in polymer blends has received extensive attention as a means of developing polymer systems with desired properties under proper processing conditions. In comparison with low molecular weight compounds, mixtures of high molecular weight components involve a nearly negligible combinatorial entropy of mixing. Thus, the negative exchange interaction was considered to be a prerequisite for the miscibility of binary mixtures of sufficiently high molecular weight.

However, some blend systems in which at least one of the components is a random copolymer have been found to be miscible for a particular range of the copolymer composition even though none of the binary combinations of the homopolymers is miscible. An increasing number of miscible copolymer blends without intermolecular interactions have been identified. Blends of poly(vinyl chloride)/poly(ethylene-co-vinyl acetate)<sup>1</sup>, poly(vinyl chloride)/poly(butadiene-co-acrylonitrile)<sup>2</sup> and poly(methyl methacrylate)/poly(styrene-co-acrylonitrile)<sup>3</sup>, systems of the type

$A_{n_1}/(C_{1-y}^D y)_{n_2}$ , are among such cases. These findings reflect that specific interactions are not always necessary for miscibility and that, by the rational design of copolymers, new technologically important miscible systems can be engineered at reasonable cost.

Blends of a series of halogen containing styrenic copolymers with poly(2,6-dimethyl-1,4-phenylene oxide) (PPO), i.e., systems of the type  $(A_{1-x}^B x)_{n_1}/C_{n_2}$ , have been studied extensively<sup>4-9</sup> and blends of two random copolymers having a common monomer segment of the system of the type  $(A_{1-x}^B x)_{n_1}/(C_{1-y}^B y)_{n_2}$  have been investigated<sup>10-11</sup>. However, no systematic experimental studies of miscibility behavior in blends of two random copolymers with four distinct repeat units of the type  $(A_{1-x}^B x)_{n_1}/(C_{1-y}^D y)_{n_2}$  in which six segmental interaction parameters are required for a description of the miscibility behavior have been reported so far.

The main goal of this thesis is the extension of a mean field treatment to random copolymer blends of the type  $(A_{1-x}^B x)_{n_1}/(C_{1-y}^D y)_{n_2}$  and the analysis of miscibility behavior in these blends. The phase stability above the glass transition temperature was explored. The monomer sequence distribution in the styrene-acrylonitrile copolymers employed in this work was also investigated.

In this chapter the general principles underlying polymer-polymer miscibility as a background to this thesis work will be discussed. In addition, a review of the literature on copolymer blend studies will be presented.

### A. Theory of Polymer-Polymer Miscibility

The purpose of this section is to briefly review the thermodynamic theories dealing with polymer blends. The stability of any binary system requires that the Gibb's free energy of mixing be negative:

$$\Delta G_m = \Delta H_m - T\Delta S_m < 0 \quad (1.1)$$

and that the second derivative of the free energy with respect to some composition variable,  $X$ , be positive<sup>12</sup>:

$$(\partial^2 \Delta G_m / \partial X_i^2)_{T,P} > 0 \quad (1.2)$$

The inequality, Eqn. (1.2), requires that the energy-composition diagram be concave downward.

The boundary between the stable region and the metastable region where systems are stable to small perturbations but unstable

to large disturbances is termed the binodal. The boundary between the metastable and unstable region where the free energy-composition diagram is concave upward is termed the spinodal. The spinodal boundary is the inflection point of the free energy-composition diagram given as

$$(\partial^2 \Delta G_m / \partial X_i^2)_{T,P} = 0 \quad (1.3)$$

The locus of the binodal is found by setting the chemical potentials of both homopolymers equal in the two coexisting phases.

Upon an increase in temperature, the binary system can phase separate. The temperature at which phase separation first appears is called an lower critical solution temperature (LCST). Analogously, phase separation upon a decrease in temperature is indicative of the existence of an upper critical solution temperature (UCST). The position of the critical solution temperatures can be calculated

$$(\partial^2 \Delta G_m / \partial X_i^2)_{T,P} = (\partial^3 \Delta G_m / \partial X_i^3)_{T,P} = 0 \quad (1.4)$$

The first attempts at a description of polymer solution thermodynamics were performed by Flory<sup>13,14</sup> and Huggins<sup>15,16</sup>. The Flory-Huggins theory is based on a simple lattice representation for polymer solutions. The entropy of mixing is calculated on a

statistical basis. The polymer chain is divided into segments equal in size to the solvent molecules. Each segment and solvent molecule occupies a simple lattice site. The expression for the entropy of mixing for a binary mixture is :

$$\Delta S_m/R = (\phi_1/n_1)\ln\phi_1 + (\phi_2/n_2)\ln\phi_2 \quad (1.5)$$

where  $\phi_i$  is the volume fraction, and  $n_i$  is the number of segments per chain. The enthalpy of mixing is a van Larr-type energy term. This results in a free energy of mixing given by the following expression :

$$\Delta G_m/RT = (\phi_1/n_1)\ln\phi_1 + (\phi_2/n_2)\ln\phi_2 + \phi_1\phi_2\chi_{\text{blend}} \quad (1.6)$$

The original Flory-Huggins theory ignores the equation of state parameters of the pure components and assumes no change in the volume of mixing. According to this theory,  $\chi$  resulting only from contact energy dissimilarities between components 1 and 2, neglecting any specific interactions, is independent of concentration and molecular weight and decreases as the temperature increases. Thus, only UCST behavior can be predicted. The existence of an UCST is known to be fairly common for low molecular weight solutions. However, some polymer-polymer systems have been found to display LCST behavior.

Tompa<sup>17</sup> and Koningsveld<sup>18</sup> proposed the generalized Flory-Huggins theory in which they considered the interaction parameter to be dependent on temperature, molecular weight and composition. Koningsveld expressed the free enthalpy correction parameter  $g$ ,

$$g = \sum g_k \phi^k \quad (1.7)$$

Assuming that the temperature and concentration dependence can be separated, one can write

$$g = g_{0,1} + g_{0,2}/T + g_{0,3}T + g_{0,4}\ln T \quad (1.8)$$

Thus, depending upon the sign of  $g_{0,2}$  an LCST or UCST can be described. However, this is an empirical approach to describe the experimental data, and is lacking a molecular interpretation of the dependences of  $g$  on temperature, concentration and molecular weight.

Several theories<sup>19-21</sup> have been developed to explain the observed behavior on a more molecular level. These theories considered an additional contribution to the entropy of mixing, namely, the excess entropy of mixing resulting from volume changes on mixing, and such excess entropy effects are believed to play an important role in the overall thermodynamic behavior. Flory's equation of state theory<sup>19</sup> originated from Prigogine's assumption<sup>22</sup>

that the degrees of freedom of a molecule in a liquid can be separated into internal and external degrees of freedom. The external degrees of freedom per polymer segment are less than those for a similar small molecule and depend only on the intermolecular forces. The internal degrees of freedom depend on intramolecular chemical bond forces. Each pure component is characterized by three equation of state parameters :  $T^*$ ,  $P^*$  and  $V_{sp}^*$  which are the characteristic temperature, pressure and specific volume, respectively. The three characteristic parameters,  $V^*$ ,  $P^*$  and  $T^*$  can be determined from the experimental values of the thermal expansion coefficient  $\alpha$ , the thermal pressure coefficient  $\beta$ , and the specific volume  $V_{sp}$ . The resulting equation of state is

$$\tilde{P}\tilde{V}/\tilde{T} = \tilde{V}^{-\frac{1}{3}} / (\tilde{V}^{-\frac{1}{3}} - 1) - (1/\tilde{V}\tilde{T}) \quad (1.9)$$

where the tilde ( $\sim$ ) represents reduced parameters;  $\tilde{P} = P/P^*$ ;  $\tilde{V} = V/V^*$  and  $\tilde{T} = T/T^*$ .

According to the Prigogine-Flory theory<sup>23</sup>, as reviewed by Patterson and Robard<sup>24</sup>, the  $\chi$  parameter consists of two contributions : an interactional term and a free volume term. The sign of the enthalpy of mixing is determined by the first derivative of the  $\chi$  parameter<sup>25</sup>. That is,

$$\Delta H_m = -RT^2(\partial\chi/\partial T)\phi_2\phi_3 \quad (1.10)$$

Figure 1.1 shows the possible temperature dependence of  $\chi$ . Curve 1 shows the contribution to  $\chi$  due to contact energy dissimilarities between component 1 and component 2. In the absence of specific interactions, curve 1 decreases with temperature. Curve 2 shows the contribution to  $\chi$  due to the equation of state parameters for the two components. Curve 3 is the sum of these two contributions. Thus, the equation of state theory predicts that blends will show an LCST as the temperature increases and that an UCST will appear as the temperature decreases. However, two polymers with a specific interaction will exhibit only an LCST, in this case curve 1 will not be applicable. McMaster<sup>26</sup> evaluated the effect of molar mass, thermal expansion coefficient, thermal pressure coefficient and the entropic correction parameter on the basis of the equation of state theory and asserted that if the equation of state parameters for the two polymers are similar, the polymers have a better chance for miscibility.

Sanchez<sup>27</sup> proposed a lattice fluid theory based on similar reasoning to that of Flory's equation of state theory. For the pure components an equation of state is given by

$$\tilde{p}^2 + \tilde{p} + \tilde{T}[\ln(1 - \tilde{p}) + (1 - 1/n)\tilde{p}] = 0 \quad (1.11)$$

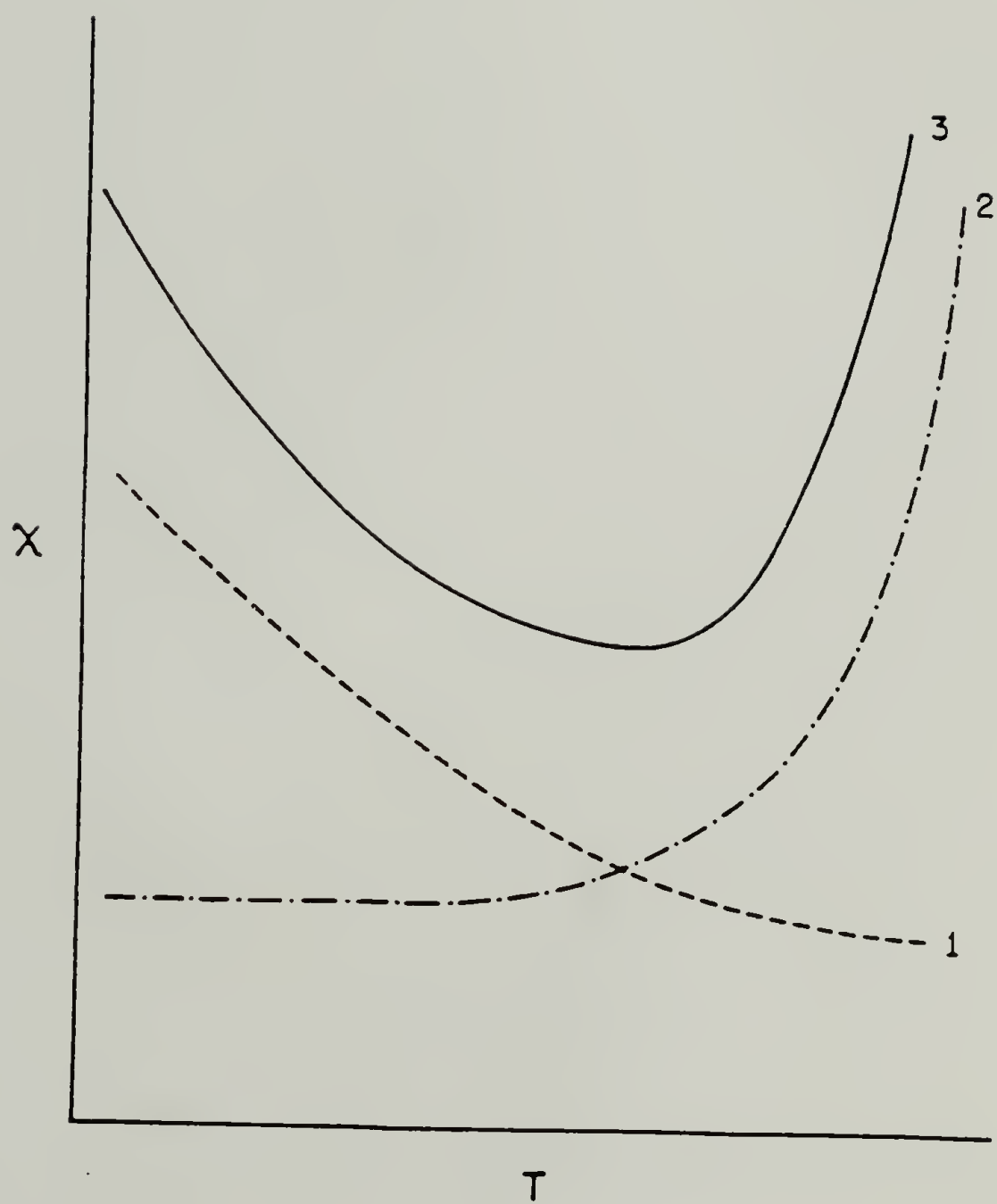


Figure 1.1. Temperature dependence of the interaction parameter

where  $\tilde{\rho}$ ,  $\tilde{P}$  and  $\tilde{T}$  are the reduced density, pressure and temperature and "n" is the number of mers. The phase behavior of the polymer mixtures could be inferred by examination of the spinodal<sup>28</sup>. The condition for phase stability was derived as

$$\tilde{\rho}(2\chi + \tilde{T}\psi^2\tilde{P}^*\beta) < (1/n_1\phi_1) + (1/n_2\phi_2) \quad (1.12)$$

where  $\psi$  is a term containing volume parameters and  $\phi_i$  the volume fractions. The right hand side of Eqn. (1.12) is a combinatorial entropy of mixing type expression. By analysis of the temperature dependences of the terms on the left hand side of Eqn. (1.12). the general features of the phase diagram could be ascertained. In all cases, LCST behavior was predicted.

According to the lattice fluid theory<sup>27</sup>, the second derivative of the free energy of mixing is composed of incompressible and compressible contributions and for a binary mixture to be miscible, the Gibbs free energy at fixed temperature and pressure should be a convex function of the concentration and specific volume. That is,

$$\partial^2 G / \partial C^2 - v\beta(\partial^2 G / \partial C \partial v)^2 > 0 \quad (1.13)$$

The second term is always negative, thus giving an unfavorable effect on mixing and since  $\beta$  increases with temperature, this term becomes pronounced at higher temperature, thus resulting in the destabilization of mixtures at elevated temperature indicative of LCST behavior.

### B. Mean Field Treatment

To explain a range of miscibility phenomena involving random copolymer blends, ten Brinke et al<sup>29</sup> proposed a mean field treatment which assumes  $\chi_{ij}$  to be independent of composition and local environment. Then  $\chi_{\text{blend}}$  in Eqn. (1.6) is, in the case of a blend of two copolymers of the type  $(A_{1-x}B_x)_{n_1} / (C_{1-y}D_y)_{n_2}$ , given by a linear combination of the respective segmental interaction parameters such that

$$\begin{aligned} \chi_{\text{blend}} = & (1-x)(1-y)\chi_{AC} + y(1-x)\chi_{AD} + x(1-y)\chi_{BC} \\ & + xy\chi_{BD} - x(1-x)\chi_{AB} - y(1-y)\chi_{CD} \end{aligned} \quad (1.14)$$

where  $x$  and  $y$  denote the copolymer compositions expressed in volume fractions.

A critical point occurs at a temperature for which  $\chi_{\text{blend}}$  equals  $\chi_{\text{blend}}^{\text{crit}}$ , given by

$$\chi_{\text{blend}}^{\text{crit}} = \frac{1}{2} (n_1^{-1/2} + n_2^{-1/2})^2 \quad (1.15)$$

Thus, miscibility corresponds to  $\chi_{\text{blend}} < \chi_{\text{blend}}^{\text{crit}}$  and immiscibility to  $\chi_{\text{blend}} > \chi_{\text{blend}}^{\text{crit}}$ .

If  $\chi_{AB}$  and/or  $\chi_{CD}$  are positive and large, i.e., of sufficiently large mutual repulsion between segments A and B, or C and D, then a region of miscibility may be predicted for a particular range of x and/or y, even if all  $\chi_{ij}$ 's are positive. This "repulsion effect" can lead to the negative net interaction energy necessary to induce thermodynamic miscibility.

Paul et al<sup>30</sup> also proposed a binary interaction model which considers that an intermolecular interaction plays an important role in the polymer blend. A van Laar type of heat of mixing is given by

$$\Delta H_m/V = \sum_{i>j} B_{ij} \phi_i \phi_j \quad (1.16)$$

where  $V$  is the total volume of mixture and  $B_{ij}$  is a binary interaction energy density between the components  $i$  and  $j$  and is related to the  $\chi$  parameters such that

$$B/kT = \chi_A/V_A = \chi_B/V_B = \tilde{\chi}_{AB} \quad (1.17)$$

where  $V_i$  is the molar volume of component  $i$ . The effective interaction energy density for the mixing of polymers A and B is given by

$$\begin{aligned} B = & B_{13}\phi_1'\phi_3' + B_{14}\phi_1'\phi_4' + B_{23}\phi_2'\phi_3' + B_{24}\phi_2'\phi_4' \\ & - B_{12}\phi_1'\phi_2' - B_{34}\phi_3'\phi_4' \end{aligned} \quad (1.18)$$

where polymer A is comprised of monomers 1 and 2 with volume fractions of each denoted by  $\phi_i'$  and polymer B is comprised of monomers 3 and 4. If  $B_{12}$  and/or  $B_{34}$  is positive and large enough, this repulsion makes  $B$  less than additive and favorable to mixing.

Kambour et al<sup>31</sup> also proposed an analogous model which considers the local free energy of mixing to be related to  $\chi$ .

The temperature dependence of  $\chi_{blend}$  is<sup>29</sup>, for blends involving copolymers,

$$\chi_{\text{blend}}^{\text{crit}}(T) = \{C/[V(T)T]\}X_{\text{eff}} \quad (1.19)$$

where  $T$  is the temperature,  $C$  is a constant,  $V$  is the reduced volume of the mixture,  $X_{\text{eff}}$  is the effective interaction parameter which is a function of copolymer composition and individual real interaction parameters. For  $X_{\text{eff}} > 0$ ,  $\chi_{\text{blend}}^{\text{crit}}$  decreases as a function of temperature whereas it increases as a function of temperature for  $X_{\text{eff}} < 0$ . For a particular copolymer composition either of these cases may occur. If  $X_{\text{eff}}$  is positive,  $\chi_{\text{blend}}$  is also positive and miscibility does not occur. If, on the other hand,  $X_{\text{eff}}$  is negative,  $\chi_{\text{blend}}$  increases as a function of temperature, resulting in an LCST behavior.

### C. Experimental Methods for Probing Polymer-Polymer

#### Miscibility

A variety of methods is available for investigating polymer blends. The experimental criteria for miscibility have been extensively reviewed<sup>27,32-34</sup>. This section will briefly discuss only those techniques which have been used in this work.

#### Optical Microscopy

The optical microscope has been extensively used to examine the morphology of rubber blends and of semi-crystalline polymers. It has a resolution down to about  $0.2\ \mu\text{m}$  if the contrast is sufficient. For binary combinations of rubbers there seems to be a crude correlation between domain size and the solubility parameter differences.

However, this method is subject to certain limitations. Mixtures of poly(styrene-co-butadiene) and polybutadiene have been described as either homogeneous<sup>35</sup> or heterogeneous<sup>36</sup>. These opposing results are due to poor phase contrast. Furthermore, if two component polymers have equal refractive indices or the dispersed phases have dimensions smaller than the resolution limit of the optical microscope, absolute judgement on the miscibility of the two polymers cannot be made.

#### Glass Transition Criterion

The examination of glass transition behavior has largely prevailed as a diagnostic test of miscibility. A miscible polymer blend will exhibit a single glass transition temperature lying between the two glass transition temperatures of the pure components. A phase separated polymer blend will exhibit two  $T_g$ 's. Polymers exhibiting a partial miscibility may show two  $T_g$ 's, one representing

a phase rich in component 1, the other representing a phase rich in polymer 2.

The techniques by which the  $T_g$ 's of polymers may be determined will be discussed.

### Differential Scanning Calorimetry

This technique is useful because of small sample requirements, relatively rapid measurement capability and high sensitivity. But,  $T_g$  measurements are subject to some drawbacks. The  $T_g$  of a polymer is rate dependent, that is the  $T_g$  occurs over a time and temperature range. Thus, the  $T_g$  criterion cannot normally yield information about equilibrium states below the  $T_g$ . In addition,  $T_g$  measurements cannot be used to assess the miscibility of two polymers if their  $T_g$ 's lie within 20°C or less of each other. In this case, the use of a derivative presentation,  $dC_p/dT$  vs.  $T$ , may somewhat alleviate this problem. If one component is present in low concentration, for example less than 10%, in the mixture, its  $T_g$  may not be detected because of the limits of the sensitivity of the technique. Crystallization of either or both constituents may also cause a problem since the sensitivity of the technique is reduced by the diminution of the amorphous phase concentration and since, in

some cases, the crystallization itself may make  $T_g$  determination obscure.

### Dynamic Mechanical Spectroscopy

Examination of the loss angle,  $\tan \delta$ , or the loss modulus,  $E''$ , can be used to assess miscibility. This can be done over a frequency range, typically two to four decades wide. The low-temperature secondary relaxations of the component polymers may also be studied to reveal the extent of mixing between the different polymer molecules. However, if the size of the phase domain is small, the magnitude of the loss peak will be reduced, and may not be detected.

### Dielectric Relaxation Spectroscopy

This technique is very powerful in the assessment of the miscibility of blends involving electrically dipolar groups. Although it is similar in many respects to its mechanical analogue, a much wider frequency range, usually six or more decades, is available, which makes the presentation of a time-temperature superposition possible. These measurements can provide information about the intra- and intermolecular interaction and the conformational effect in the blends. This technique is useful for studying the relaxational characteristics at equilibrium from the

frequency plane measurements. It can also yield information about the microstructure (i.e., the monomer level) of the mixture such as phase separation on a microscale in the blends. However, if one component has traces of ionic impurities, then a DC conductivity effect will take place, which makes the definite assessment of miscibility of blends difficult.

#### D. Review of Previous Studies of Copolymer Blends

The studies of copolymer blend systems analyzed by a mean field treatment will be listed in this section. The miscibility of PPO with random copolymers of poly(o-fluorostyrene-co-p(o)-chlorostyrene)<sup>37-39</sup>, poly(o-fluorostyrene-co-p-fluorostyrene)<sup>7,38,40</sup>, poly(o-chlorostyrene-co-p-chlorostyrene)<sup>41,42</sup>, poly(o-bromostyrene-co-p-bromostyrene)<sup>40</sup>, poly(o-fluorostyrene-p(o)-bromostyrene)<sup>43</sup>, and poly(p-fluorostyrene-co-p(o)-bromostyrene)<sup>43</sup> has been studied. Copolymers of o-fluorostyrene with p-chlorostyrene containing 15-62 mole% p-ClS are miscible with PPO in all proportions<sup>9,37-39</sup>. Blends of this copolymer with 74 mole% p-ClS showed phase separation at 250 °C. Miscibility in the PPO/poly(o-fluorostyrene-co-o-chlorostyrene) system was observed for copolymers containing between 15 and 36 mole % o-chlorostyrene and phase separation was observed after annealing to a temperature of 230 °C<sup>9,37-39</sup>.

Blends of PPO with copolymers of poly(p-fluorostyrene-co-o-fluorostyrene) containing from 10 to 38 % p-fluorostyrene were miscible in all proportions and showed LCST behavior<sup>7,38,40</sup>. Blends of PPO with copolymers of poly(p-chlorostyrene-co-o-chlorostyrene) with the p-chlorostyrene content from 23 to 64 % were miscible in all proportions and exhibited phase separation upon annealing at elevated temperatures indicative of an LCST<sup>41,42</sup>. The LCST was around 220°C when the copolymer composition was 0.23 or 0.65 mole fraction p-ClS and rose to 300°C at about 0.40 mole fraction p-ClS content. The copolymer of poly(o-fluorostyrene-co-p-bromostyrene) only with 11-73 mole % p-bromostyrene was miscible with PPO<sup>43</sup>.

Miscibility of PPO with random copolymers of poly(styrene-co-p(o)-bromostyrene)<sup>40,44</sup>, poly(styrene-co-p(o)-fluorostyrene)<sup>5,8</sup>, and poly(styrene-co-p(o)-chlorostyrene)<sup>40,42,45</sup> has been studied. The blends of PPO with random copolymers of poly(styrene-co-p-bromostyrene) with a p-bromostyrene content of less than 60 mole % were miscible after annealing up to 200°C and showed an LCST at elevated temperature<sup>40,44</sup>. The blends of PPO with poly(styrene-co-o-bromostyrene) with an o-bromostyrene content of less than 40 mole % showed similar behavior<sup>40,44</sup>.

The blends of PPO with poly(styrene-co-p-fluorostyrene) copolymers of p-fluorostyrene content less than 56 mole % were

miscible in all proportions and the same blends with copolymers containing 46-56 % p-fluorostyrene showed phase separation at elevated temperature<sup>5,8</sup>. Copolymers of poly(styrene-co-o-fluorostyrene) with less than 82 % o-fluorostyrene blended with PPO do not show any phase separation<sup>5,8</sup>. In the case of the blends of PPO with poly(styrene-co-o(p)-chlorostyrene), the LCST dropped sharply for the copolymer composition range of 60-75 mole % p-chlorostyrene and the blends of PPO with poly(styrene-co-p-chlorostyrene) with 67 mole % or less p-ClS were miscible<sup>40,42,45</sup>.

Miscibility of polystyrene with random copolymers of poly(o-fluorostyrene-co-p-fluorostyrene)<sup>7,40</sup>, poly(styrene-co-p(o)-fluorostyrene)<sup>5</sup>, poly(styrene-co-p-bromostyrene)<sup>40</sup>, and poly(o-chlorostyrene-co-p-chlorostyrene)<sup>6,46</sup> has been studied. The blend of polystyrene with poly(o-chlorostyrene-co-p-chlorostyrene) showed a great sensitivity to the degree of polymerization of either or both components which could be a result of the very low positive value of the interaction parameter between styrene and o-chlorostyrene<sup>6,46</sup>.

The blend of polystyrene with poly(styrene-co-o-fluorostyrene) was miscible and the blend of polystyrene with poly(styrene-co-p-fluorostyrene) with 46 mole% of p-fluorostyrene showed a single  $T_g$ , but additional proof is needed to verify

miscibility<sup>5</sup>. In the case of the blend of polystyrene with poly(o-chlorostyrene-co-p-chlorostyrene), a miscibility window was found for a copolymer composition of about 68 to 98 mole % o-chlorostyrene at 150 °C<sup>6,46</sup>. The maximum in the miscibility window occurred at a composition of 83 mole % o-chlorostyrene. The temperature dependence of  $\chi$  in this blend was also studied by using polystyrene samples of varying molecular weights.

In the case of the blend of polystyrene with poly(styrene-co-p(o)-bromostyrene), the copolymers of o-bromostyrene and styrene with over 40 mole % o-bromostyrene exhibited two distinct  $T_g$ 's<sup>40</sup>. The copolymer with 20 mole % o-bromostyrene appeared to exhibit a single  $T_g$ . The copolymers of p-bromostyrene and styrene with p-bromostyrene content of over 50 mole % p-bromostyrene were immiscible with polystyrene.

Kambour et al<sup>31</sup> calculated  $\chi_{po,p-BrS}$  to be 0.22 at about 120 °C based on a study of PPO/poly(styrene-co-p-bromostyrene) blends; these workers also studied the blend of polystyrene with brominated PPO. Paul et al<sup>30</sup> studied blends of polyesters which may be considered to be random copolymers of  $CH_x$  and COO units.

The blends of syndiotactic PMMA with random copolymers of isotactic poly(methyl/ethyl methacrylate) have been studied<sup>47</sup>. Only the copolymers with an ethyl methacrylate content below 45 % were miscible with syndiotactic PMMA.

Shiomi et al<sup>11,48</sup> studied blends of chlorinated PVC(CPVC)/poly(ethylene-co-vinyl acetate), CPVC/poly(vinyl chloride-co-vinyl acetate), poly(vinyl chloride-co-vinyl acetate)/poly(ethylene-co-vinyl acetate), and poly(styrene-co-maleic anhydride)/poly(styrene-co-acrylonitrile). Ueda et al<sup>49</sup> studied the miscibility behavior in blends of chlorinated polyethylene which might be treated as random copolymers of  $\text{CH}_2$  and  $\text{CHCl}$  segments and found that these blends exhibited an LCST or UCST depending upon the degree of chlorination and the nominal  $\chi$  between  $\text{CH}_2$  and  $\text{CHCl}$  was also shown to be dependent upon the mean degree of chlorination.

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## CHAPTER II

### PREPARATION AND PROPERTIES OF SULFONYLATED POLY(2,6-DIMETHYL-1,4-PHENYLENE OXIDE) COPOLYMERS

The preparation and properties of a series of novel thermally stable random copolymers of sulfonylated poly(2,6-dimethyl-1,4-phenylene oxide) (SPP0) copolymers starting from poly(2,6-dimethyl-1,4-phenylene oxide) (PPO) were explored. The resulting copolymers blended with styrenic copolymers are represented as  $(C_{1-y}^D y)_{n_2}$  in this work.

Polymer modifications by means of chemical, radiative or mechanochemical methods have received much attention recently. These modifications result in structurally well-defined polymers and copolymers and provide changes in solubility characteristics, surface properties, catalytic activities, increased thermal stability and tailored miscibility.

Several modification reactions of PPO such as bromination<sup>1-3</sup>, carboxylation<sup>4,5</sup>, sulfonation<sup>6,7</sup>, phosphorylation<sup>2,3,8</sup> and vinylation<sup>9</sup> have been reported. These

modification reactions usually yield products with lower thermal stability than that of unmodified PPO.

Friedel-Crafts acylation or sulfonylation reactions have been used to make high performance polymers such as poly(arylene ether sulfones)<sup>10</sup> and poly(arylene ether ketones)<sup>11</sup>. In this chapter the preparation and properties of SPPPO copolymers obtained by a Friedel-Crafts sulfonylation of PPO are presented.

#### A. Experimental Section

##### Materials and Reactions

PPO from General Electric Co., was purified by precipitation in excess methanol from 5% toluene solution and then dried in a vacuum oven at 100°C. The measured intrinsic viscosity was 0.52 dl/g ( $\text{CHCl}_3$ , 25°C).

Nitrobenzene was distilled and the middle fraction (b.p. 86°/10 mm Hg) was collected. Anhydrous aluminum chloride (Fisher Scientific) and benzenesulfonyl chloride (Eastman Organic Chemicals) were used as received.

A series of SPPO copolymers was prepared by varying the ratios of benzenesulfonyl chloride to PPO. The reaction scheme is depicted in Figure 2.1.

A typical run for a theoretical degree of sulfonylation of 45 mole % degree of sulfonylation, was as follows :

In a four neck flask was dissolved 10.0 g of PPO in 120 ml of nitrobenzene and 5.5 g of  $\text{AlCl}_3$  was added. After the catalyst was dissolved, 6.6 g of benzenesulfonyl chloride was added gradually and the temperature was kept at  $45^\circ\text{C} \pm 1^\circ$ . After 27 hours the aluminum chloride complex was destroyed by adding the reaction mixture dropwise to methanol acidified with 4 volume % of HCl. The precipitated polymer was filtered and washed with additional acidified methanol and water and dried.

The product was finally reprecipitated into methanol from THF solution and then redried in a vacuum oven. A control sample was prepared in the same manner for 60 hours without adding benzenesulfonyl chloride, except that chloroform was used as a solvent during the reprecipitation process.

Characterization. The degree of sulfonylation was determined from the sulfur to carbon ratio based on elemental analyses performed by the University of Massachusetts Microanalysis Laboratory.

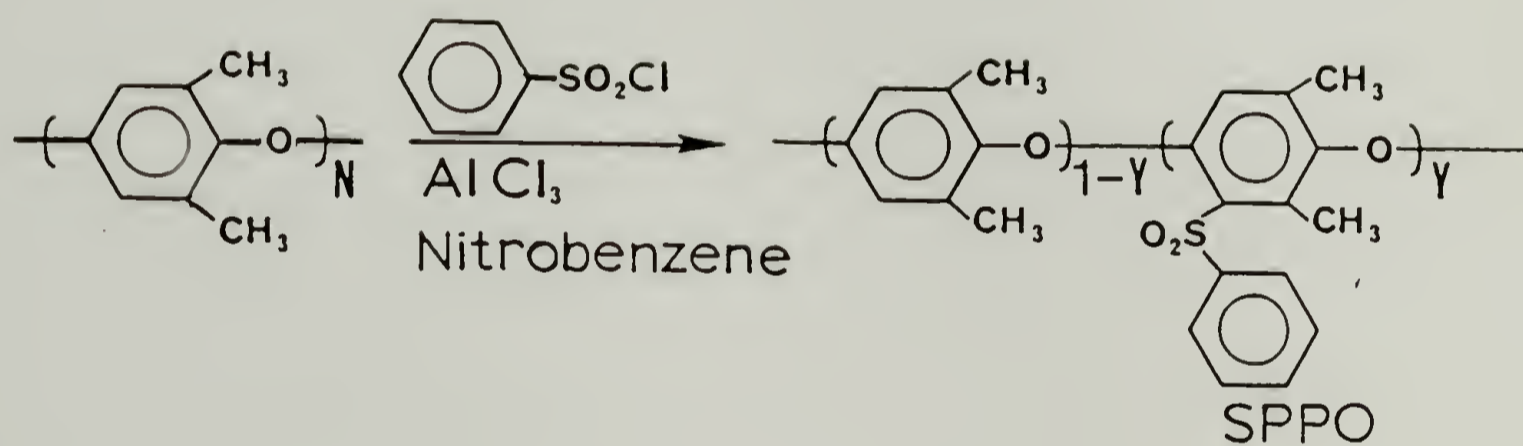


Figure 2.1. Schematic diagram of the modification reaction of PPO

Molecular weights, based on calibration with monodisperse polystyrene standards (Polymer Laboratories), were determined on a Waters Associate 150-C ALC/GPC interfaced with a Data Module. The eluant for SPP0 was THF delivered at  $1.0 \text{ ml min}^{-1}$  at ambient conditions.

Densities of the copolymers in the form of cast films were measured at  $23^{\circ}\text{C}$  using a density gradient column. The linear gradient column was prepared from a solvent mixture of carbon tetrachloride and heptane and calibrated over a range of densities from  $1.02$  to  $1.26 \text{ g cm}^{-3}$  with calibrated glass beads.

Infrared spectra were obtained using KBr pellets in a Perkin-Elmer 1320 infrared spectrophotometer.

$^1\text{H}$ -NMR spectra were recorded on a Varian XL-300 NMR spectrometer with tetramethyl silane as an internal standard. All samples were examined in  $\text{CDCl}_3$  solutions.

DSC measurements were performed on a Perkin-Elmer DSC 7 microcalorimeter controlled by a Perkin-Elmer 7500 computer at a heating rate of  $20^{\circ}\text{C/min}$  under nitrogen and indium was used as a standard.  $T_g$  was taken as the inflection point of the  $\Delta C_p$ , the specific heat increment at the glass transition.  $\Delta C_p$ 's were averaged for at least two runs.

Thermogravimetric measurements of the powdered samples were made using a Perkin-Elmer TGS-2 thermobalance with a heating rate of  $10^{\circ}\text{C}/\text{min}$  under nitrogen. The samples were predried at  $200^{\circ}\text{C}$  for 20 min in the TGA furnace to remove any absorbed water.

Dynamic mechanical measurements were carried out with a Polymer Laboratories DMTA operated in the three point bending mode with a strain amplitude of  $60\mu\text{m}$ . The SPPPO copolymer films, which were cast from chlorobenzene solution and dried in a vacuum oven, were annealed above  $T_g$  in the DMTA furnace to remove any residual solvent and analyzed over the frequency range 0.1 Hz to 30 Hz under a nitrogen atmosphere. Measurements were carried out in the temperature range  $-140^{\circ}\text{C}$  to  $280^{\circ}\text{C}$  at a heating rate of  $1.5^{\circ}\text{C}/\text{min}$ . After completion of dynamic mechanical measurements on a dried sample with a degree of sulfonylation of 38.8 wt%, the sample was immersed in distilled water at room temperature for 7 days. The wet sample was removed, and the excess water was wiped off with filter paper. The water uptake was determined to be 0.25 % by weighing.

PPO powders were compression molded into films at  $280^{\circ}\text{C}$  under nitrogen and annealed above  $T_g$  in the DMTA furnace before dynamic mechanical measurements.

Dielectric measurements for the SPPPO copolymer samples (degree of sulfonylation 38.8 wt%), which were obtained as described

above, were carried out with a General Radio model 1689M RLC Digibridge at 50 KHz over a temperature range from  $-155^{\circ}$  to  $280^{\circ}\text{C}$  with a nitrogen purge. The temperature was raised at a rate of  $2.0^{\circ}\text{C}/\text{min}$ . Samples approximately 0.1 mm in thickness were employed with an active electrode cell diameter of 3.3 cm.

## B. Results and Discussion

Figure 2.2 shows the degree of sulfonylation determined by elemental analysis versus the theoretical degree of sulfonylation given by the molar ratio of benzenesulfonyl chloride to PPO. As the degree of substitution increases, it is more difficult to reach higher conversion since unreacted sites for further reaction are screened by the neighboring reacted units. Thus, longer reaction times and increased amounts of benzenesulfonyl chloride were required for higher degrees of sulfonylation.

Table 2.1 shows the molecular weight characteristics of PPO and a series of SPPO copolymers. The weight average molecular weight of SPPO copolymers increases with the degree of sulfonylation.

SPPO 90, the copolymer with the highest degree of sulfonylation, is soluble in a variety of organic solvents. At a solution concentration of 5 wt% it is soluble in THF, chlorobenzene,

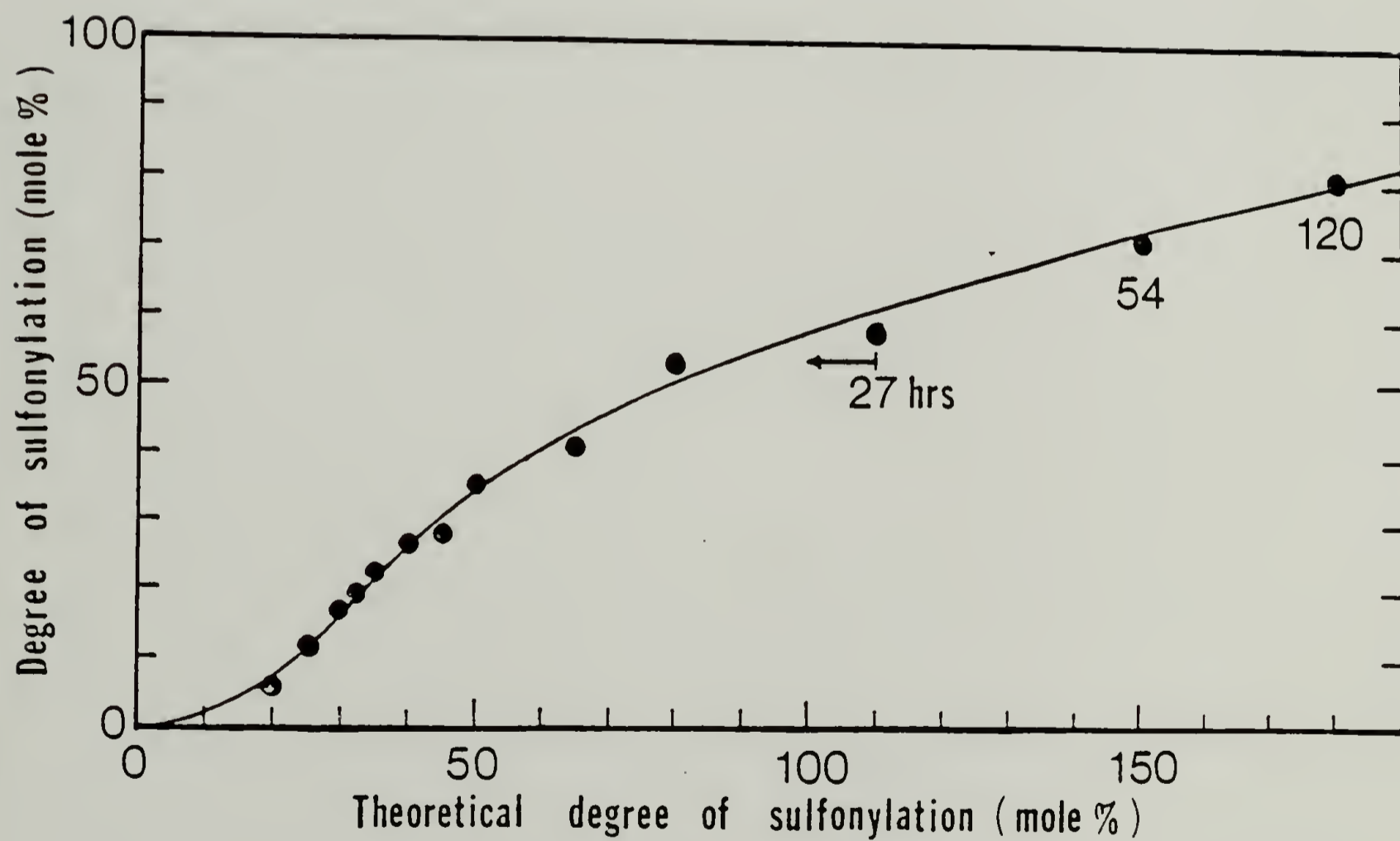


Figure 2.2. Degree of sulfonylation vs. theoretical degree of sulfonylation. The numbers 27, 54 and 120 indicate reaction times in hours

Table 2.1

Molecular Weights of Sulfonated  
Poly(2,6-dimethyl-1,4-phenylene oxide) Copolymers

	$\overline{M}_n \times 10^{-4}$	$\overline{M}_w \times 10^{-4}$	$\overline{M}_w/\overline{M}_n$
PPO <sup>a)</sup>	1.72	3.50	2.03
SPPO 12	1.83	4.21	2.30
SPPO 24	1.73	4.85	2.80
SPPO 30	1.58	4.42	2.80
SPPO 34	1.60	4.40	2.75
SPPO 39	1.51	4.85	3.21
SPPO 44	1.65	5.49	3.33
SPPO 47	1.99	5.80	2.91
SPPO 54	2.60	6.24	2.40
SPPO 55	2.52	6.08	2.41
SPPO 60	2.44	7.81	3.20
SPPO 72	2.56	8.07	3.15
SPPO 75	2.50	7.33	2.93
SPPO 85	2.48	8.72	3.52
SPPO 90	2.79	8.81	3.16

a) Toluene was used as an eluant.

nitrobenzene, chloroform, N,N-dimethyl acetamide, dimethyl sulfoxide, and N-methylpyrrolidone but is insoluble in acetone, toluene, and carbon tetrachloride at room temperature.

Figure 2.3 shows the variation of the density of SPP0 as a function of the degree of sulfonylation. No evidence of swelling or dissolution of samples in mixed solvents was observed even after a month of immersion. The densities of the SPP0 copolymers increase linearly with the degree of sulfonylation. By extrapolation the density of a completely sulfonylated homopolymer is estimated to be  $1.26 \text{ g cm}^{-3} \pm 0.005$ . The density of PPO ( $1.09 \text{ g cm}^{-3}$ ) compares well with the value of  $1.066 \text{ g cm}^{-3}$  determined by Fried<sup>12</sup>.

The structure of these modified materials was confirmed by infrared and  $^1\text{H}$ -NMR spectra. Figure 2.4 shows the infrared spectra of unmodified PPO and one of its sulfonylated derivatives. Only the region ranging from  $600\text{--}1600 \text{ cm}^{-1}$  is shown for clarity of display since little change could be seen in other regions. The SPP0 copolymer exhibits new  $\text{-SO}_2\text{-}$  absorption peaks at  $1150 \text{ cm}^{-1}$ .

Figures 2.5, 2.6 and 2.7 show  $^1\text{H}$ -NMR spectra of PPO and some SPP0 copolymers. Based on a series of spectra, chemical shift assignments have been made and are shown in Figure 2.6. In comparison to the starting PPO, pendant aromatic protons located at

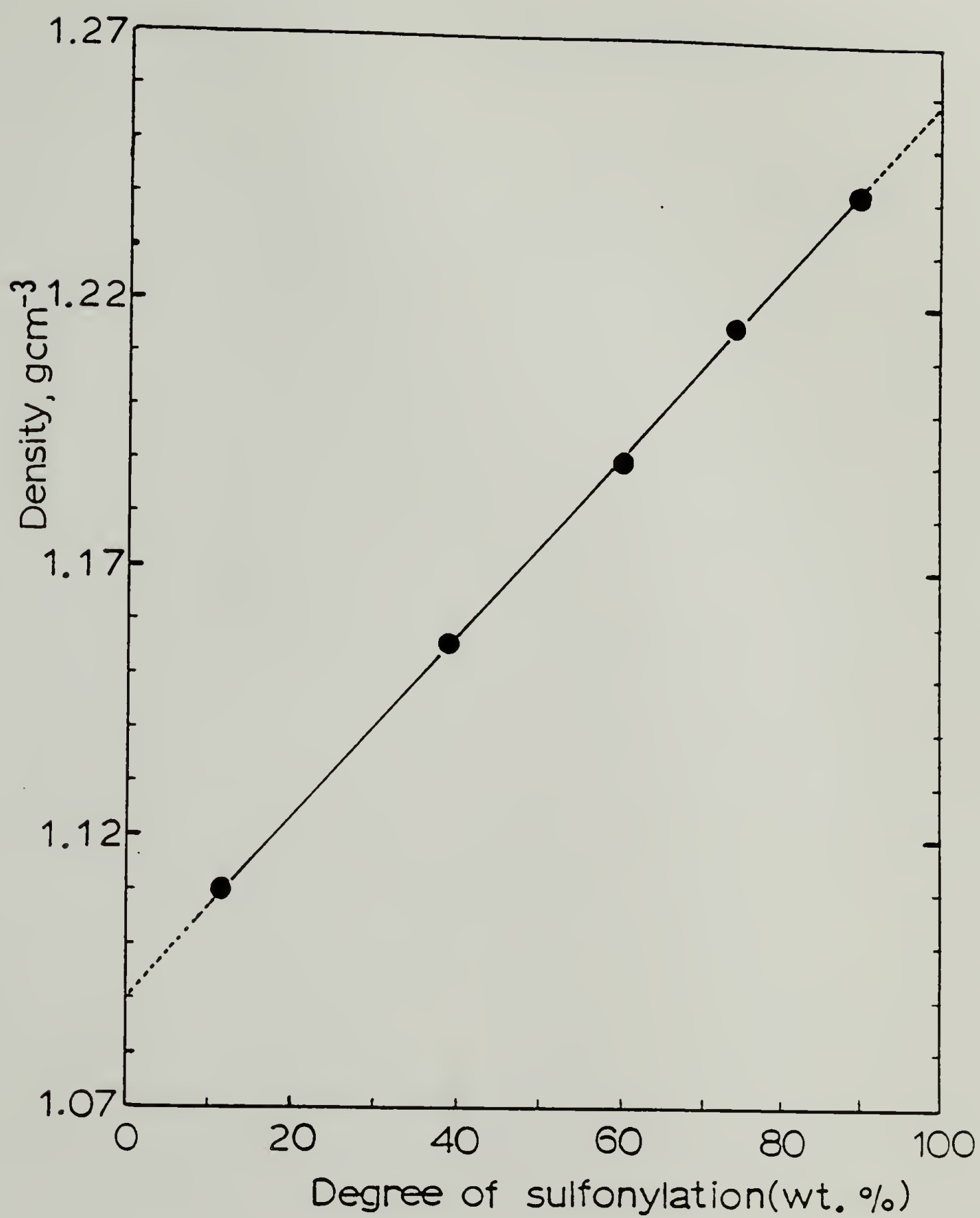


Figure 2.3. Density of SPP0 copolymers vs. degree of sulfonylation

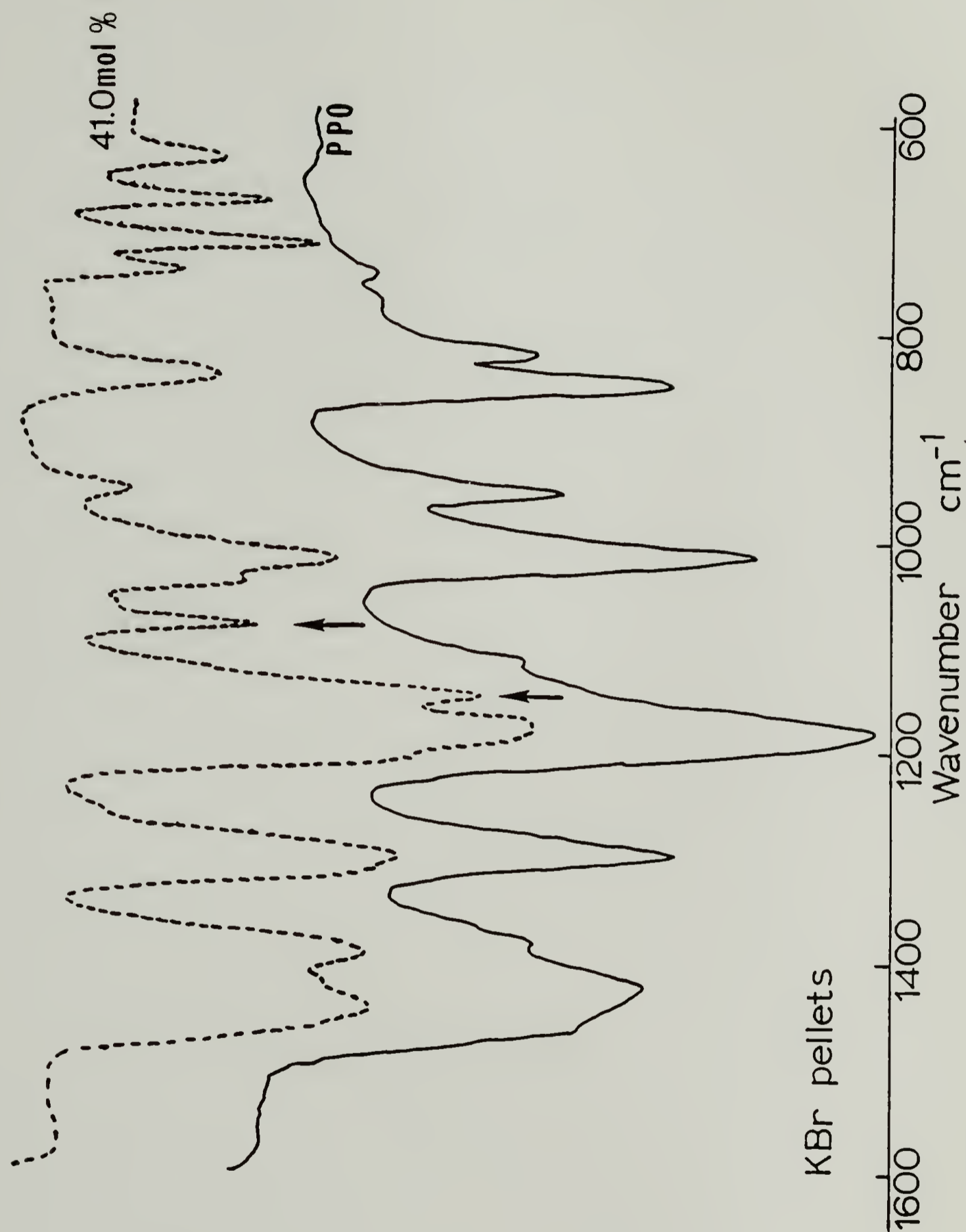
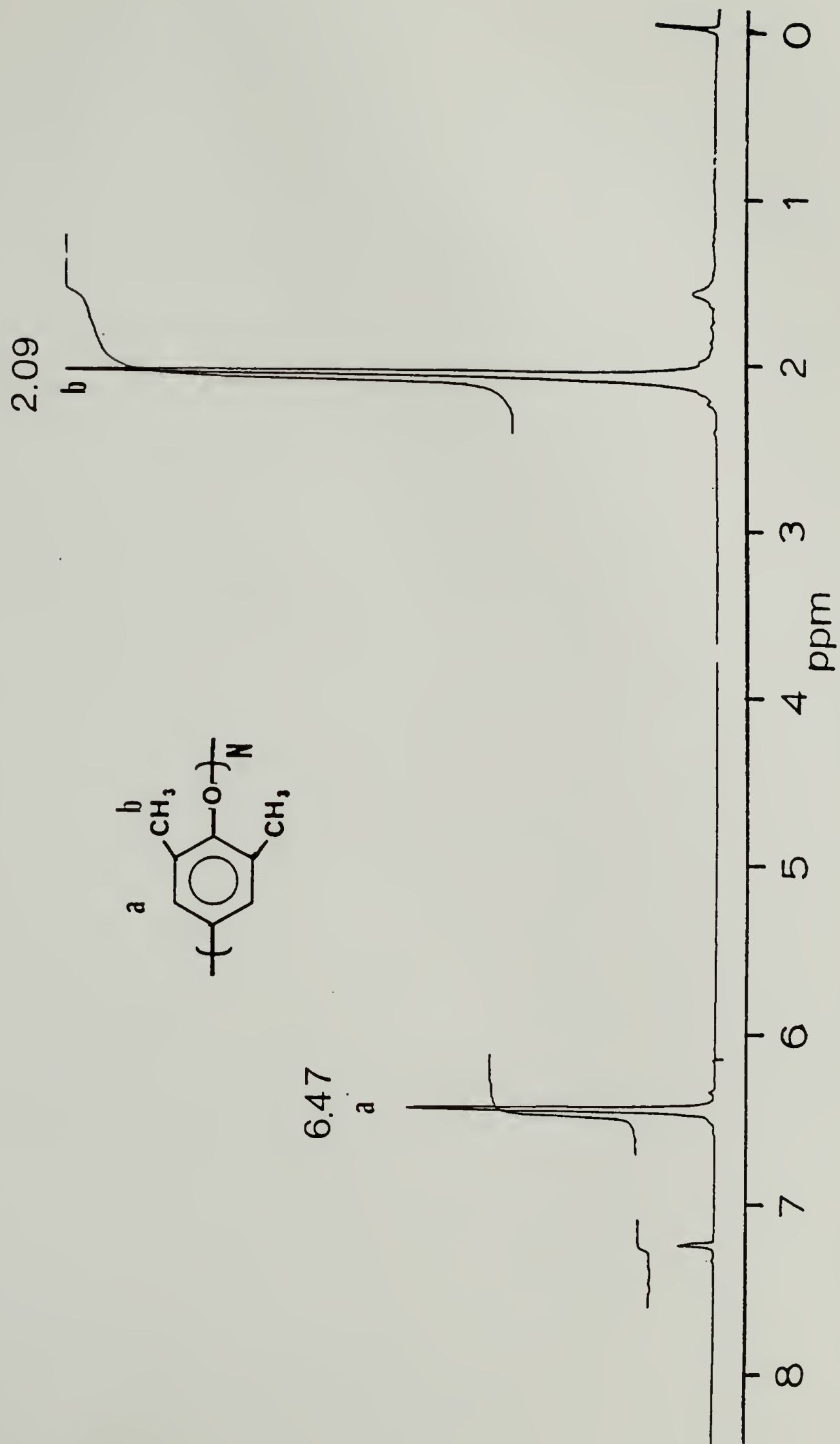


Figure 2.4. IR spectra of PPO (solid line) and sulfonated PPO, degree of sulfonation: 41.0 mole% (broken line)

Figure 2.5.  $^1\text{H-NMR}$  spectrum of PPO

35.2 mol %

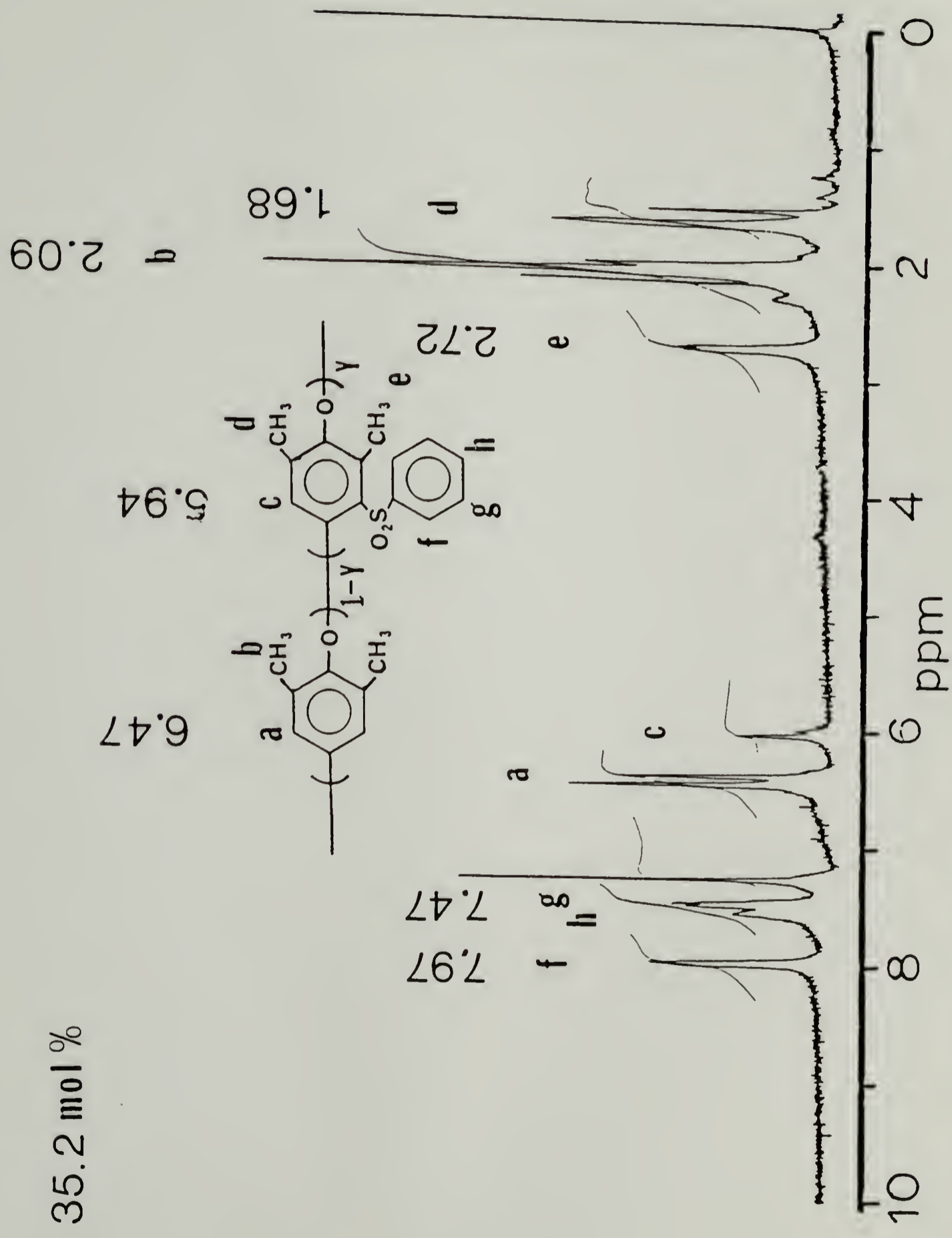


Figure 2.6.  $^1\text{H}$ -NMR spectrum of sulfonated PPO; degree of sulfonation: 35.2 mol %

80.2 mol %

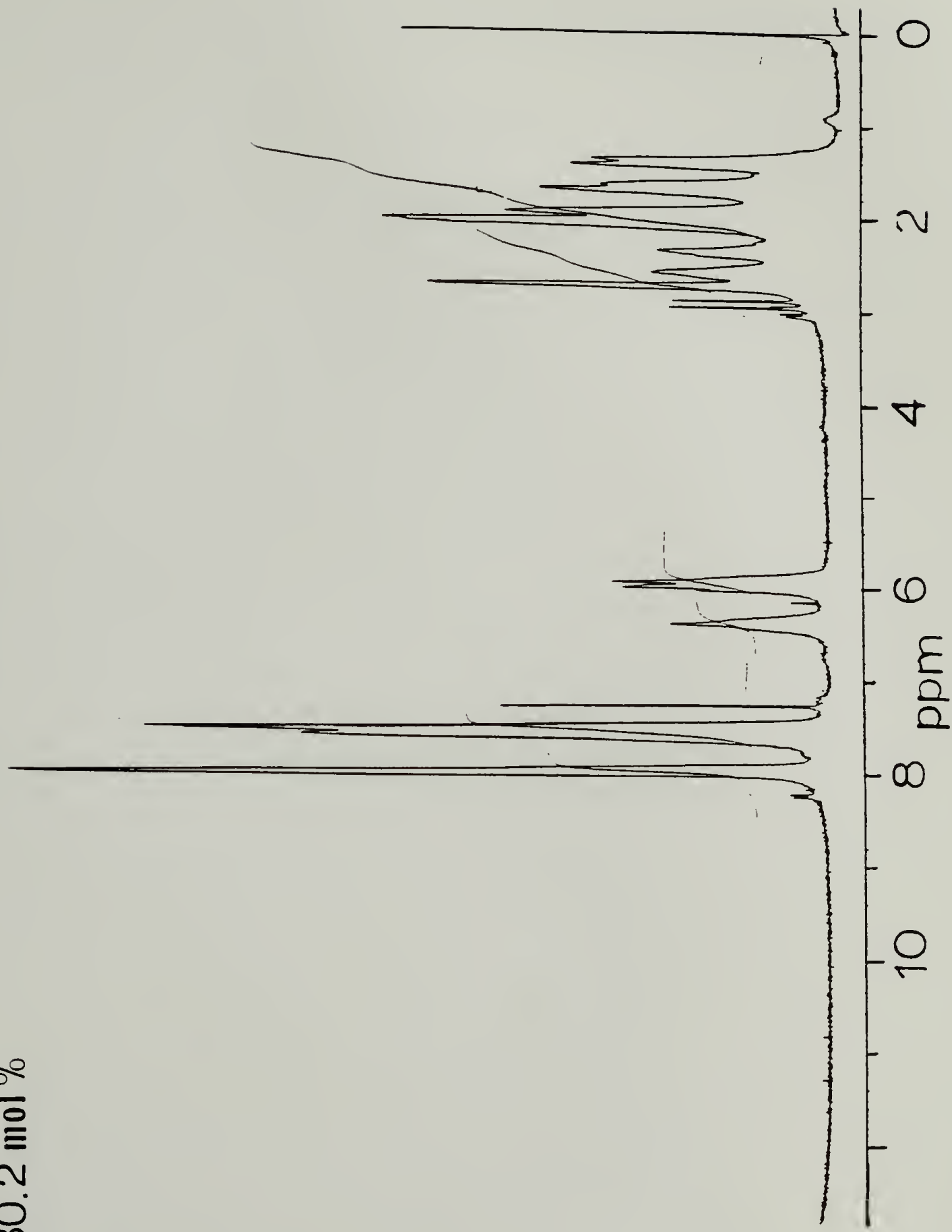


Figure 2.7.  $^1\text{H}$ -NMR spectrum of sulfonated PPO; degree of sulfonation: 80.2 mole%

ortho, meta and para positions to the electron withdrawing sulfone group in the SPP0 copolymer are resolved at 7.97, 7.47 and 7.60 ppm, respectively.

Some of the physical properties of a series of SPP0 copolymers are tabulated in Table 2.2, where the range of error in the measurement of  $\Delta C_p$  is estimated to be less than 10 %. Figure 2.8 shows that the glass transition temperature ( $T_g$ ) increases linearly with the weight percent of sulfonylation. The control sample exhibited the same  $T_g$  and infrared spectrum as those of PPO itself, which implies that no competing side reactions or chain degradation take place.

Many attempts<sup>13-15</sup>, mostly empirical in nature, have been made to predict the effect of composition on the  $T_g$ 's of random amorphous copolymers. Assuming that copolymers behave like solutions of small molecules with regard to packing behavior and that the relationship of ideal volume-additivity of the repeating units in the copolymers holds and taking into account the thermal expansion in the glassy and rubbery states, Gordon and Taylor<sup>13</sup> derived the relation.

$$T_g = [T_{g_1} + (kT_{g_2} - T_{g_1})W_2] / [1 + (k - 1)W_2] \quad (2.1)$$

Table 2.2

Properties of Sulfonylated Poly(2,6-dimethyl-1,4-phenylene oxide)  
Copolymers

Sample	Degree of Sulfonylation		$T_g$ °C	$\Delta C_p$ J/g/deg	Transition		Density g cm <sup>-3</sup>
	Mole %	Wt %			Width <sup>a)</sup>	°C	
PPO	0	0	218	0.217	7.4		
SPPO 12	5.8	11.8	227	0.187	7.8		1.110
SPPO 24	12.4	23.5	234	0.172	12.0		
SPPO 30	16.8	30.4	244	0.162	8.6		
SPPO 34	19.2	34.0	247	0.159	9.6		
SPPO 39	22.6	38.8	251	0.153	12.6		1.156
SPPO 44	26.2	43.5	255	0.150	11.8		
SPPO 47	28.7	46.6	257	0.141	9.2		
SPPO 54	35.2	54.1	259	0.138	9.2		
SPPO 55	35.6	54.5	261	0.134	9.8		
SPPO 60	41.0	60.1	266	0.129	11.8		1.190
SPPO 72	53.6	71.5	272	0.110	11.6		
SPPO 75	57.6	74.6	279	0.104	11.0		1.216
SPPO 85	71.6	84.5	287	0.095	10.4		
SPPO 90	80.2	89.8	293	0.070	14.0		1.241

a) Transition width was determined from twice the difference,

$$T_g - T_{g, \text{onset}}$$

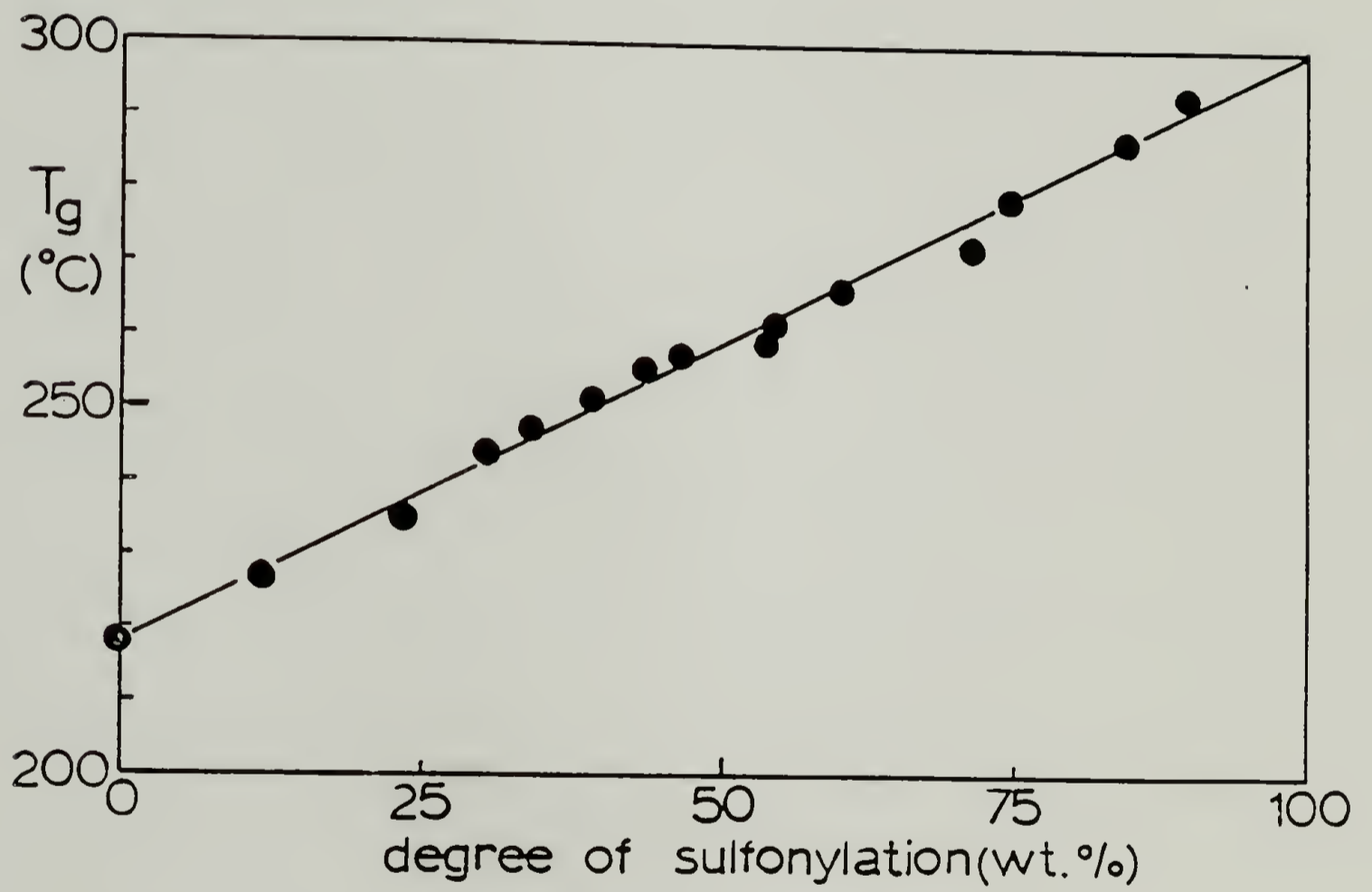


Figure 2.8. Glass transition temperature vs. degree of sulfonylation

where  $k$  is an empirical constant and  $W_2$  is the weight fraction of component 2. As can be seen in Figure 2.8, the best fit of the experimental results is given by the Gordon-Taylor equation with  $k=1$ . The extrapolated  $T_g$  of a completely sulfonylated homopolymer is seen to be  $300^\circ\text{C}$ . PPO itself obeys freely rotating chain statistics on an intramolecular basis i.e., there is little hindrance to rotation about the oxygen ether bonds in the main chain. Dielectric relaxation studies by Karasz et al<sup>16</sup> and conformational energy calculations by Tonelli<sup>17</sup> confirm this concept of free rotation in PPO.

The intermolecular forces and the chain packing play a decisive role in affecting the molecular motion in the glassy state<sup>2</sup>. In the case of the SPPPO copolymers, it is reasonable to assume that the bulky and very polar phenyl sulfone group attached to the phenylene oxide unit has the effect of increasing the  $T_g$  of the SPPPO copolymer by raising the intermolecular and steric barrier to the rotation of monomer units.

$\Delta C_p$ , the specific heat increment at  $T_g$  per unit mass, decreases linearly with the degree of sulfonylation, as shown in Figure 2.9. This behavior has also been reported for random

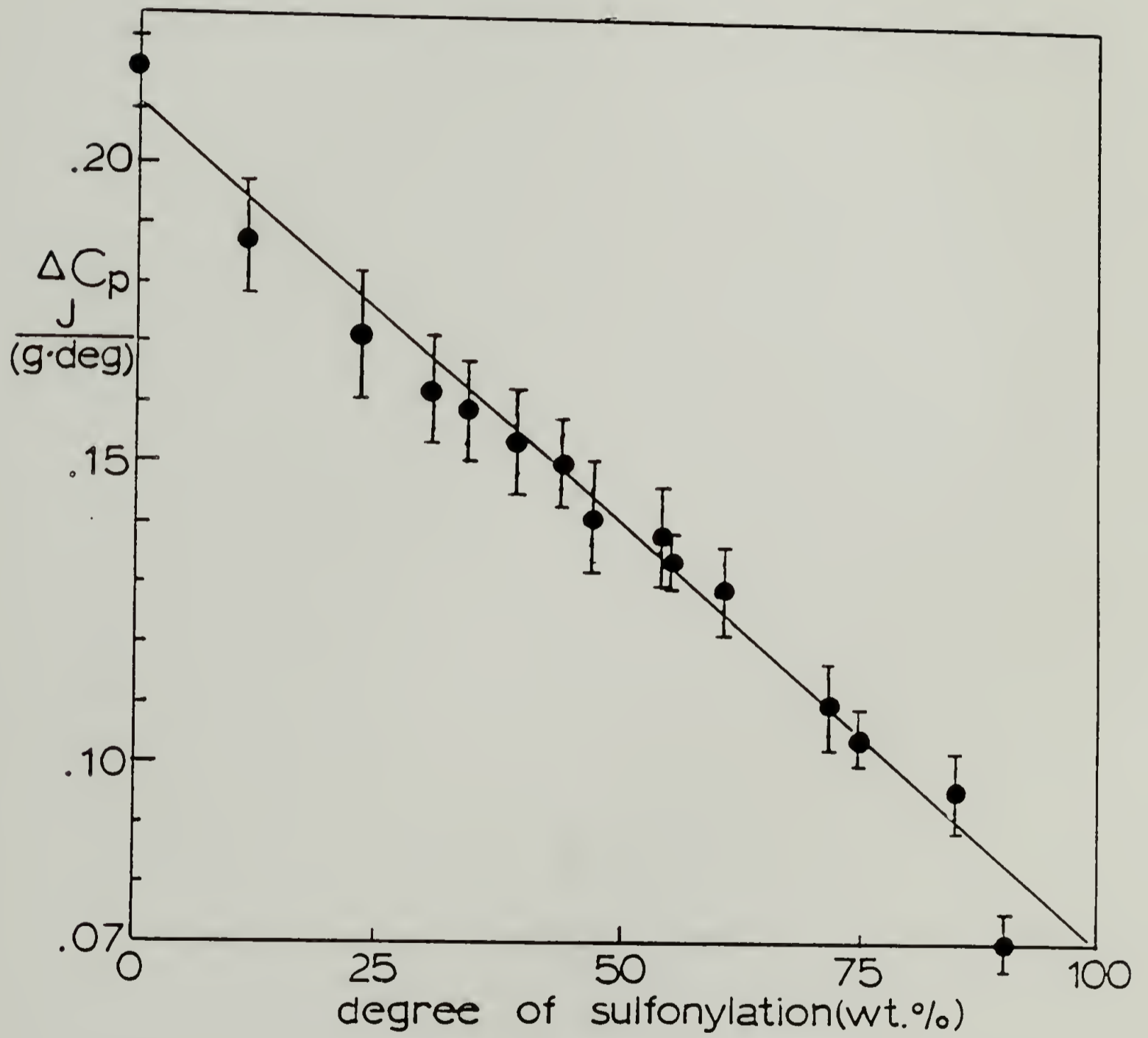


Figure 2.9.  $\Delta C_p$ 's of SPP0 copolymers vs. degree of sulfonylation

copolymers of poly(o-fluorostyrene-co-p-fluorostyrene)<sup>18</sup> and also for some miscible blends<sup>12,18</sup>. i.e.,

$$\Delta C_p = W_1 \Delta C_{p_1} + W_2 \Delta C_{p_2} \quad (2.2)$$

where  $W_i$  is the weight fraction of component  $i$ .

Figure 2.10 compares TGA traces of PPO and some modified PPO's. The data for phosphorylated PPO were cited from ref. 19. The thermal stability of PPO has been found not to decrease upon sulfonylation. SPPO copolymers with the degree of sulfonylation of 71.5 wt% start to lose weight at 370°C and experience a 10 % weight loss when a temperature of 470°C is reached. Figure 2.11 shows the temperatures of indicated weight loss for a series of the SPPO copolymers. These temperatures appear to be nearly independent of the degree of sulfonylation, which is unusual in the light of previous results on other derivatives which showed that substitution onto PPO decreased both thermal and oxidative stability<sup>20</sup>.

The temperature dependences of the storage moduli ( $E'$ ), loss moduli ( $E''$ ), and loss factor ( $\tan \delta$ ) at 10 Hz for PPO, dry and wet samples of SPPO copolymer (both with a degree of sulfonylation of 38.8 wt%) are shown in Figures 2.12, 2.13 and 2.14, respectively.

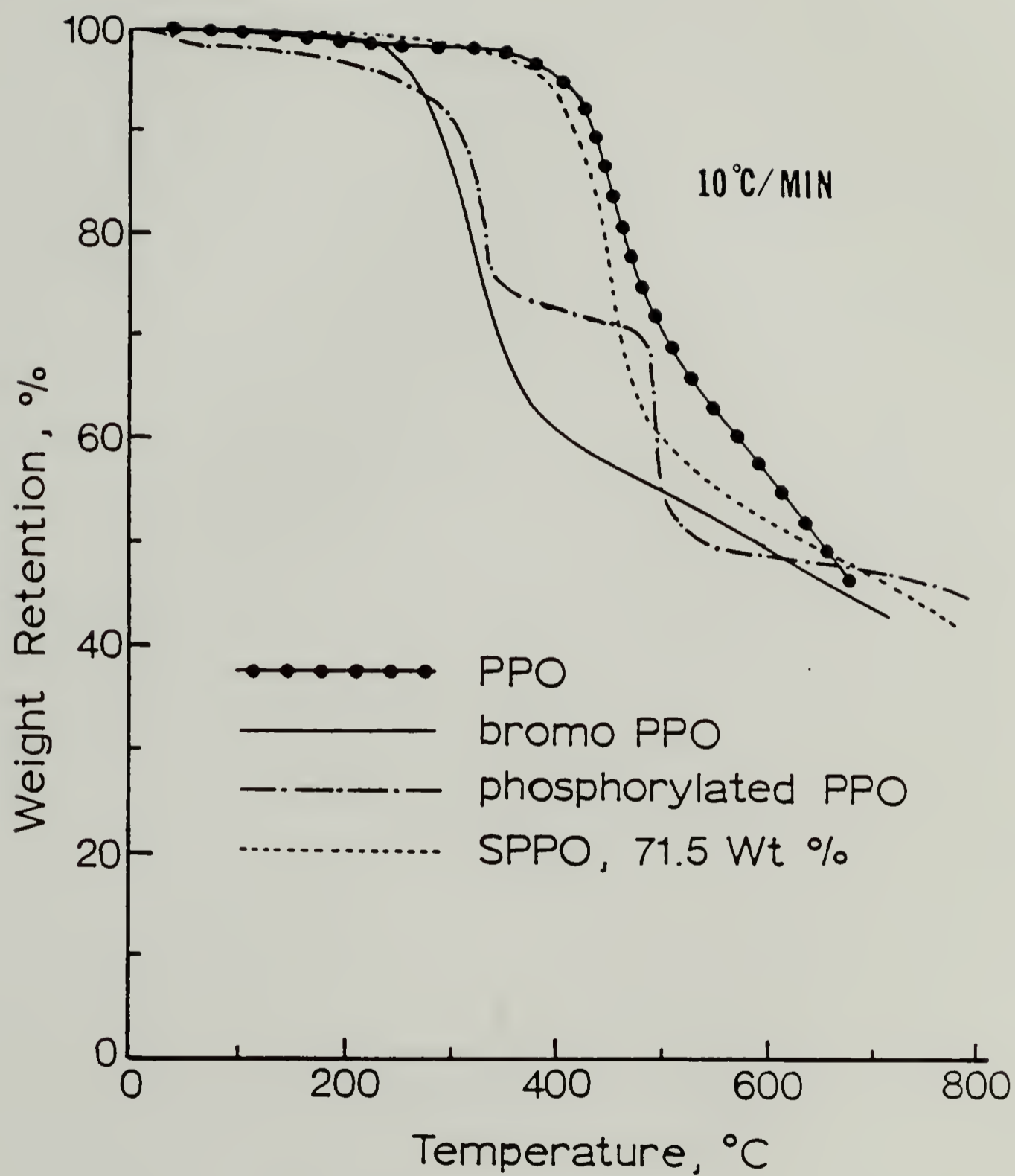


Figure 2.10. Thermogravimetric analysis of PPO and some modified PPO's

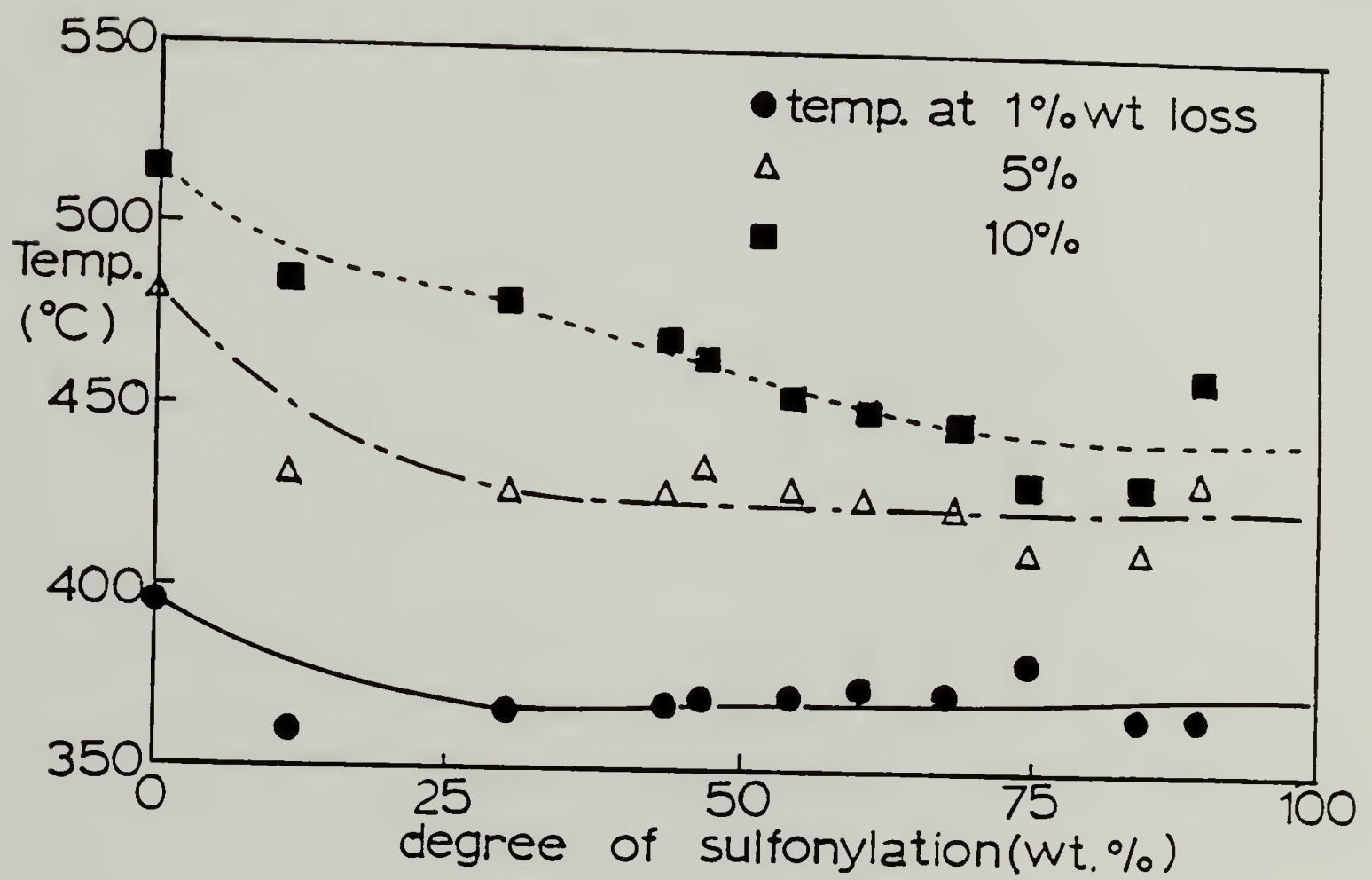


Figure 2.11. Temperatures of indicated weight loss in sulfonylated PPO during heating at  $10^{\circ}\text{C min}^{-1}$

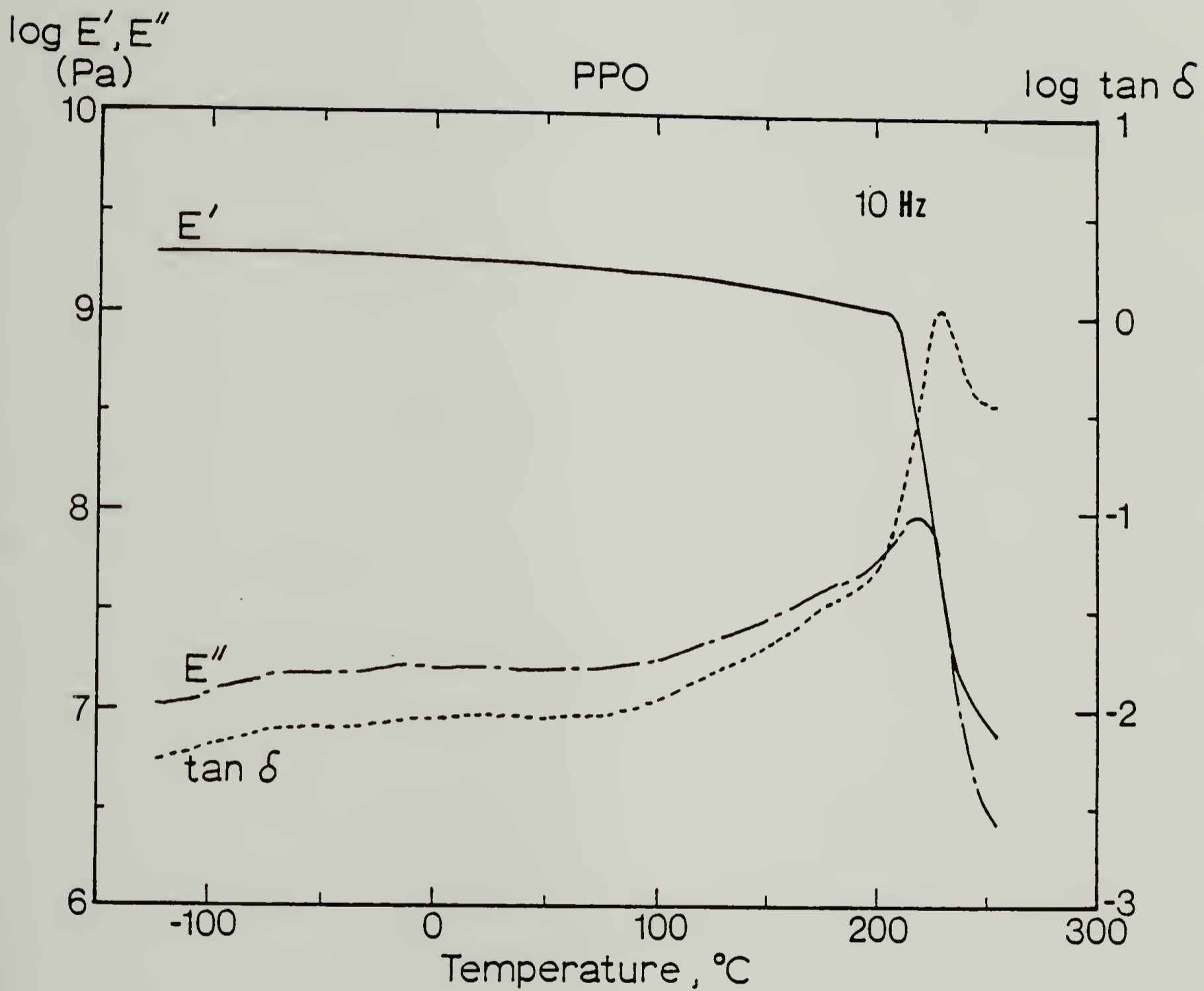


Figure 2.12. Temperature dependences of mechanical  $E'$ ,  $E''$  and  $\tan \delta$  for PPO at 10 Hz

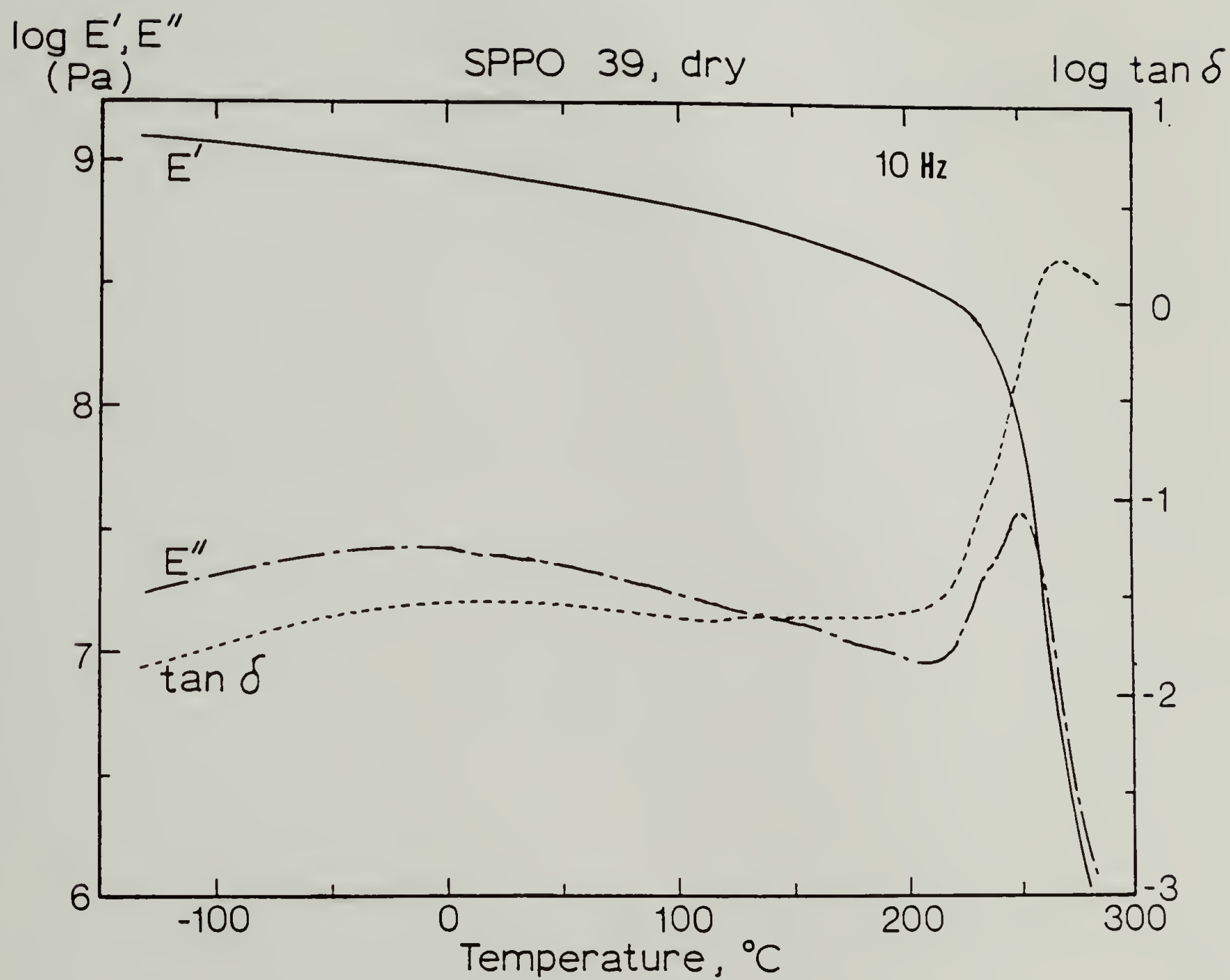


Figure 2.13. Temperature dependences of mechanical  $E'$ ,  $E''$  and  $\tan \delta$  for dry SPP0 39 at 10 Hz

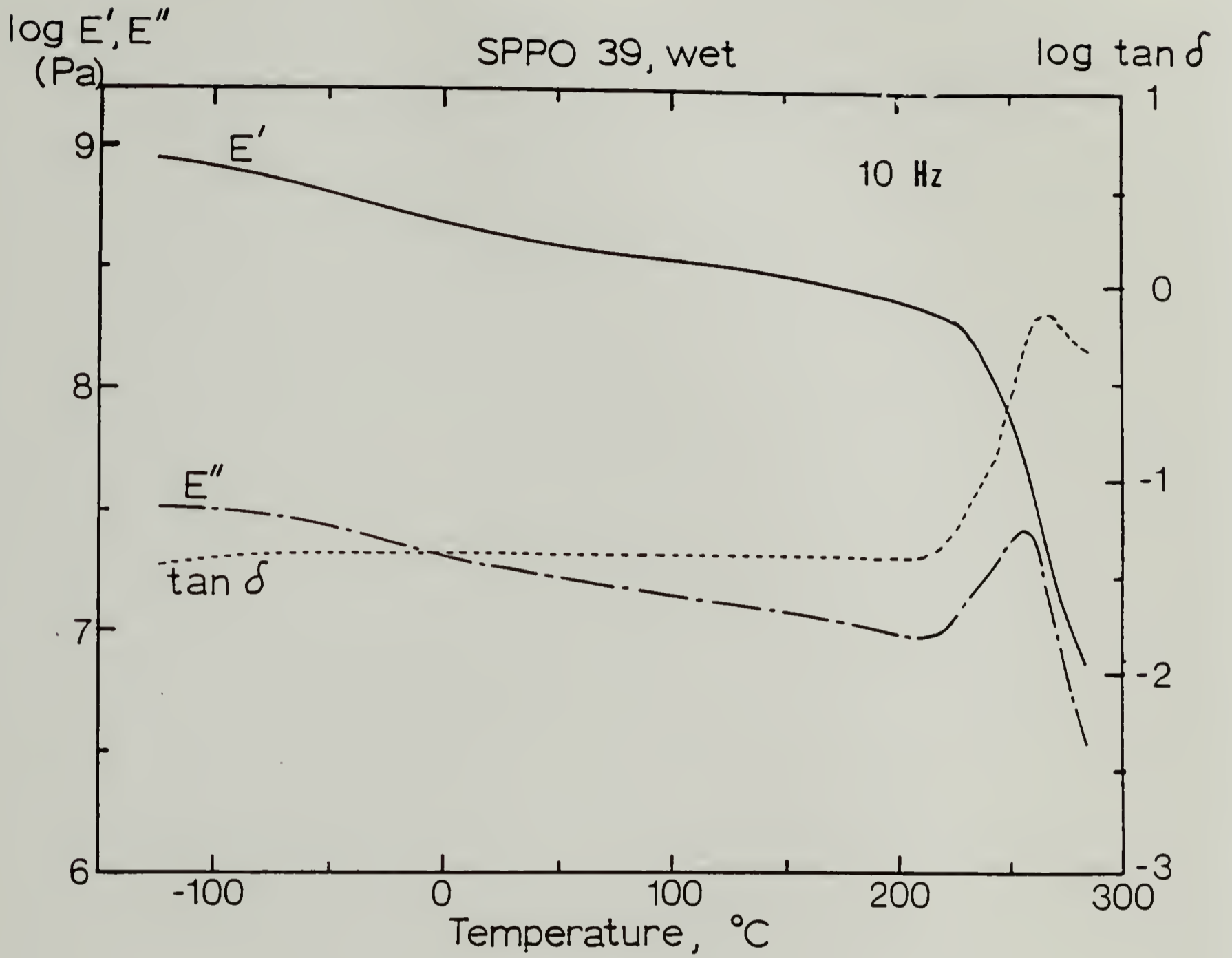


Figure 2.14. Temperature dependences of mechanical  $E'$ ,  $E''$  and  $\tan \delta$  for wet SPP0 39 at 10 Hz

In contrast to previous results<sup>21-24</sup> which showed that PPO exhibited three mechanical relaxations, in the temperature range employed in the current study, only one  $\alpha$ -relaxation associated with the glass-rubber transition around 230°C was observed as shown in Figure 2.12. The storage moduli for the three samples decrease with increasing temperature and show a marked decrease around  $T_g$ . In addition, a slight decrease of the storage modulus for the SPP0 copolymer can be observable in the presence of water. The  $\tan \delta$  peak maximum for the SPP0 copolymer around 260°C is indicative of the  $\alpha$ -relaxation process associated with the glass transition involving the onset of long-range segmental motions of the main chain. This temperature compares well with the  $T_g$  (251°) measured by DSC if frequency differences are taken into account.

The very broad low-temperature  $\beta$ -relaxation, which is spread over several decades of temperature centered around -10°C, is readily observed for the dry SPP0 copolymer, as shown in Figure 2.13. However, the  $\beta$ -relaxation for the wet sample, as seen in Figure 2.14, is not observed. The  $\alpha$ -relaxation peak position for the wet sample decreased only slightly (2°C) compared with that of the dry sample owing to gradual redrying during the measurements. However, the removal of water by annealing in the DMTA furnace regenerated a distinct broad  $\beta$ -relaxation.

Any motion of the polymer segment in a localized lattice, absorbed species, impurities or structural irregularities are known to be associated with low temperature relaxation<sup>25</sup>. In the case of the poly(arylene ether sulfones) the amplitude of  $\beta$ -relaxation was found to increase as the water content increased<sup>26</sup> probably because of the participation of absorbed water in hydrogen bonds to polar groups.

In contrast to poly(arylene ethers) bearing polar groups on the main chain, rather peculiar behavior was observed for the SPP0 copolymer. In particular, the secondary  $\beta$ -relaxation disappeared in the presence of water. The association of water with the pendant sulfone group may cause either average motion of the phenyl sulfone group to become slower by structure tightening, or a hindrance of the local motion which gives rise to the  $\beta$ -relaxation.

It has been reported that the addition of water and methanol to nylon decreases the amplitude of the  $\gamma$ -relaxation and shifts it to slightly lower temperature<sup>27</sup>. This effect was ascribed to the formation of mechanically stable bridges between amide groups in adjacent chains and water acting as an antiplasticizer.

The decrease in the amplitude of the  $\beta$ -relaxation has been observed in bisphenol A-polysulfone by the addition of 4,4'-dichlorodiphenyl sulfone<sup>28-30</sup>, which is known to act as an

antiplasticizer of the polysulfone. The similar suppression of the  $\beta$ -relaxations of bisphenol A-polycarbonate with added antiplasticizer has also been observed<sup>31</sup>. However, there are not enough data at present to suggest that water acts as an antiplasticizer in the SPPO copolymer.

For the SPPO copolymer, there are several possible local motions which could be responsible for the  $\beta$ -relaxation. First, there may be local motion of the pendant phenyl sulfone groups. Second, a local twisting motion of the ether group proposed by Yamafuji et al<sup>32</sup> may occur. Third, methyl group motion may cause a local mode process.

According to Schaefer et al<sup>33</sup> a ring flip process is not permitted for the stiffer PPO main chain. Broad line NMR studies on PPO<sup>34</sup> revealed that the methyl groups are in motion at  $-180^{\circ}\text{C}$ . Thus, local motions of the phenyl sulfone groups appear to be the source of the very broad  $\beta$ -relaxation at  $-10^{\circ}\text{C}$ . In addition, this motion is considered not to be entirely intramolecular since it depends on the surroundings of the sulfone group.

The temperature dependence of dielectric  $\epsilon''$  for the SPPO copolymer with a degree of sulfonylation of 38.8 wt%, as shown in Figure 2.15, supports this hypothesis, although dc conductive loss<sup>35</sup>

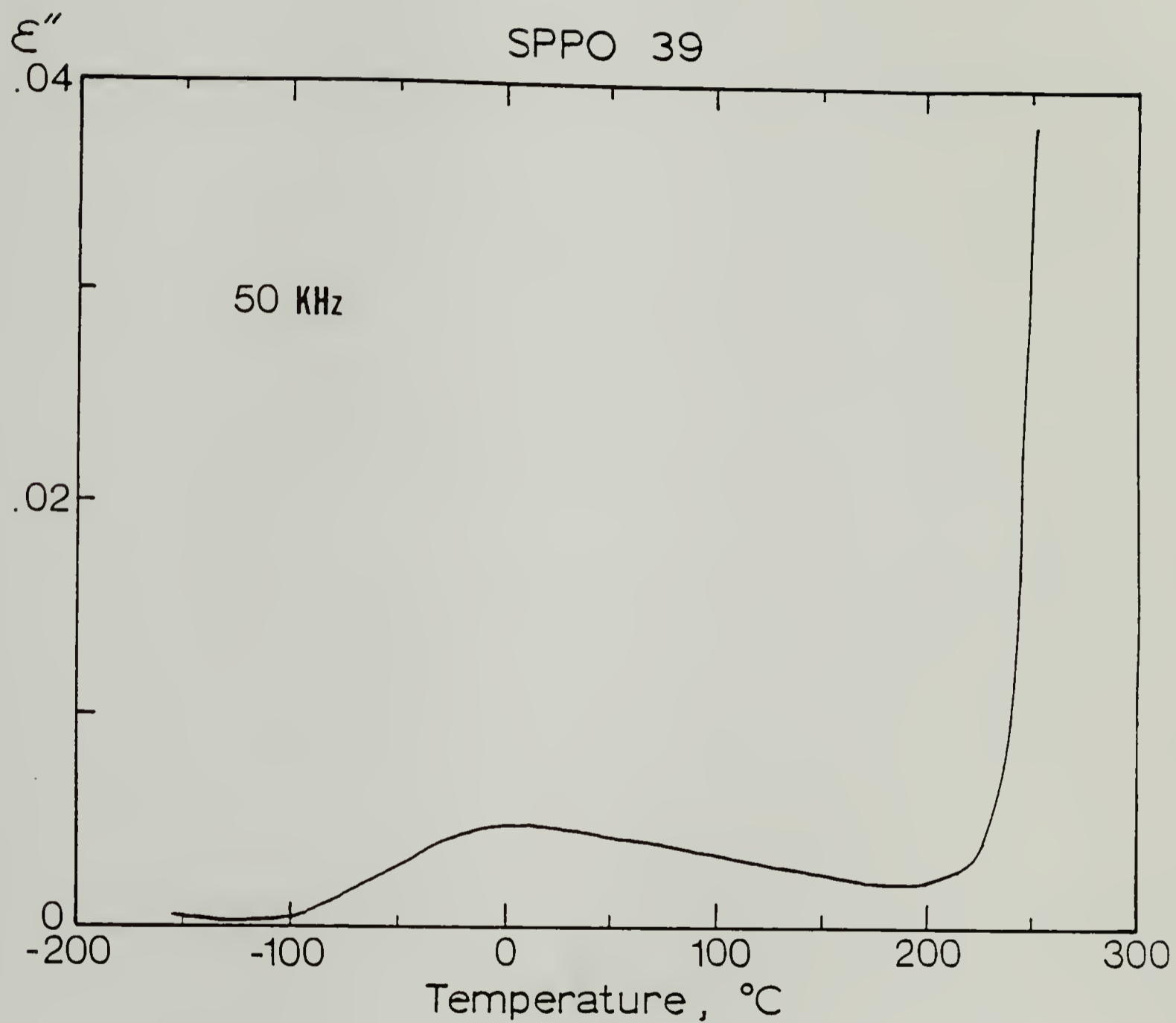


Figure 2.15. Temperature dependences of dielectric  $\epsilon''$  for dry  
SPP0 39 at 50 KHz

is seen to be significant at higher temperatures. The broad secondary  $\beta$ -relaxation at 0°C can be clearly seen. The height of the dielectric  $\epsilon''$  peak is on the order of  $10^{-2}$ . It is noted that the amplitude of the  $\beta$ -relaxation of SPPO is quite large compared to that of PPO, which may be due to the contribution of the dielectrically active sulfone group.

In the case of PPO low-temperature dielectric relaxation was reported to appear at -100°C, and its molecular origin is uncertain<sup>16</sup>. The height of the dielectric  $\epsilon''$  for  $\gamma$ -relaxation is only  $3 \times 10^{-3}$ ; the low intensity of the relaxations is ascribed to the relatively nonpolar nature of PPO.

Accordingly, a localized mode of the dipolar sulfone group appears to be responsible for the  $\beta$ -relaxation of the SPPO copolymer at 0°C. The temperature shift of the dielectric  $\beta$ -relaxation compared with the dynamic mechanical  $\beta$ -relaxation can be understood by taking into account the frequency difference or the differing relative contribution of dipolar and mechanical motions of the pendant tetrahedral sulfone group, whose exact nature of motion is unknown.

The activation energies for the mechanical  $\alpha$ -relaxation of the PPO and SPPO copolymer were compared from the multiple frequency run using the relation :

$$-E_a/2.3R = d \log f / d(1/T) \quad (2.3)$$

In the case of the SPP0 copolymer with a degree of sulfonylation of 38.8 wt% the mechanical  $\tan \delta$  peak temperatures observed for 0.1, 1, 3 and 30 Hz are 251°C, 256°C, 258°C and 263°C, respectively, as shown in Figure 2.16. Figure 2.17 shows an Arrhenius plot of the frequencies as a function of the reciprocal temperature for the peak maxima. The SPP0 copolymer of higher degree of sulfonylation has the larger activation energy, reflecting the increased intermolecular and steric barrier to long-range segmental motion by the sulfonylation reaction of PPO.

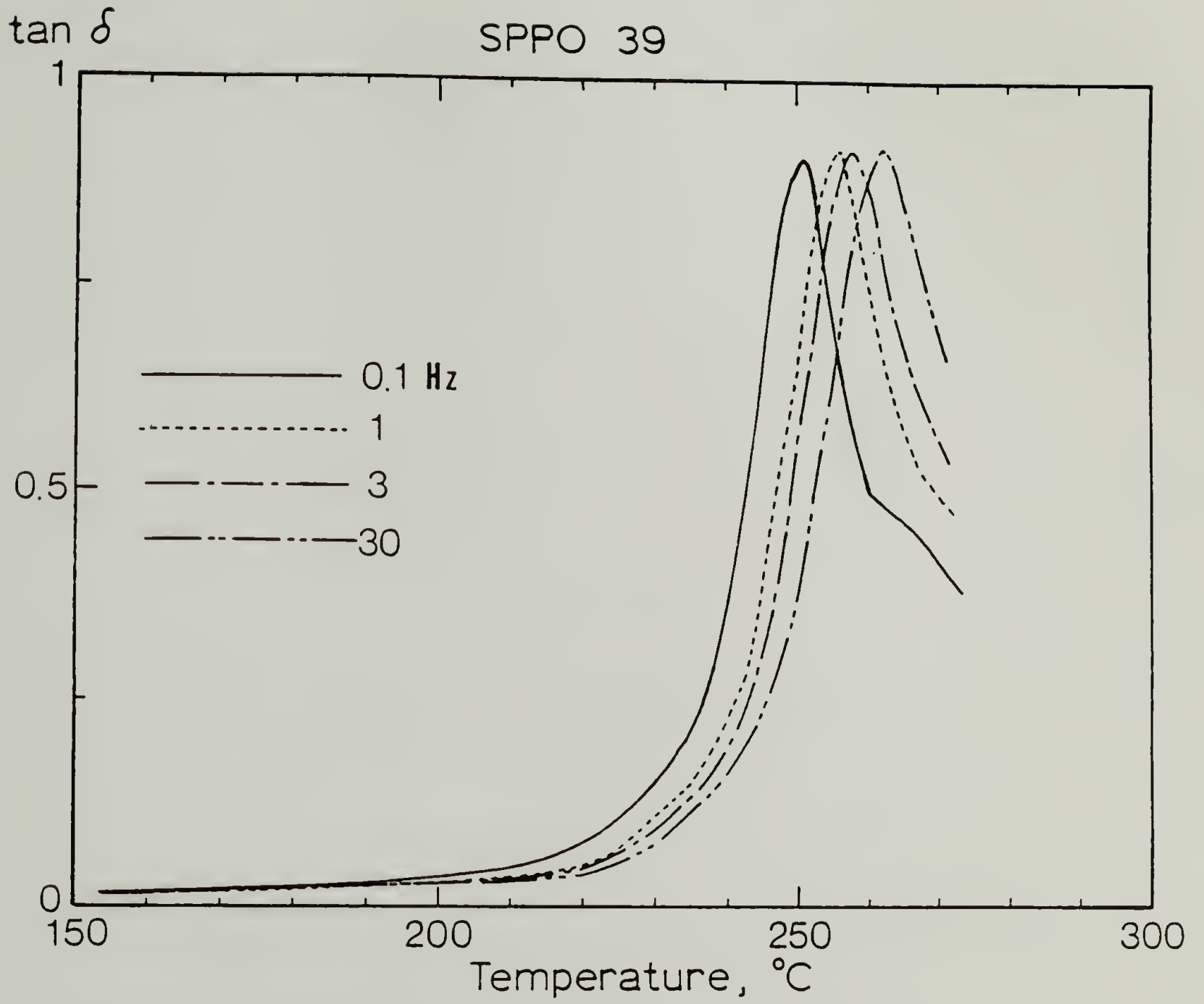


Figure 2.16. Frequency dependences of mechanical  $\tan \delta$  curves  
for dry SPPO 39

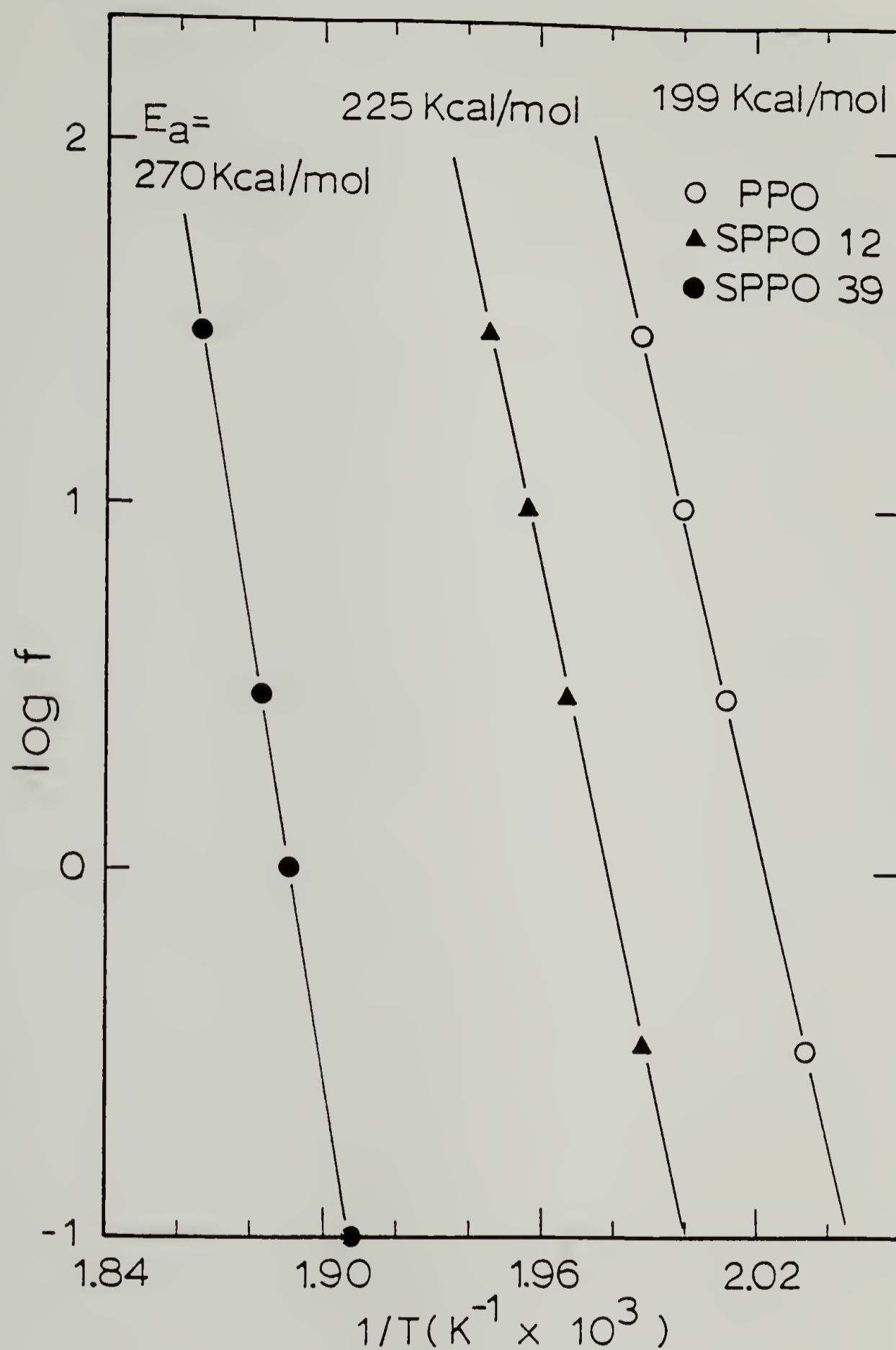


Figure 2.17. Arrhenius plot of relaxation maxima vs. frequency for PPO, SPPO 12 and SPPO 39

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### CHAPTER III

#### MISCIBILITY IN BLENDS OF SULFONYLATED POLY(2,6-DIMETHYL-1,4-PHENYLENE OXIDE) (SPPO) COPOLYMERS AND IN BLENDS OF POLYSTYRENE/SPPO COPOLYMERS

This chapter is divided into two parts. The first part describes the miscibility behavior in blends of SPPO copolymers differing only in copolymer composition, systems of the type  $(C_{1-x}D_x)_{n_1} / (C_{1-y}D_y)_{n_2}$  where C and D refer to unsulfonylated phenylene oxide and sulfonylated phenylene oxide units, respectively. The segmental interaction parameter between unsulfonylated and sulfonylated unit in SPPO copolymers ( $\chi_{CD}$ ) is determined from the critical composition difference for miscibility. This determination is based on Scott's prediction<sup>1</sup> and is made using a mean field treatment, as discussed in Chapter I.

Scott predicted that copolymers with a certain degree of heterogeneity in chemical compositions would be thermodynamically unstable. Namely, two random copolymers differing only in composition are not necessarily miscible in all proportions. Accordingly, there is a tolerable difference in copolymer composition

above which the blends are immiscible. This prediction has been corroborated for several copolymer blend systems<sup>2-7</sup>. The tolerable difference in copolymer composition for the blends of SPP0 copolymers was determined by DSC and optical microscopy.

The second part describes miscibility behavior and phase stability in blends of polystyrene with SPP0 copolymers, systems of the type  $A_{n_1}/(C_{1-y}D_y)_{n_2}$  where A refers to the styrene unit. Based on the  $\chi_{CD}$  determined in the first part,  $\chi_{AD}$  is determined by employing a mean field treatment. From the temperature induced phase separation study LCST behavior was observed and interphase mixing in the two phase blend is also discussed on the basis of the glass transition width.

#### A. Experimental Section

The sulfonylation procedure and the characterization of a series of SPP0 copolymers were described in Chapter II. Polystyrene samples ( $M_w = 13,000, 68,000$  and  $115,000$ ) were purchased from Polymer Laboratories and used as received. All the samples had  $\bar{M}_w/\bar{M}_n < 1.05$ . The numeral following polystyrene represents its molecular weight, thus the polystyrene sample with  $\bar{M}_w$  of  $115,000$  is designated as PS-115.

Blends (50/50 wt%) were prepared by casting films from 2 wt% THF solutions. The solvent was allowed to evaporate slowly at ambient conditions for at least four days and the resulting films were placed in a vacuum oven at 140°C for 96 hr to completely remove residual solvent.

Glass transition temperatures were measured in the same way as described in Chapter II. Due to the proximity of the  $T_g$ 's of the constituents in some blends, first derivative DSC thermograms were also recorded.  $T_g$  measurements to assess the miscibility of two polymers are suitable only if their  $T_g$ 's are sufficiently far apart from each other. Thus, if the differences in the glass transition temperatures of each constituent were greater than 15°C, then DSC and optical microscopy were employed to determine miscibility. Otherwise, only the latter was used.

Optical micrographs were taken on a Leitz optical microscope with cross-polarizers at a magnification of 100X. Solutions of 50/50 wt% blend mixtures in THF were cast onto microscope slides. After drying at ambient conditions, these were further dried under vacuum and annealed at 290°C for 15 min followed by rapid quenching into liquid  $N_2$ .

The temperature induced phase separation study in the blends of polystyrene with SPP0 copolymers was done by heating the samples

to 290°C and maintaining them for 20 min followed by rapid cooling (-320 K/min) to room temperature and subsequent scanning at 20°C/min, unless otherwise noted.

## B. Results and Discussion

### i). Blends of SPP0 Copolymers

Figures 3.1-3 show typical DSC thermograms with their first derivative curves. One can see clearly that the blends exhibit two distinct  $T_g$ 's for each constituent with slight inward shift of  $T_g$  of each component indicative of some partial miscibility. Figure 3.4 displays a DSC thermogram for the blend of PPO with SPP0 24, implying its two phase nature. However, the blends at  $\Delta$  wt% = 18.3 and 20.5, as seen in Figures 3.5 and 3.6, show a single  $T_g$  between those of the pure constituents.

To verify that the single  $T_g$  observed in the blend is not due to an experimental artifact concerned with the sensitivity of DSC, samples of pure SPP0 72 and SPP0 90 were separated in a DSC sample pan by a thin aluminum foil barrier to prevent mixing, as similarly done by Ueda<sup>8</sup>. The resulting DSC thermogram is also

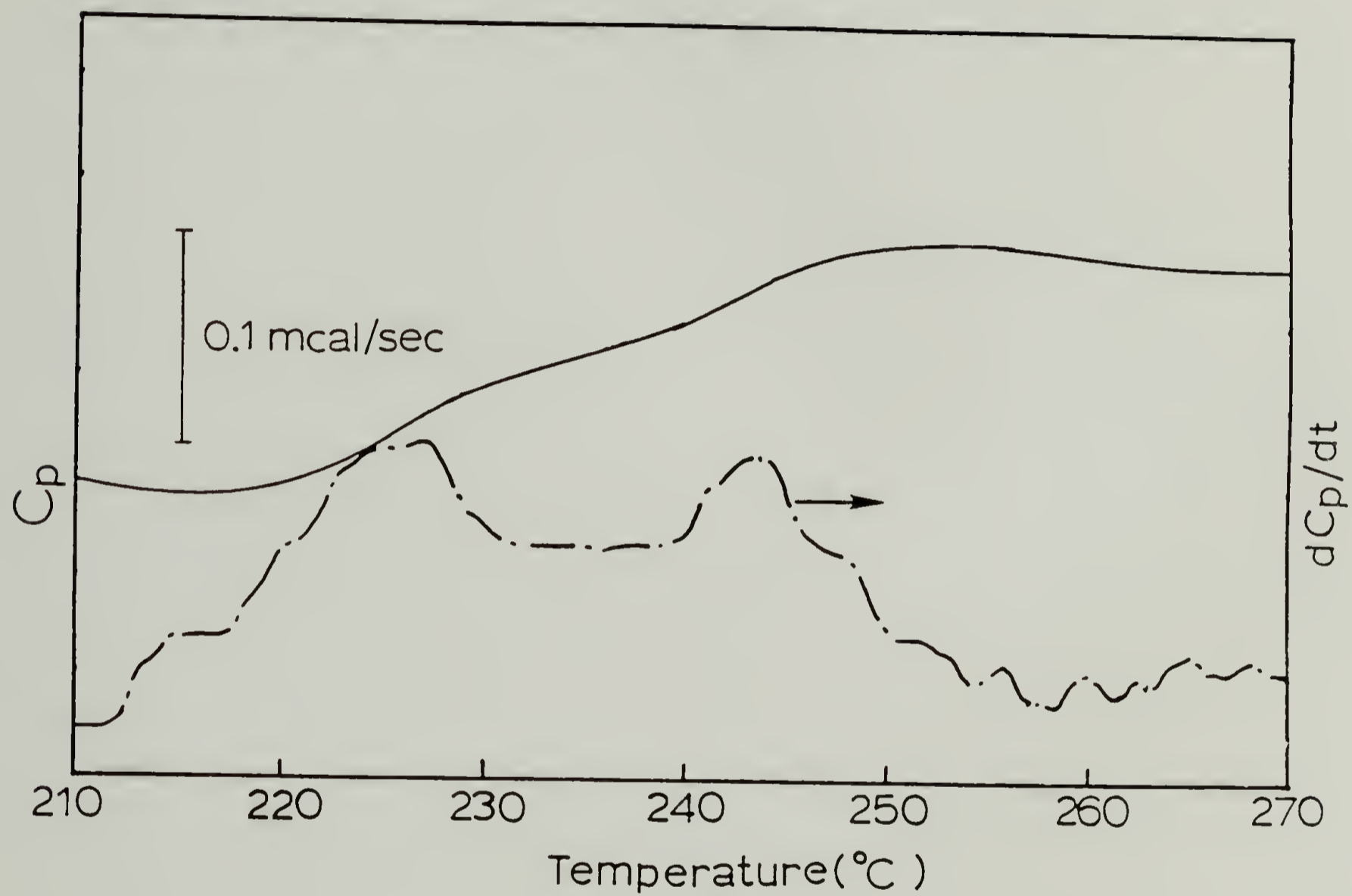


Figure 3.1. DSC thermogram for SPP0 12/34 (50/50 wt% blend)

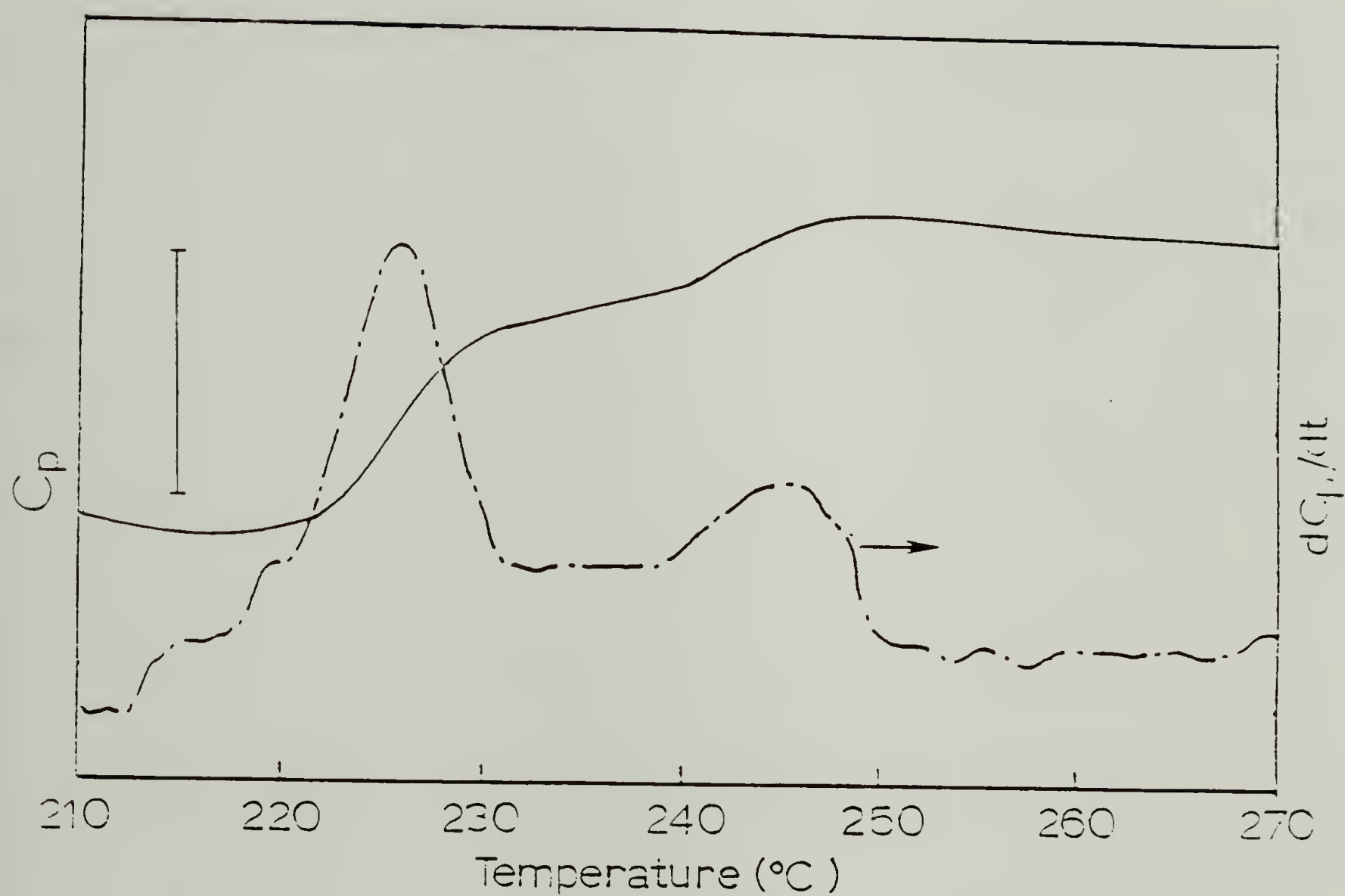


Figure 3.2. DSC thermogram for CPPC 12/39 (50/50 wt% blend)

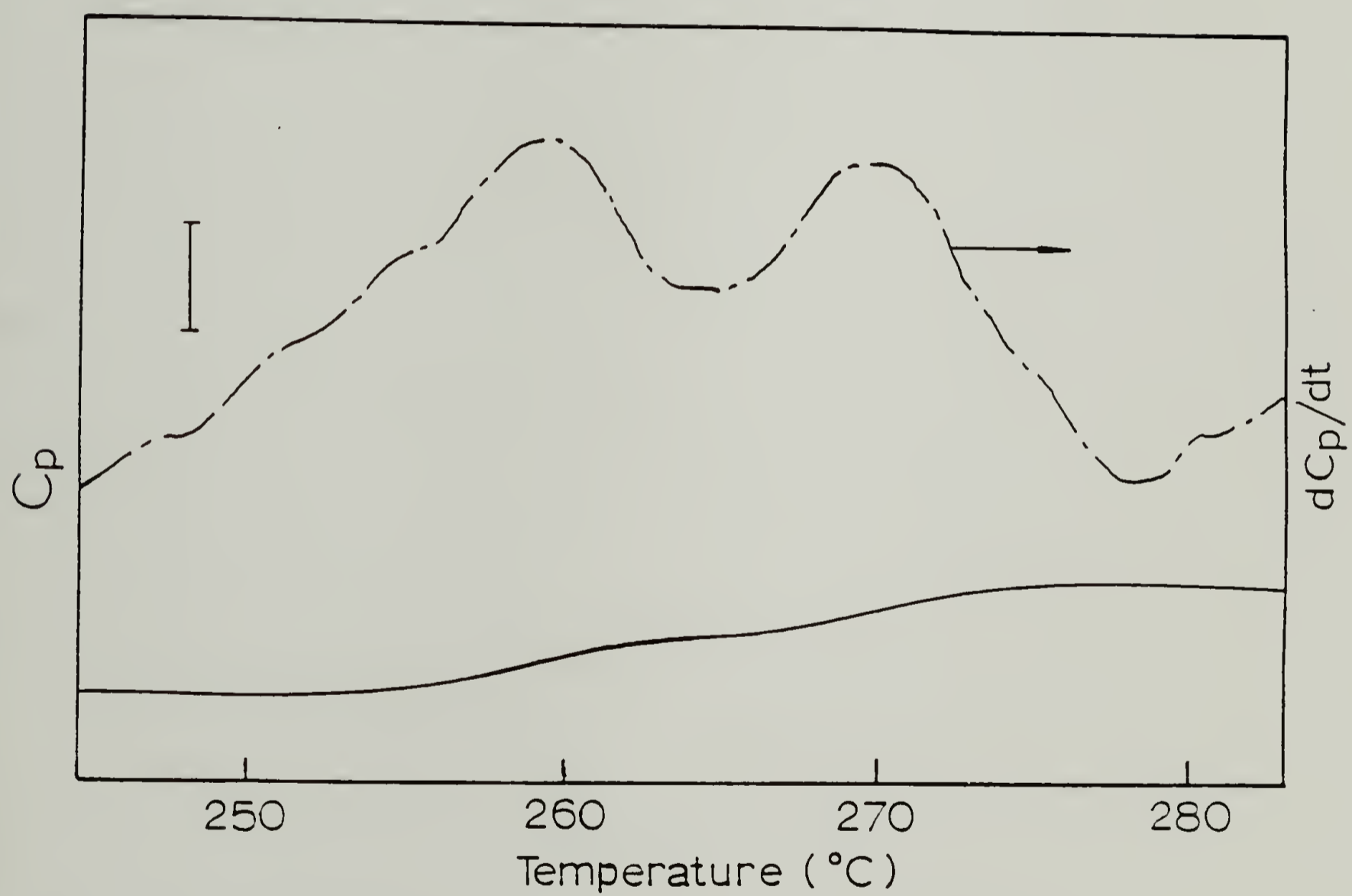


Figure 3.3. DSC thermogram for SPP0 47/75 (50/50 wt% blend)

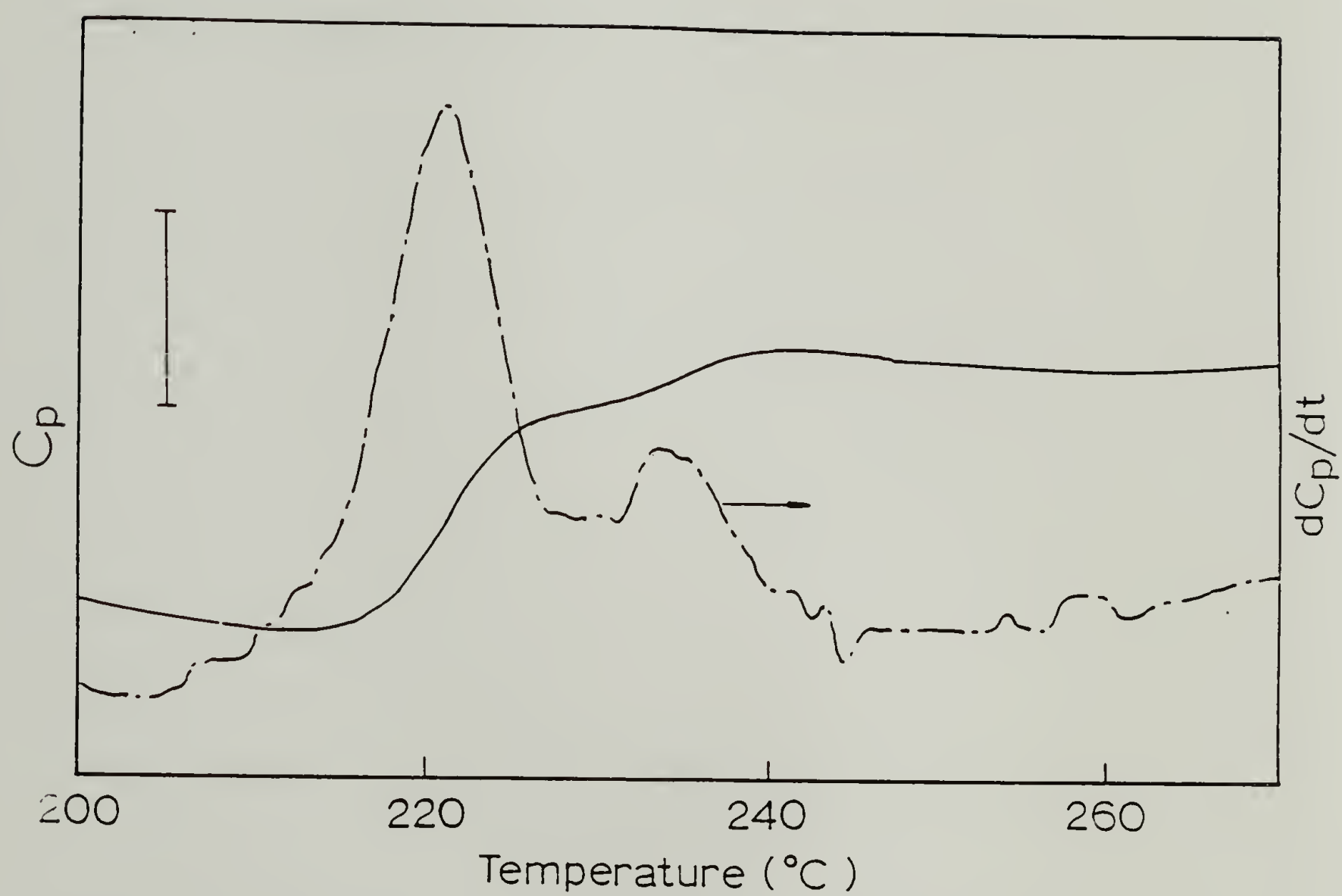


Figure 3.4. DSC thermogram for PPO/SPP0 24 (50/50 wt% blend)

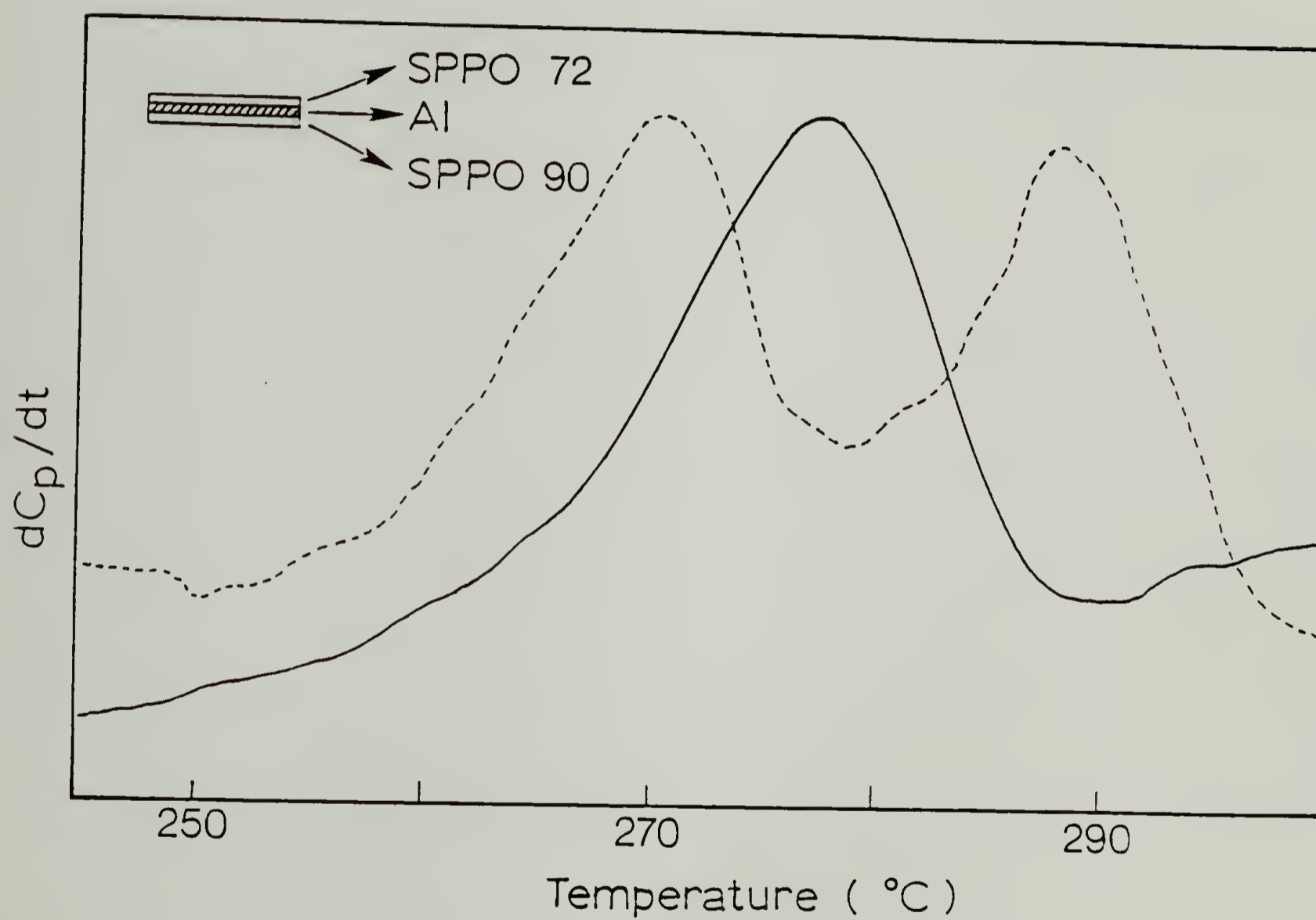


Figure 3.5. DSC thermogram for SPPPO 72/90 (50/50 wt% blend).

Dotted line indicates pure constituents separated by aluminum foil.

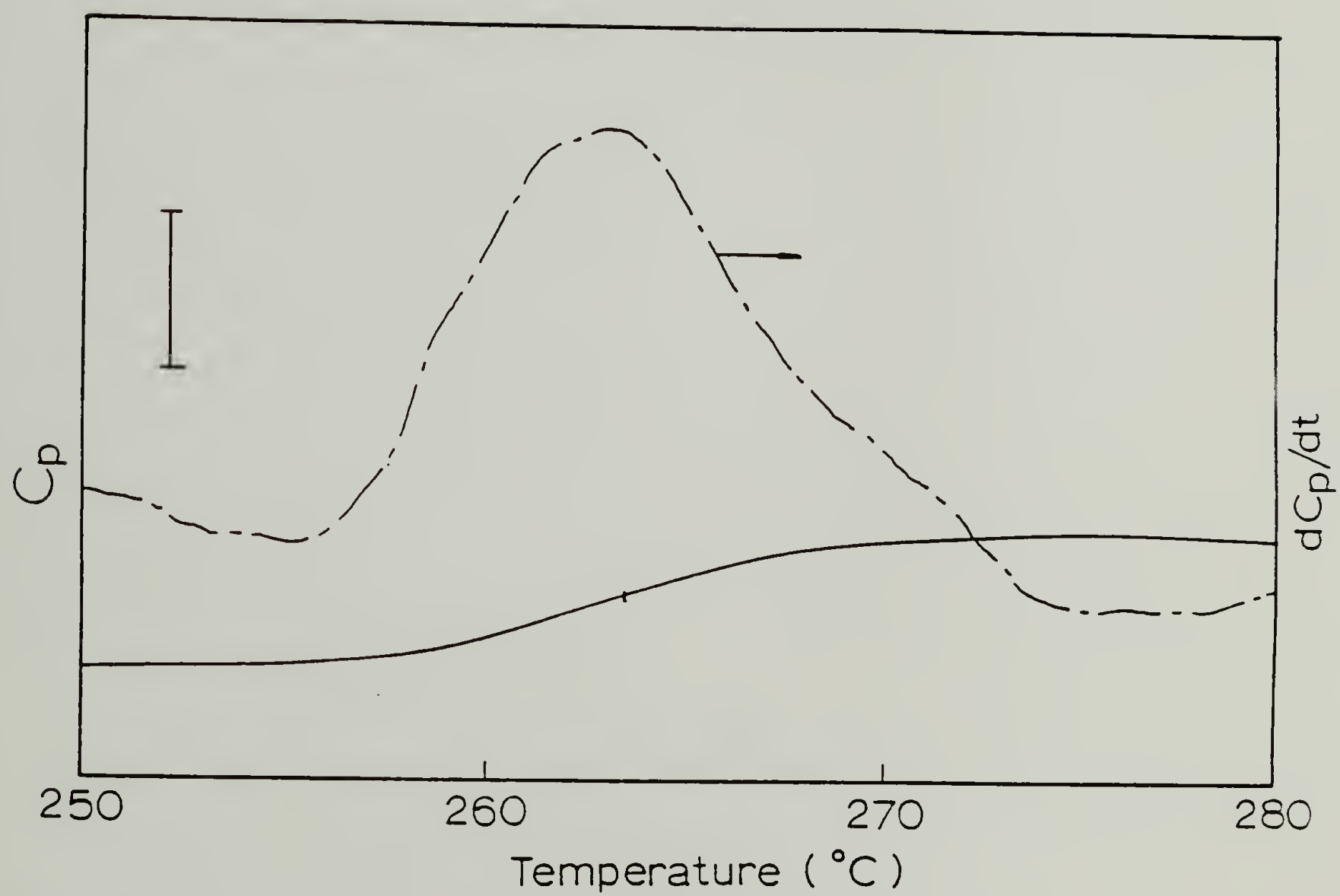


Figure 3.6. DSC thermogram for SPP0 54/75 (50/50 wt% blend)

displayed in Figure 3.5, and shows two  $T_g$ 's for each component, thus reflecting clearly that the single  $T_g$  observed for the blend of SPP0 72/90 is due to a homogenization of the two blend constituents.

Figure 3.7 shows optical micrographs in which phase separation is observed at  $\Delta$  wt% equal to or greater than 22.2. The kinetics of phase separation in blends depends on the viscosity of the medium and the thermodynamic driving force<sup>9</sup>. Thus, it is necessary to keep equal degrees of superheating for each blend in comparing the growth of the segregated domains. Although the phase boundary remains undetermined at present, it can be seen qualitatively that the domains of the phase separated blend become larger as  $\Delta$  wt% increases. However, no evidence of phase separation in the blend at  $\Delta$  wt% below 18.6 was observed.

Two techniques employed in the current study are considered to be supplementary based on the summary of results illustrated in Figure 3.8. However, it should be pointed out that two experimental probing techniques of miscibility reflect different length scales. That is, the DSC has a length scale of several hundreds angstroms, while the optical microscope has a maximum resolution down to about 0.2  $\mu\text{m}$ .

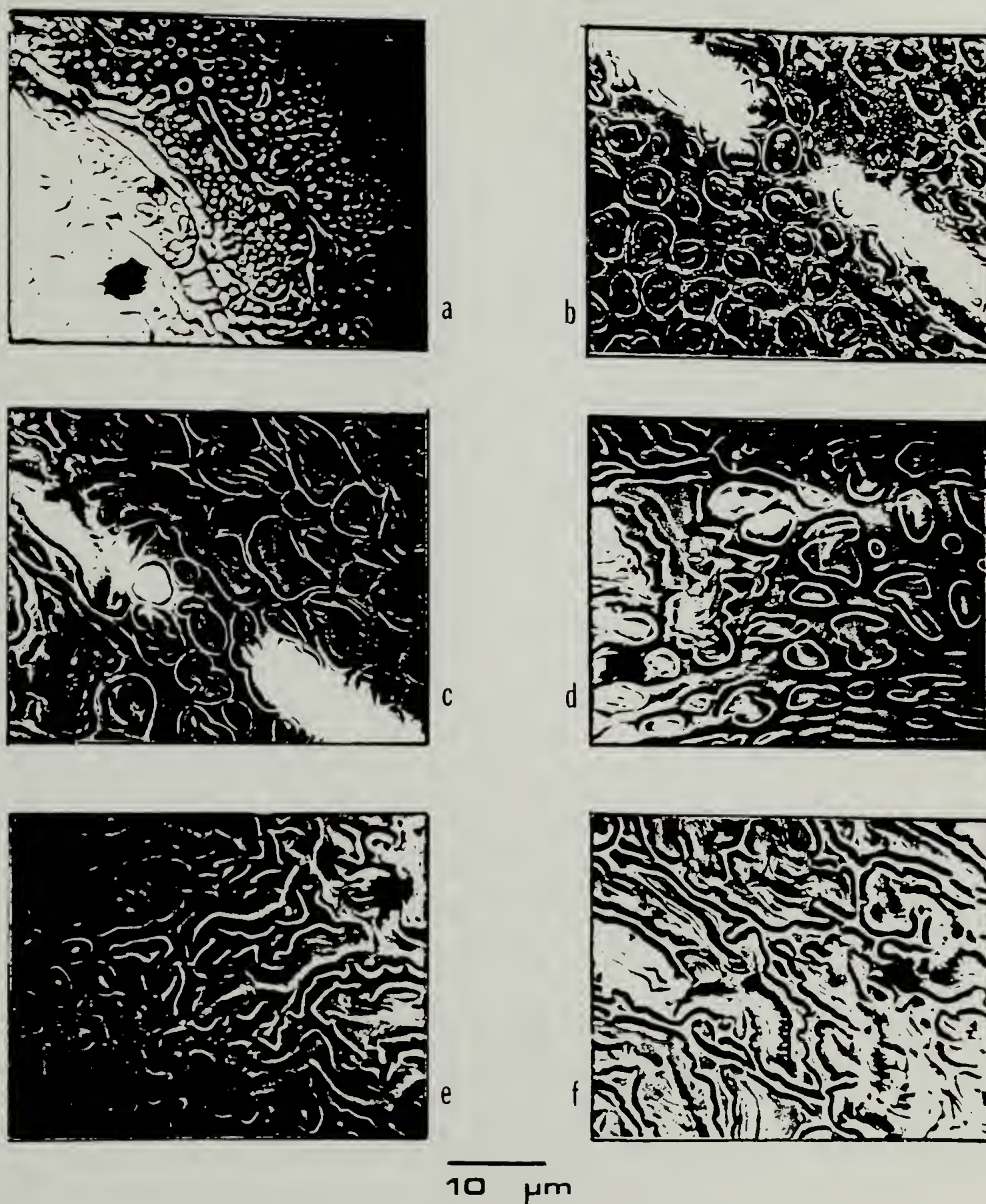


Figure 3.7. Optical micrographs for 50/50 wt% blends :

(a) SPPO 12/34; (b) SPPO 30/54; (c) SPPO 30/55;

(d) SPPO 12/39; (e) SPPO 47/75; (f) SPPO 12/44

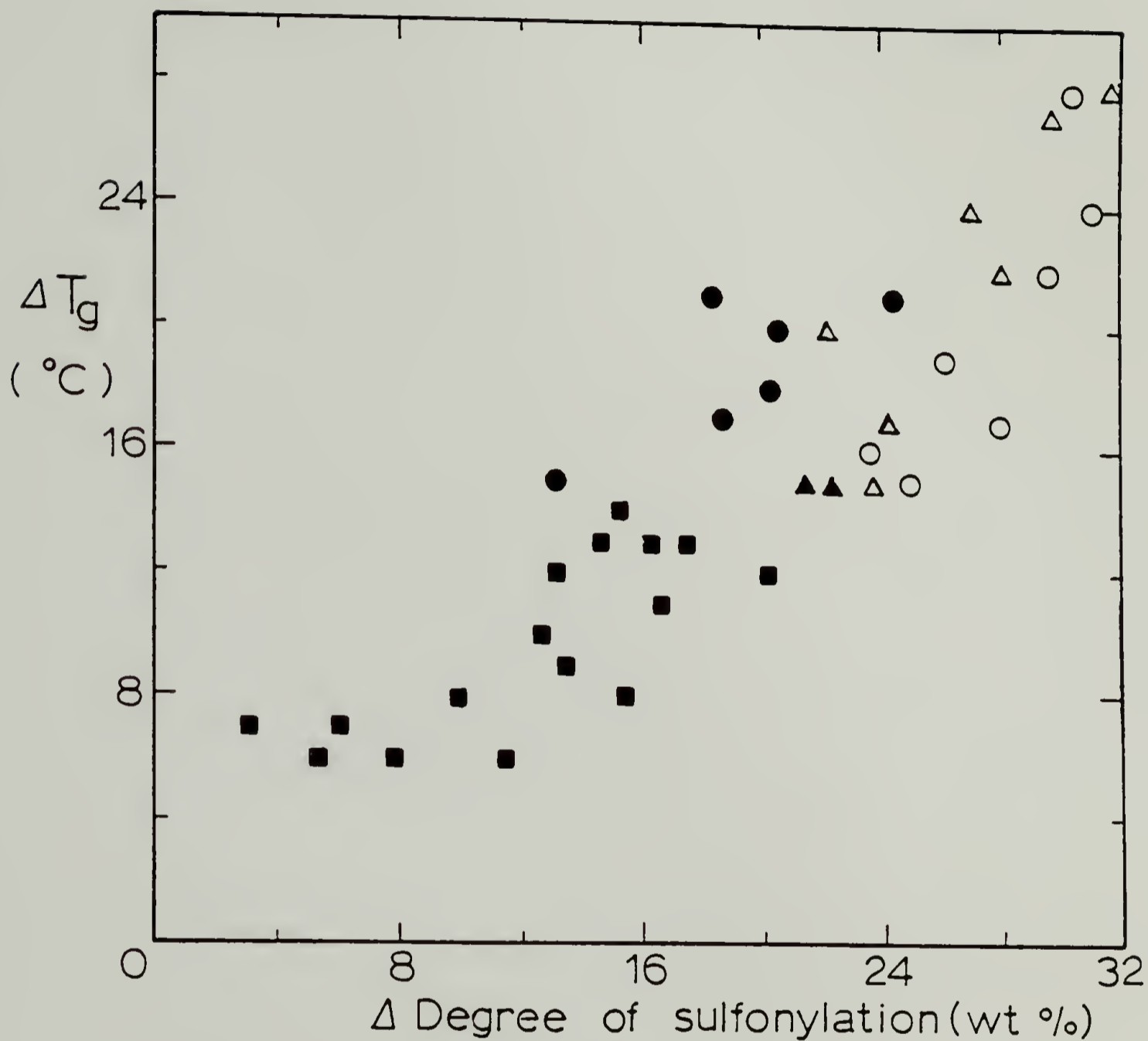


Figure 3.3  $\Delta T_g$  vs.  $\Delta$  degree of sulfonylation. Filled and open symbols represent one phase and two phase systems, respectively. The data represented by triangles were obtained by DSC and optical microscopy. The data represented by circles were obtained by DSC only. The data represented by squares were obtained by optical microscopy only.

For a mixture of two copolymers which differ only in copolymer composition, i.e.,  $A = C$  and  $B = D$ , in the blend system of  $(A_{1-x}B_x)_{n_1} / (C_{1-y}D_y)_{n_2}$ , Eqn. (1.14) reduces to :

$$\chi_{\text{blend}} = (x - y)^2 \chi_{CD} \quad (3.1)$$

At a critical point one can write, from Eqn. (1.15) and Eqn. (3.1),

$$\frac{1}{2} \left( n_1^{-\frac{1}{2}} + n_2^{-\frac{1}{2}} \right)^2 = (x - y)^2 \chi_{CD} \quad (3.2)$$

Figure 3.9 shows an isothermal miscibility diagram of 50/50 wt% blends of SPP0 copolymers. The critical composition difference  $|x - y|_{\text{crit}}$  in the blend for phase separation varies from 0.20 at the lower degree of sulfonylation to 0.26 at the higher degree of sulfonylation.

Based on the Flory-Huggins lattice treatment of binary mixtures, Koningsveld<sup>10</sup> proposed an expression which takes into account the disparity between the relative sizes of the monomer units. This disparity gives rise to differing numbers of nearest-neighbor contacts, provided that the number of nearest-neighbor contacts is proportional to the interacting surface areas.

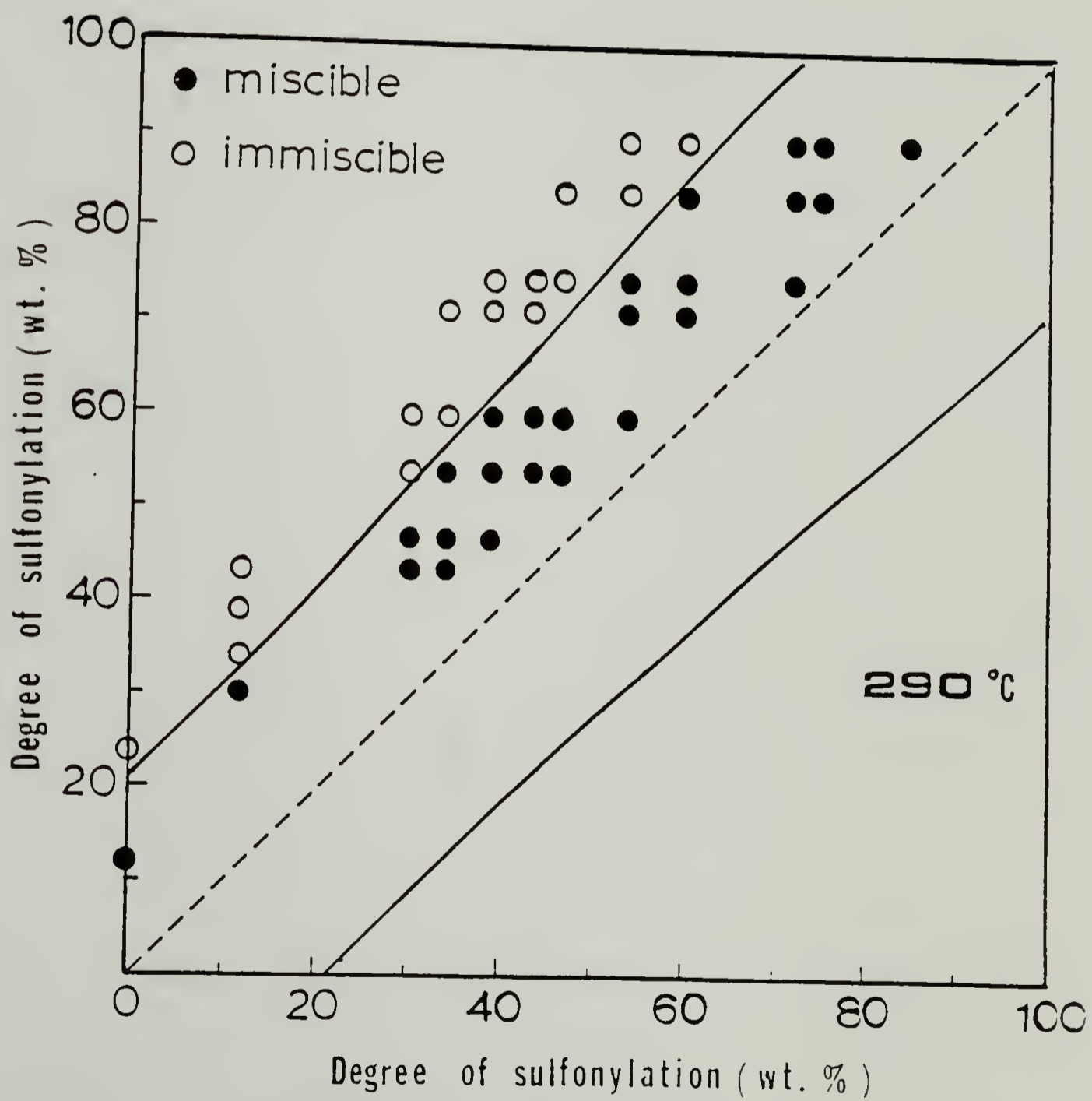


Figure 3.9. Isothermal miscibility diagram of 50/50 wt% blends of SPPO

In the case of blends of acrylic or methacrylic copolymers<sup>4,6</sup>, the disparity of monomer size has been found to affect miscibility behavior significantly. As the content of a monomer of larger surface area increases, the critical composition difference increases, i.e., the respective copolymer blends tend to be much more miscible.

The phenylene oxide unit (C) and the sulfonylated phenylene oxide unit (D) in the present system have, from the calculation of Bondi's group contribution<sup>11</sup>, surface areas of  $68 \times 10^{-9} \text{ cm}^2/\text{mole}$  and  $115 \times 10^{-9} \text{ cm}^2/\text{mole}$ , respectively, which are greatly different from each other. The slight increase in the critical difference in degree of sulfonylation for miscibility at higher degree of sulfonylation may be due to an increasing interacting surface area.

Table 3.1 shows  $|x-y|_{\text{crit}}$  and the effective degree of polymerization,  $N$ , which is equal to the weight-average molar mass of the copolymer divided by the mass of PPO repeat unit. By introducing  $|x-y|_{\text{crit}}$  and  $N$  into Eqn. (3.2) we determine  $\chi_{\text{CD}}$ , the segmental interaction parameter between unsulfonylated and sulfonylated repeat units in the SPP0 copolymer, to be 0.15-0.06 at 290°C. Figure 3.10 displays the composition (mean degree of sulfonylation) dependence of  $\chi_{\text{CD}}$  which decreases with increasing degree of sulfonylation,

Table 3.1

Mean Degree of Sulfonylation Dependence of  $x_{CD}$ 

Mean Degree of Sulfonylation %	n	$ x-y _{crit}$	$x_{CD}, 290^{\circ}C$
10	330	0.20	0.15
20	360	0.21	0.13
30	390	0.22	0.11
50	470	0.24	0.07
70	590	0.26	0.05

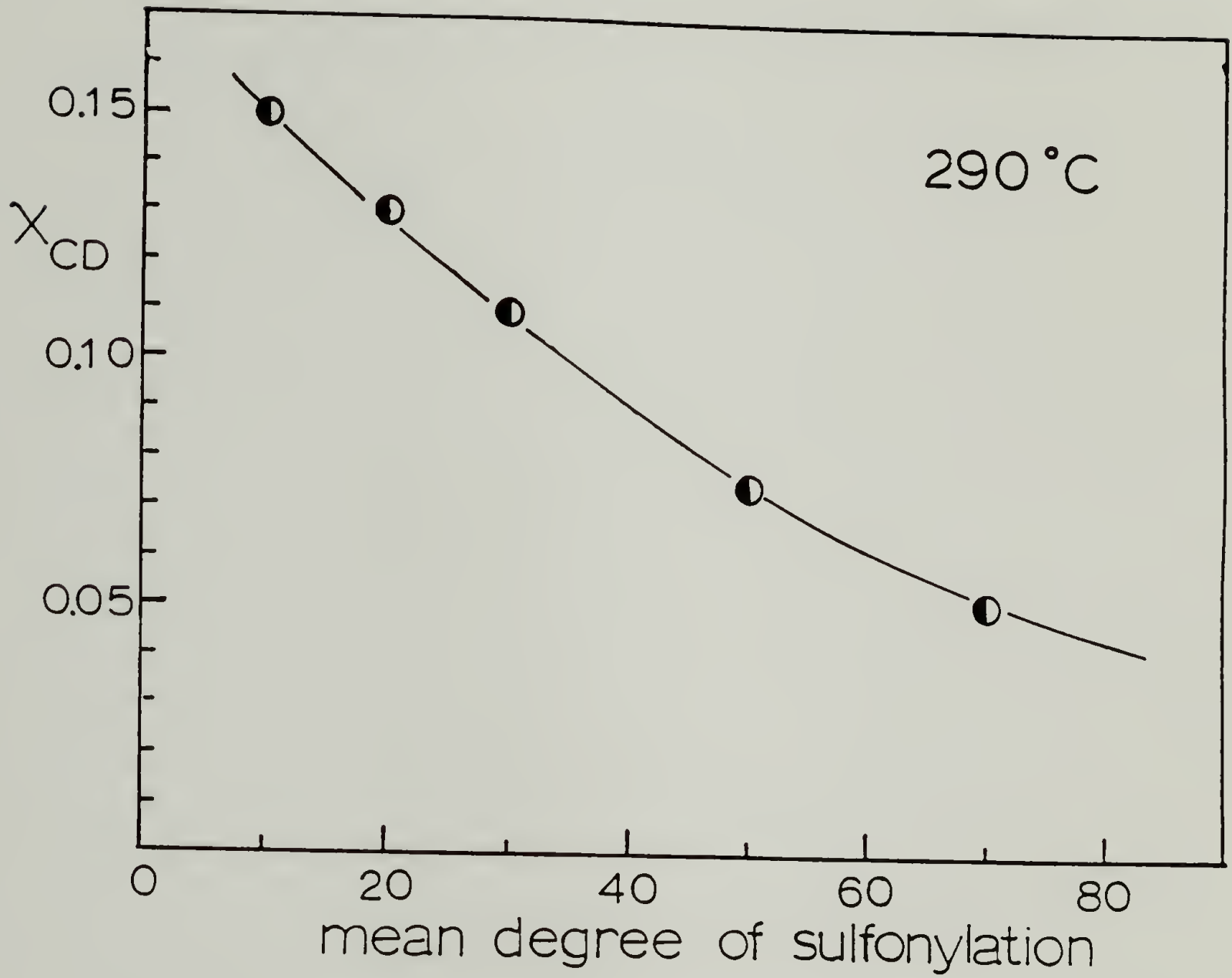


Figure 3.10. Mean degree of sulfonation dependence of  $\chi_{CD}$  at 290 °C

indicating that the van Laar type exchange interaction energy decreases with increasing degree of sulfonylation.

To determine the critical phenomena in the present system, sample annealing up to 360°C, above which significant degradation of polymers appears to occur, has been attempted. However, the phase separation of miscible blends or the homogenization of immiscible blends could not be induced by annealing, implying either that  $\chi_{CD}$  is very temperature-insensitive or that phase boundary on the temperature plane is very stiff.

#### ii). Blends of Polystyrene with SPP0 Copolymers

Blends of SPP0 with the degree of sulfonylation equal to or less than 23.5 wt% were miscible with PS-115 using a miscibility criterion of a single, composition-dependent glass transition. Blends of PS-115/SPP0 with the degree of sulfonylation of 30.4 wt% didn't show a single intermediate  $T_g$  over the whole range of blend compositions but exhibited a single  $T_g$  at the blend composition of 50/50 wt% and thus, are regarded as being miscible in this work.

In contrast, SPP0 with the degree of sulfonylation equal to or greater than 34.0 wt% was found to be immiscible with PS-115. The two  $T_g$  values observed didn't correspond to those of the pure

components, indicating a separation into mixed phases. As will be discussed later, this partial miscibility increases as the degree of sulfonylation of SPP0 approaches the critical degree of sulfonylation (31 wt%) for phase separation in these blends.

Figure 3.11 displays the DSC thermograms (normalized to the weight of the sample) of SPP0 12/PS-115 blends. Figure 3.12 shows the composition dependences of the  $T_g$ 's of these blends and a comparison of the compositional variation of  $T_g$  to the thermodynamic or empirical expressions. Based on the entropy of mixing of two polymers and assuming temperature independent heat capacity increments, Couchman<sup>12</sup> derived the relation

$$\ln T_g = (W_1 \Delta C_{p1} \ln T_{g1} + W_2 \Delta C_{p2} \ln T_{g2}) / (W_1 \Delta C_{p1} + W_2 \Delta C_{p2}) \quad (3.3)$$

where  $W_1$  and  $W_2$  refer to the weight fractions of the blend constituents,  $T_{g1}$  and  $T_{g2}$  are the  $T_g$ 's of the pure components and  $\Delta C_{p1}$  and  $\Delta C_{p2}$  are the heat capacity increments at  $T_g$  for each constituent.

Fox equation<sup>13</sup> is given by

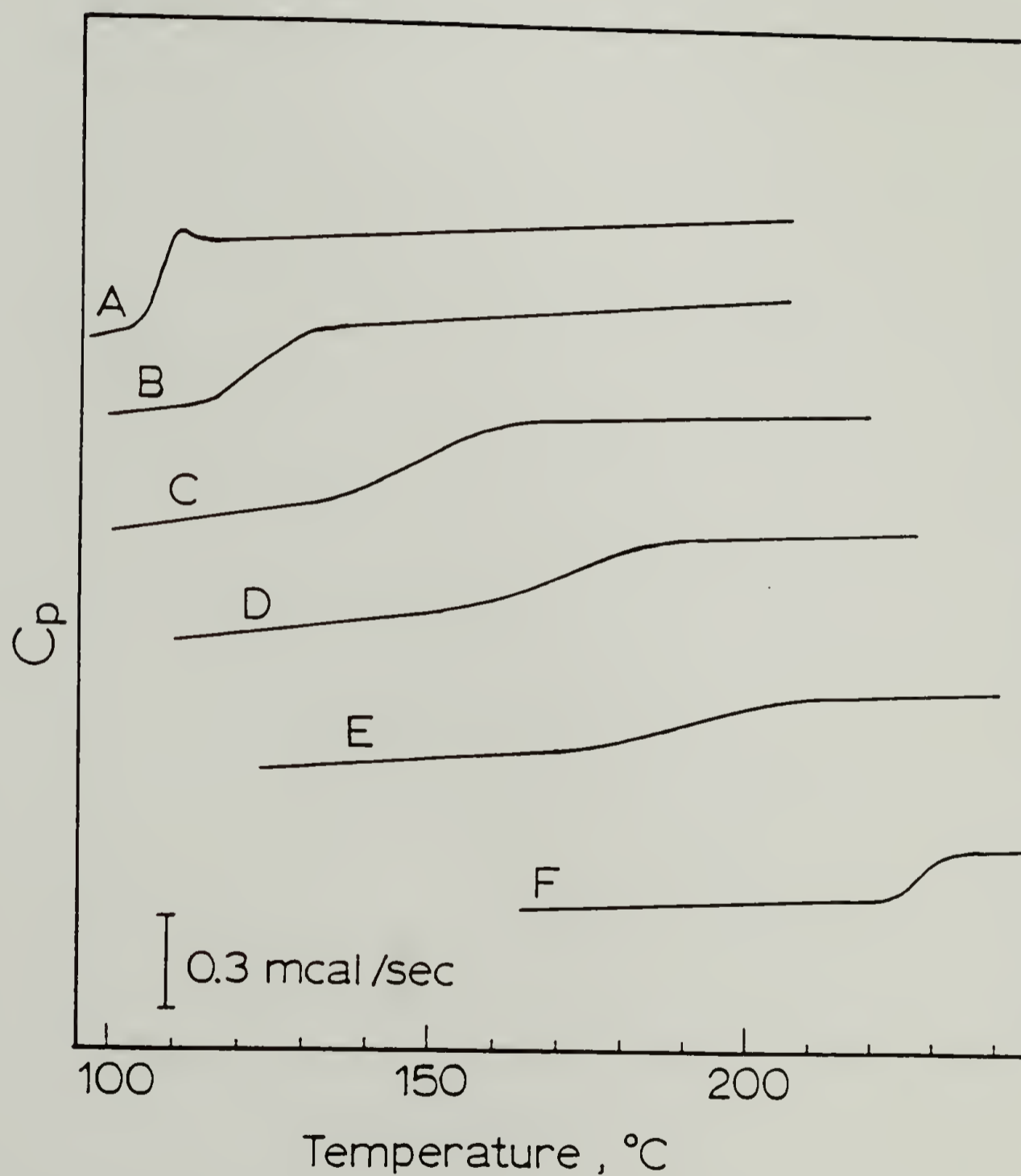


Figure 3.11. DSC thermograms of PS-115, SPP0 12 and blends :

(A) pure PS-115; (B) 25 wt% SPP0 12; (C) 50 wt% SPP0 12;  
 (D) 70 wt% SPP0 12; (E) 85 wt% SPP0 12; (F) pure SPP0 12

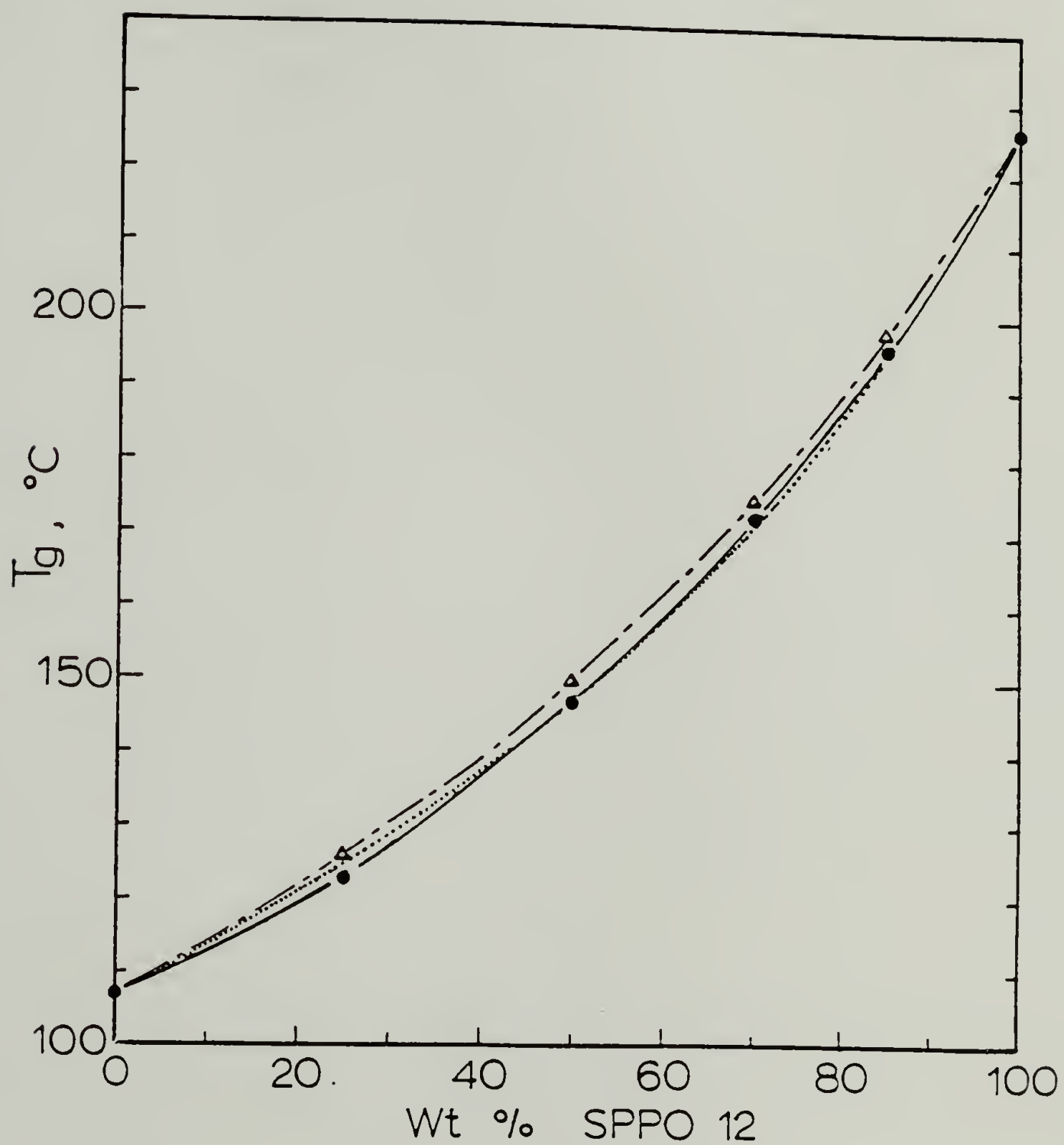


Figure 3.12. Dependence of  $T_g$ 's on the weight fraction of SPP0 12

for the PS-115/SPP0 12 blends. Dashed lines represent the Couchman equation, and dotted lines represent the Fox equation with  $k=0.66$ .

$$(W_1 + kW_2)/T_g = W_1/T_{g1} + kW_2/T_{g2} \quad (3.4)$$

The  $T_g$  values calculated using Couchman equation and Fox equation with  $k = 0.66$  are in good agreement with the experimental values.

The pertinent parameters used in the calculation are  $\Delta C_p(\text{PS}) = 0.28 \text{ J/g.deg}$  and  $\Delta C_p(\text{SPP0 12}) = 0.18 \text{ J/g.deg}$ .

Transition width of the blend,  $\Delta T_g$  as defined by  $2(T_g - T_g', \text{onset})$ , is plotted as a function of the weight fraction of SPP0 12 in Figure 3.13. The  $\Delta T_g$ 's of the blends are much broader than those of the pure components as noted previously for the blend of polystyrene with PPO<sup>14</sup>. This feature may be due to local compositional fluctuation still present within the miscible blend. A maximum width of the glass transition region of the blends around 80 wt% of SPP0 12 can be ascribed to a much larger fluctuation in local composition resulting from a skewed phase diagram toward the low molecular weight component, SPP0 12, as discussed by Koningsveld<sup>15</sup>. The driving force for phase segregation will be maximum at the blend composition corresponding to the critical point, which is predicted to exist above the decomposition temperature of each constituent. These blends exhibit LCST behavior, as discussed later.

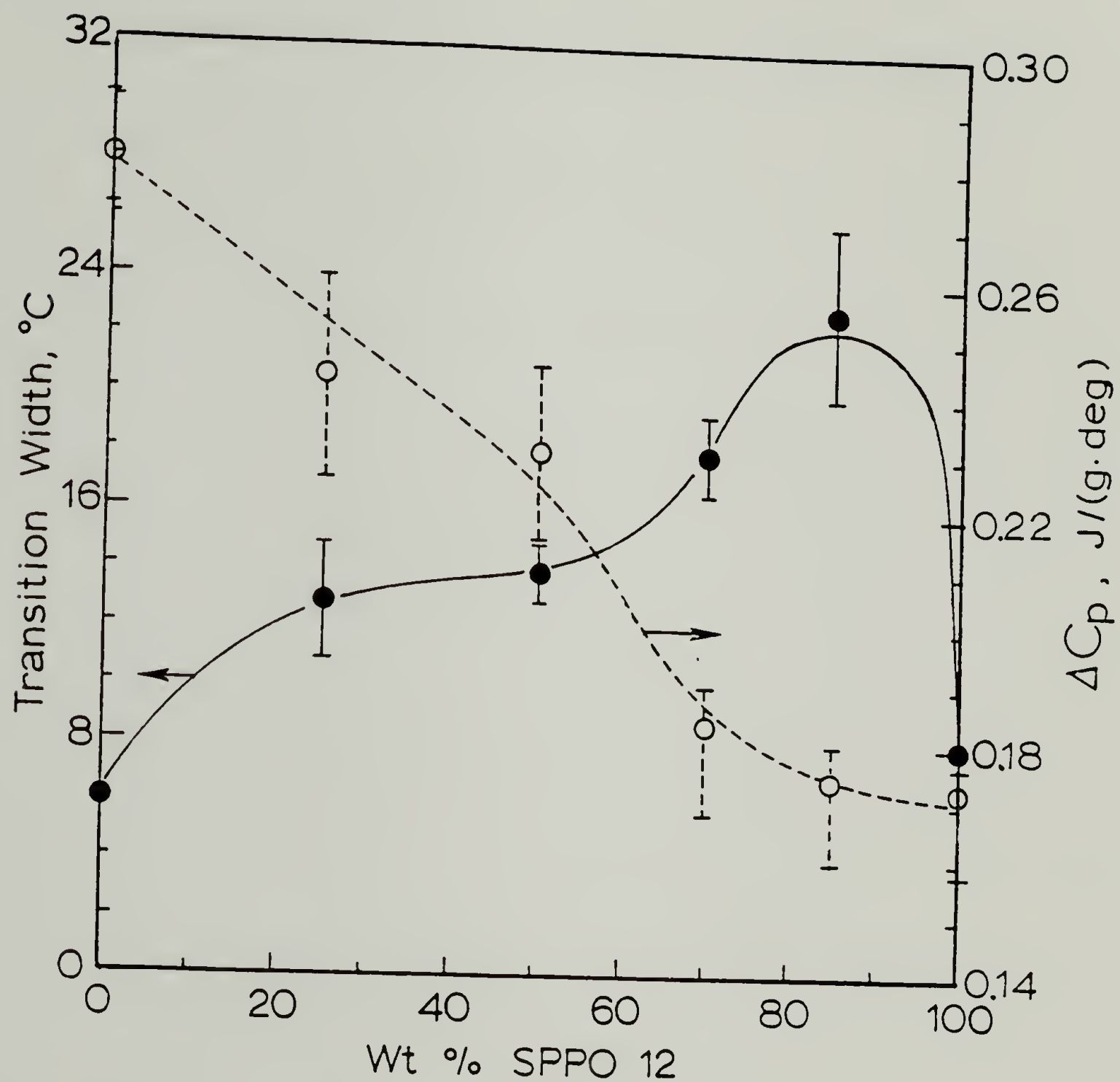


Figure 3.13. Width of the glass transition and  $\Delta C_p$ 's for the PS-115/SPPO 12 blends as a function of blend composition

Taking the polydispersities in chain length into account, Koningsveld<sup>16</sup> derived an expression relating the composition at the critical point, i.e.,

$$\phi_{2C} = 1/[1 + (N_{w2} a_1 / N_{w1} a_2)^{\frac{1}{2}}] \quad (3.5)$$

where  $a_i = N_{zi} / N_{wi}$  and  $N_{wi}$  and  $N_{zi}$  refer to the degree of polymerization based on the weight average molecular weight and on the z-average molecular weight, respectively. The critical point in the current blends is calculated to be at 74 wt% of SPPO 12 by employing  $N_{w1} = 1150$ ,  $a_1 = 1$ ,  $N_{w2} = 350$  and  $N_{z2} = 700$  (determined from GPC measurements). This calculation compares well with the observed maximum  $\Delta T_g$  around 80 wt% of SPPO 12.

Figure 3.13 also shows the blend composition dependence of the transition intensity ( $\Delta C_p$ ) i.e., the specific heat increment at  $T_g$ . The  $\Delta C_p$ 's of the blends decrease sigmoidally or almost linearly with the addition of SPPO 12. The latter case follows the relation found for some miscible blends<sup>17</sup> such that

$$\Delta C_p = W_1 \Delta C_{p1} + W_2 \Delta C_{p2} \quad (3.6)$$

In these blends of the type,  $A_{n_1}/(C_{1-y}D_y)_{n_2}$ , three segmental interaction parameters are involved and  $\chi_{blend}$  is, according to the mean field treatment<sup>18</sup>, given by

$$\chi_{blend} = (1 - y)\chi_{AC} + y\chi_{AD} - y(1 - y)\chi_{CD} \quad (3.7)$$

At the critical condition,  $\chi_{blend}$  equals  $\chi_{blend}^{crit}$  given as follows :

$$\chi_{blend}^{crit} = \frac{1}{2}(n_1^{-\frac{1}{2}} + n_2^{-\frac{1}{2}})^2 \quad (3.8)$$

The experimental results reflect that the critical degree of sulfonylation of SPP0 above which the copolymers are immiscible with PS-115 is 31 wt% at 290°C. Here, we employ  $\chi_{AC} = -0.043$ , recently recalculated from the miscibility study<sup>19</sup> of blends of PPO with poly(o-chlorostyrene-co-p-chlorostyrene). (Macconnachie et al<sup>20</sup> reported, by the small angle neutron scattering study of blends of deuterated PPO with polystyrene,  $\chi_{AC} = -0.033 \sim -0.021$  over a temperature range of 104 to 273°C). Thus, equating  $\chi_{blend}$  with  $\chi_{blend}^{crit}$  of 0.0035 and using  $\chi_{CD}$  of 0.15, as determined in the first part of this chapter,  $\chi_{AD}$ , the segmental interaction parameter between styrene and sulfonylated phenylene oxide unit, is determined

to be 0.20. It should be noted that the use of 50/50 wt% blends, rather than those compositions corresponding to the critical solution temperatures may induce some errors in the estimation of  $\chi$ . However, it is particularly interesting that  $\chi_{AD}$  and  $\chi_{CD}$  are of similar values. Accordingly, phenylene oxide and styrene unit in this system may be considered as equivalent units, thus these blends may be represented as  $A_{n_1} / (A_{1-y}^D y)_{n_2}$ .

Figure 3.14 displays transition width of 50/50 wt% blends of PS-115/SPPPO as a function of the degree of sulfonylation. The data represent the transition widths of single  $T_g$ 's in miscible blends, provided the degrees of sulfonylation are equal to or less than 30.4 wt%. The left extreme of the abscissa in Figure 3.14 represents the blend of PS with PPO. Transition widths of two phase blends with degrees of sulfonylation greater than 31 wt% are indicated for the PS rich phase and an inward shift in  $T_g$  indicates the difference between the  $T_g$  of the PS rich phase and that of pure PS. Some remarks should be mentioned here. First, the transition width of miscible blends slightly increases, reflecting a larger fluctuation in local composition, namely, an apparent decrease in the miscibility of the mixtures as the degree of sulfonylation increases. Second, the two phase blends form mixed phases and this partial miscibility decreases as the degree of sulfonylation deviates from the critical degree of sulfonylation, as expected. In addition, despite the fact that there

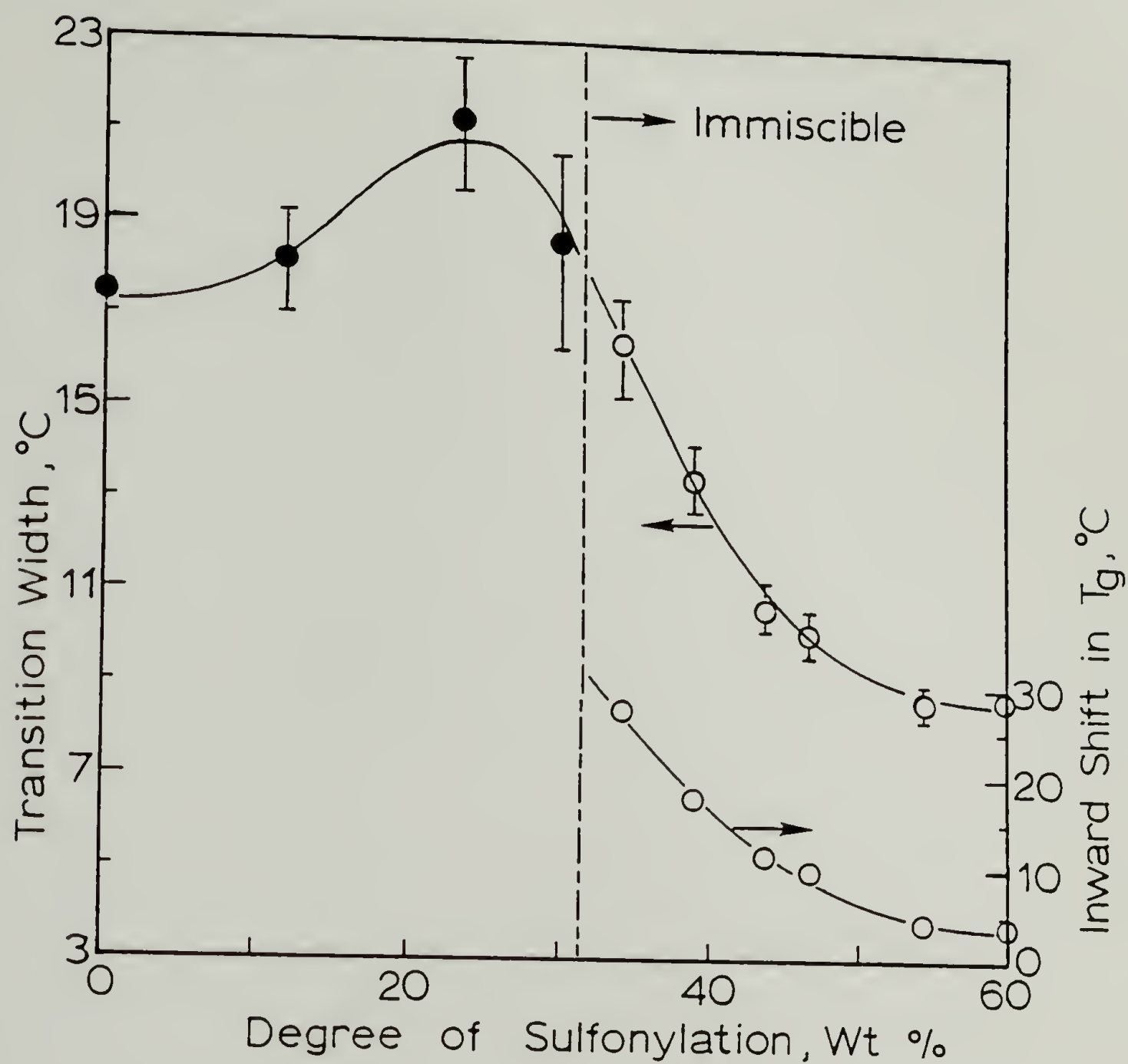


Figure 3.14. Width of the glass transition and inward shift in  $T_g$  for PS-115/SPP0 blends vs. degree of sulfonylation. Widths and inward shifts of the two phase blends are indicated for the PS rich phase.

are no chemical constraint between the two constituents which may result in macrophase separation, the  $T_g$  of the PS rich phase in the blend of PS-115/SPP0 with the degree of sulfonylation of 34 wt% shifts inward by 27°C. If we assume that the simple Fox equation<sup>13</sup> (with  $k = 1$ ) in Eqn. (3.4) is valid to predict the  $T_g$  of the mixed phase, then the PS rich phase is composed of 75 wt% PS and 25 wt% SPP0. Third, as the degree of sulfonylation deviates from the critical degree of sulfonylation, the transition width decreases indicative of a smaller composition fluctuation resulting from decreased interphase mixing. Namely, the segregated phase region is much purer, as the degree of sulfonylation increases. In this context, employing the values of  $\chi_{blend}$  which were calculated from Eqn. (3.7) and summarized in Table 3.2, one can get an initial slope of  $-1/3$  from the  $\log(\text{transition width}) - \log(\chi_{blend})$  plot, as seen in Figure 3.15. It seems likely that the increased  $\chi_{blend}$  which requires an increased van Laar type exchange interaction involved on mixing of the two constituents, makes the interphase mixing less significant, provided that the contribution of compressibility of the mixture involving SPP0 with differing degrees of sulfonylation is assumed to be negligible at the sample annealing temperature of 290°C.

To investigate the critical phenomena of these blends, thermally induced phase separation study by using PS with varying

Table 3.2

Transition Width and Calculated  $x_{\text{blend}}$  Values

Degree of Sulfonylation, wt%	Transition Width, °C	$x_{\text{blend}} \times 10^3$
30.4		-1.60
34.0	17.0	5.96*
38.8	13.5	15.67
43.5	10.7	25.80
46.6	10.0	32.90
54.1	9.0	51.20
60.0	9.0	66.80

\* It is to be noted that  $x_{\text{blend}}^{\text{crit}} = 3.50 \times 10^{-3}$

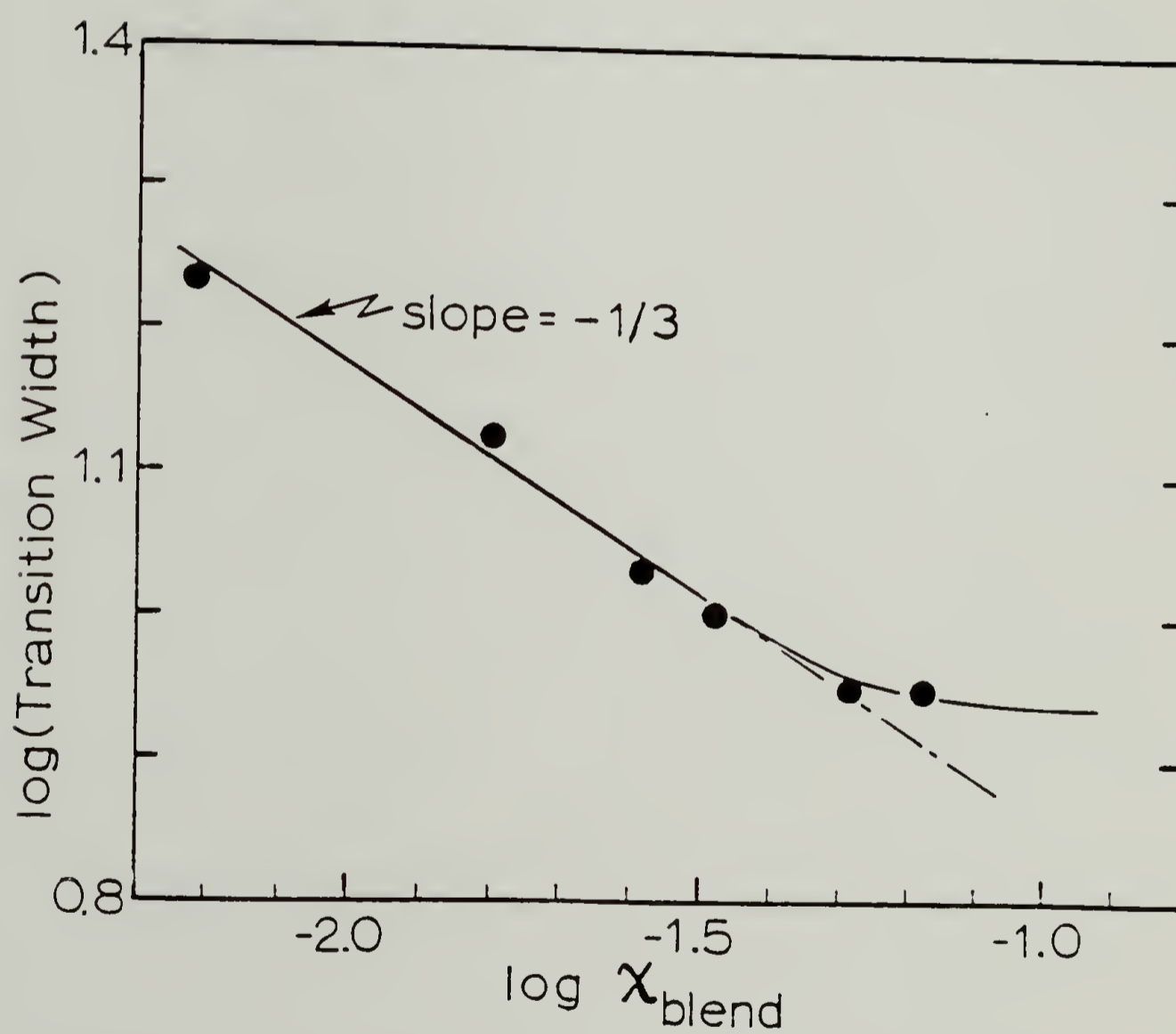


Figure 3.15. Width of the glass transition for PS-115/SPP0 blends  
vs.  $\chi_{\text{blend}}$

molecular weights was carried out. Figure 3.16 shows the DSC thermograms for 40/60 wt% of PS-13 (and PS-68)/SPP0 34 blends. The samples annealed at lower temperature show a single  $T_g$ . However, at higher temperatures they exhibit two distinct  $T_g$ 's indicative of a separation into mixed phases. From a series of DSC studies the phase diagram seen in Figure 3.17 was constructed, which represents the existence of an LCST behavior.

The equation of state theory<sup>21</sup> and the lattice fluid theory<sup>22</sup> predict that polymer-polymer mixtures which are miscible at lower temperatures tend to exhibit phase separation at higher temperatures in contrast to the predictions of the classical Flory-Huggins theory<sup>23</sup>. For binary mixtures to be miscible the second derivative of the free energy of mixing (at fixed temperature and pressure) which is composed of incompressible and compressible contributions should satisfy the relation<sup>24</sup>

$$\partial^2 G / \partial C^2 - v\beta (\partial^2 G / \partial C \partial v)^2 > 0 \quad (3.9)$$

where  $G$ ,  $C$ ,  $v$  and  $\beta$  refer to the molar Gibbs free energy, concentration, specific volume and the compressibility of the mixture, respectively. The second term in Eqn. (3.9) is always negative, thus giving an unfavorable effect on mixing. Since  $\beta$  increases with temperature, this term becomes more pronounced at

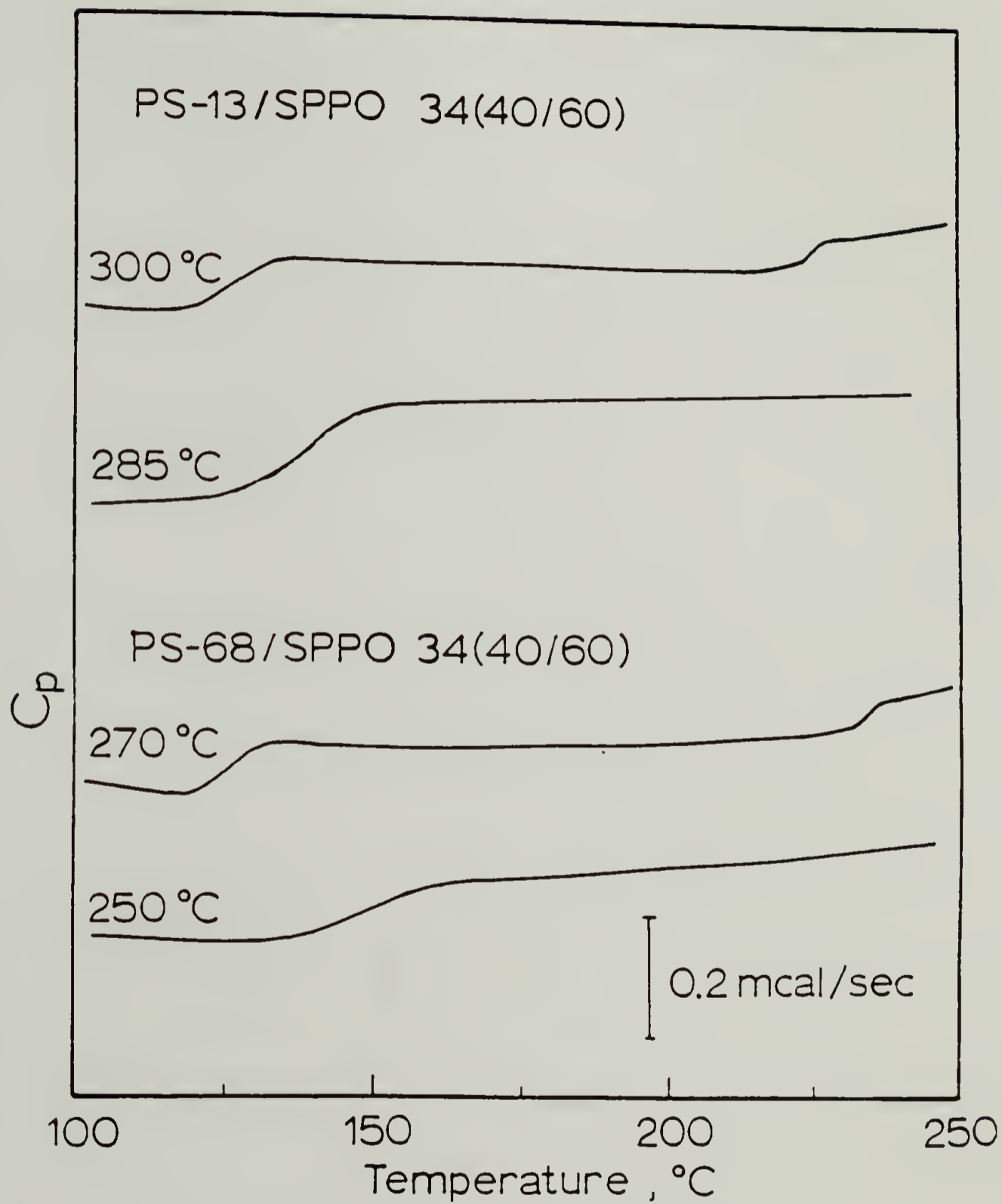


Figure 3.16. DSC thermograms of blends of SPPO 34 and PS of different molecular weights annealed at the indicated temperatures

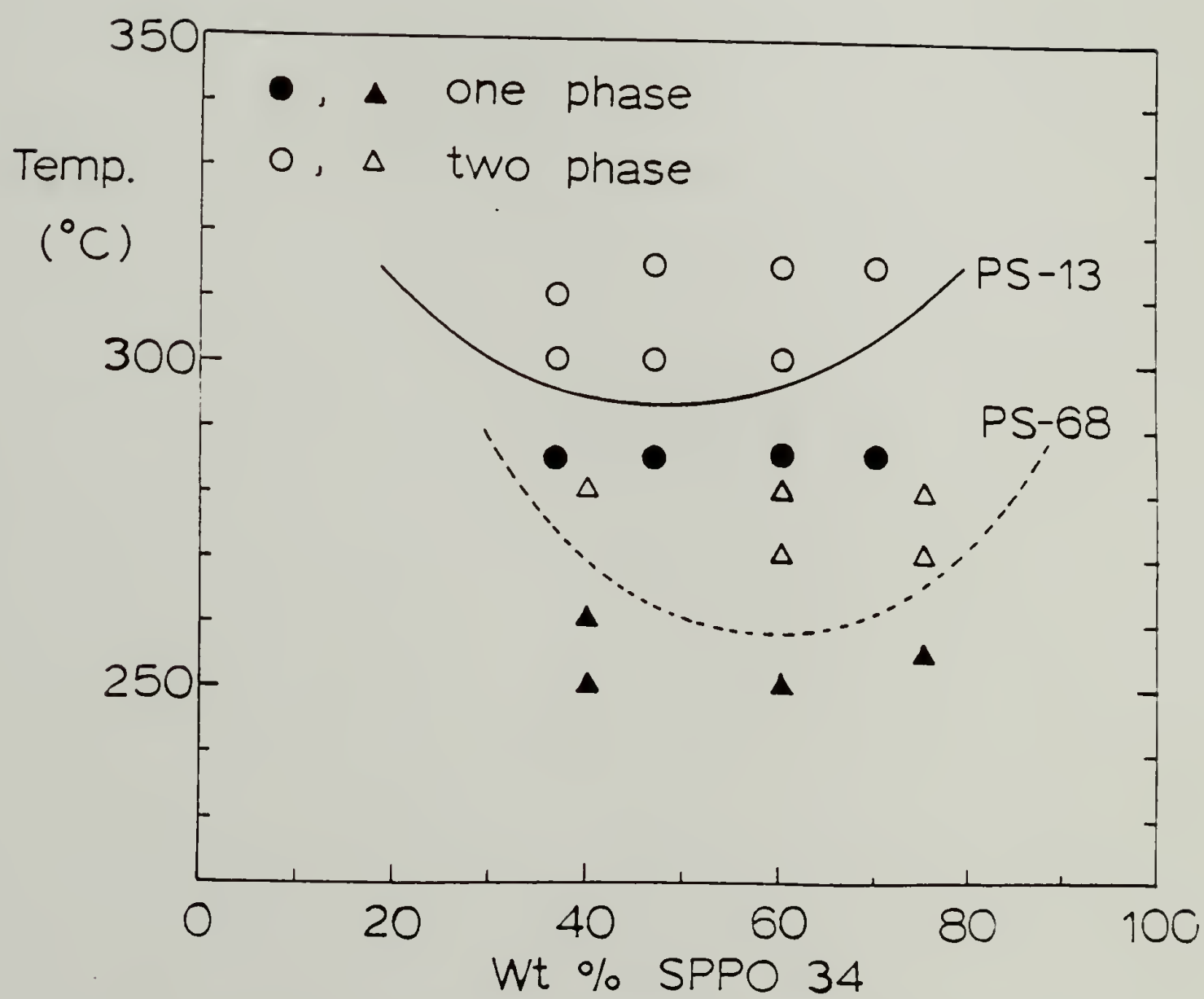


Figure 3.17. Phase diagram for blends of PS/SPP0 34

higher temperature, thus resulting in the destabilization of the mixture at high temperature. In this system a weak intermolecular interaction (which is directionally dependent in nature<sup>25</sup>) between PS and PPO segments is also involved. Thus, at higher temperature this interaction will be diluted by randomization by which the combinatorial entropy of mixing will be regained more or less. It should be noted that this orientational effect was neglected in the original equation of state theory. However, the unfavorable compressibility contributions appear more dominant than the entropy regain, thus explaining the occurrence of phase separation at elevated temperature.

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## CHAPTER IV

### MONOMER SEQUENCE DISTRIBUTIONS IN POLY(STYRENE-CO-ACRYLONITRILE)

A microstructure of copolymer, more specifically, a comonomer sequence distribution is known to affect miscibility behavior by varying intrachain interactions. A model to take into account that effect on the miscibility behavior has been proposed by Balazs et al<sup>1</sup>.

styrene[1]-acrylonitrile[2] (SAN) copolymers, unless special processes are employed, tend to have an alternating sequences during copolymerization because a product of the monomer reactivity ratio,  $r_1 r_2$ , is much smaller than unity ( $r_1 = 0.52$ ,  $r_2 = 0.03$ )<sup>2</sup>.

Accordingly, studies of comonomer sequence distribution in SAN copolymers employed in this work were carried out by dielectric relaxation and  $T_g$  measurements to see if these copolymers are of quite random in nature, and are presented in this chapter.

A comparison of experimentally determined dipole moments with those calculated on the basis of the rotational isomeric state

model<sup>3</sup> can provide information on the microstructures of vinyl polymers or copolymers such as the degree of stereoregularity, tacticity or monomer sequence distribution<sup>4-8</sup>. The dielectric properties of the copolymers obtained by frequency plane measurements are correlated with considerations of dyad distributions calculated from monomer reactivity ratios, which allows us to deduce information on intra- and intermolecular interaction in copolymers<sup>9</sup>.  $T_g$  measurements are interpreted on the basis of an expression proposed by Johnston<sup>10</sup> which considers the effect of monomer sequence distribution on the  $T_g$  of copolymers.

#### A. Experimental Section

The SAN copolymers (SAN 5 - SAN 48) were obtained from Dow Chemical Co., courtesy of Dr. Sue McKinley; SAN 76 was supplied by Du Pont Co., Courtesy of Dr. R. Saxton. Polymer compositions were determined by nitrogen analysis.

Molecular weights and densities of molded films were determined as described in Chapter II. The molecular weight of SAN 76 could not be measured because of its insolubility in THF. The inherent viscosity of SAN 76 at the concentration of 0.5 g/dl was 0.63 dl/g in *n*-butyrolactone at 35°C.  $T_g$  measurements were performed

similarly as described in Chapter II. Samples of monodisperse polystyrene (Polymer Laboratories,  $\bar{M}_w = 115,000$ ) and samples of polyacrylonitrile (Polysciences, Inc.) were also subjected to  $T_g$  measurements. All characterization details are listed in Table 4.1.

Dielectric measurements for the SAN copolymer samples, which were obtained by compression molding into films, were carried out isothermally at 56 discrete frequencies in the range of 20 Hz to 100 KHz with a General Radio model 1689M RLC Digibridge. Samples approximately 0.3 mm thick were employed with an active electrode cell diameter of 3.3 cm. The temperature of the sample assembly was maintained within  $\pm 0.2^\circ\text{C}$  with a thermocouple in contact with the sample disc in the Polymer Laboratories DETA head. At least 1 hr was required for the temperature to reach equilibrium between measurements. Temperature scan modes at 1, 10, 50 KHz over a temperature range from  $-155$  to  $170^\circ\text{C}$  were also used. The temperature was raised at a rate of  $2.0^\circ\text{C}/\text{min}$ .

## B. Results and Discussion

Figure 4.1 and 4.2 display  $\epsilon'$  and  $\epsilon''$  for SAN 32 on the frequency plane, respectively; Figure 4.3 shows the Argand diagram (Cole-Cole plot) for SAN 32. Good superposition over a range of

Table 4.1

Compositions and Properties of Poly(styrene-co-acrylonitrile)

Sample	AN		$\bar{M}_n \times 10^{-5}$	$\bar{M}_w \times 10^{-5}$	$T_g$ (°C)
	Mole %	Wt %			
SAN 5	11.5	5.4	1.18	3.34	109
SAN 18	33.4	18.0	1.24	2.10	111
SAN 21	38.1	21.2	0.92	1.59	113.7
SAN 26	44.8	26.2	1.34	2.23	112.5
SAN 32	52.0	32.1	1.56	2.80	111.6
SAN 48	67.6	47.7	1.09	2.28	113.7
SAN 76	86.0	76.0	a)		108.0

a) see text.

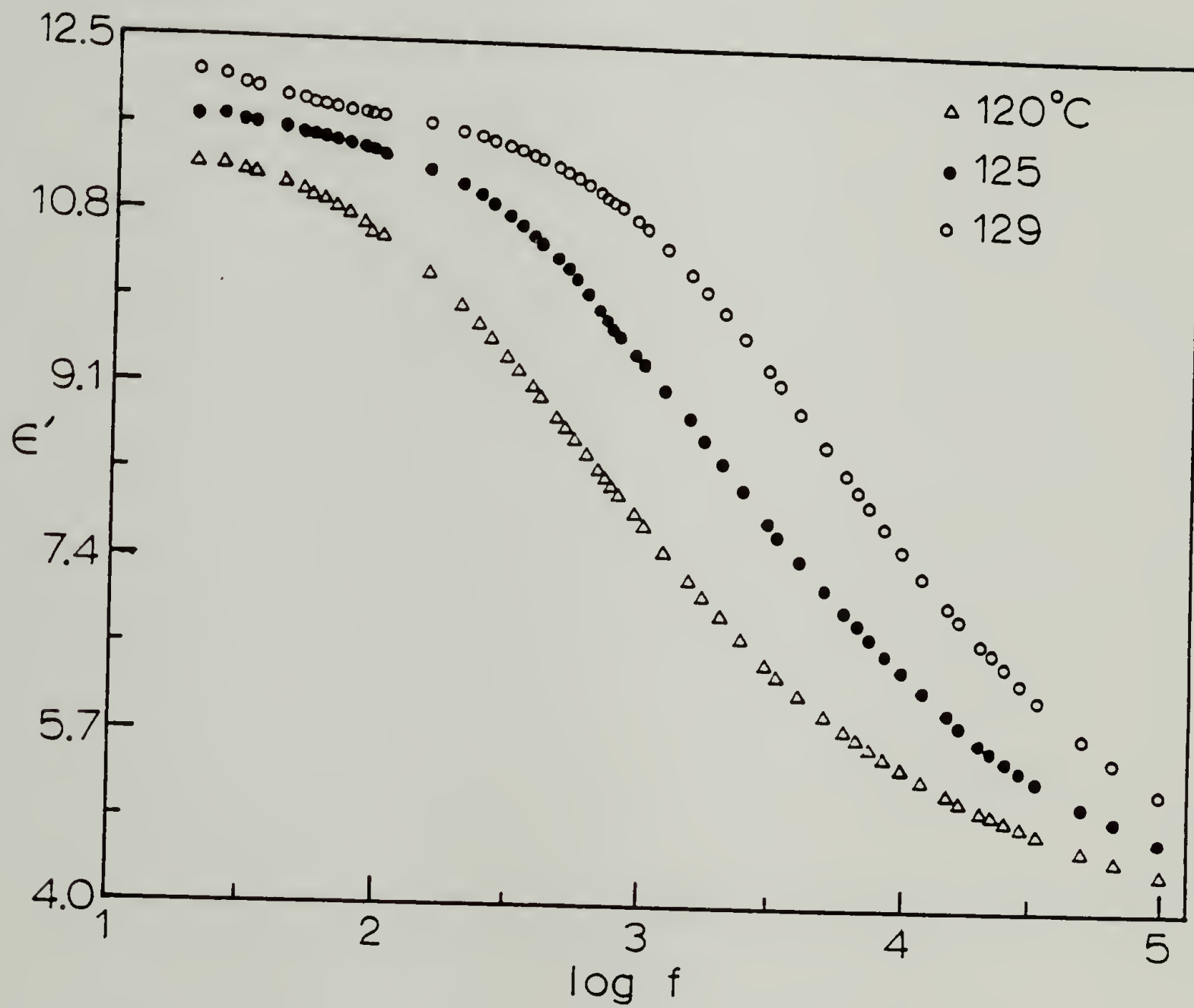


Figure 4.1. Frequency dependence of dielectric constant,  $\epsilon'$ , for  
SAN 32

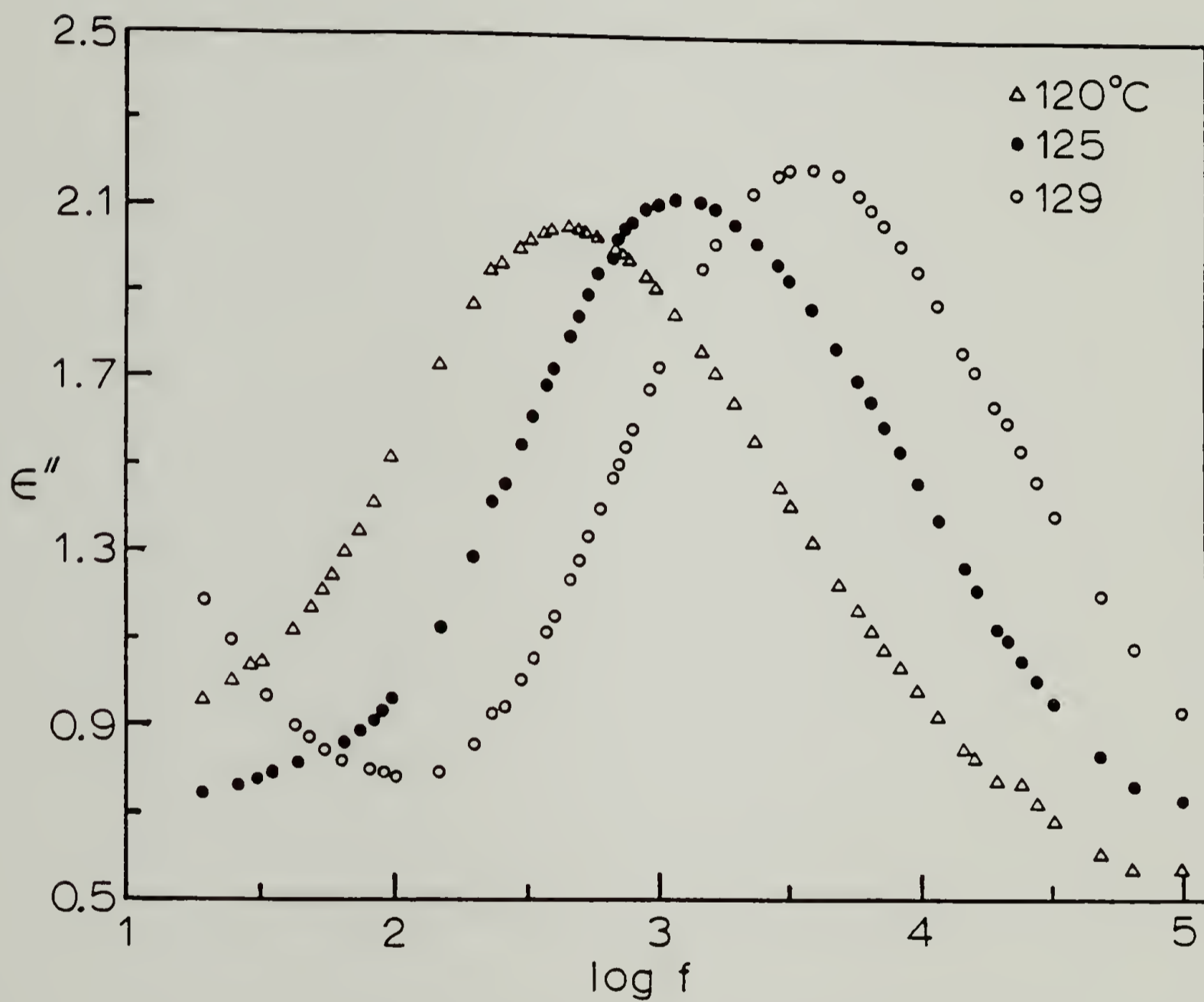


Figure 4.2. Frequency dependence of dielectric loss factor,  $\epsilon''$ ,  
for SAN 32

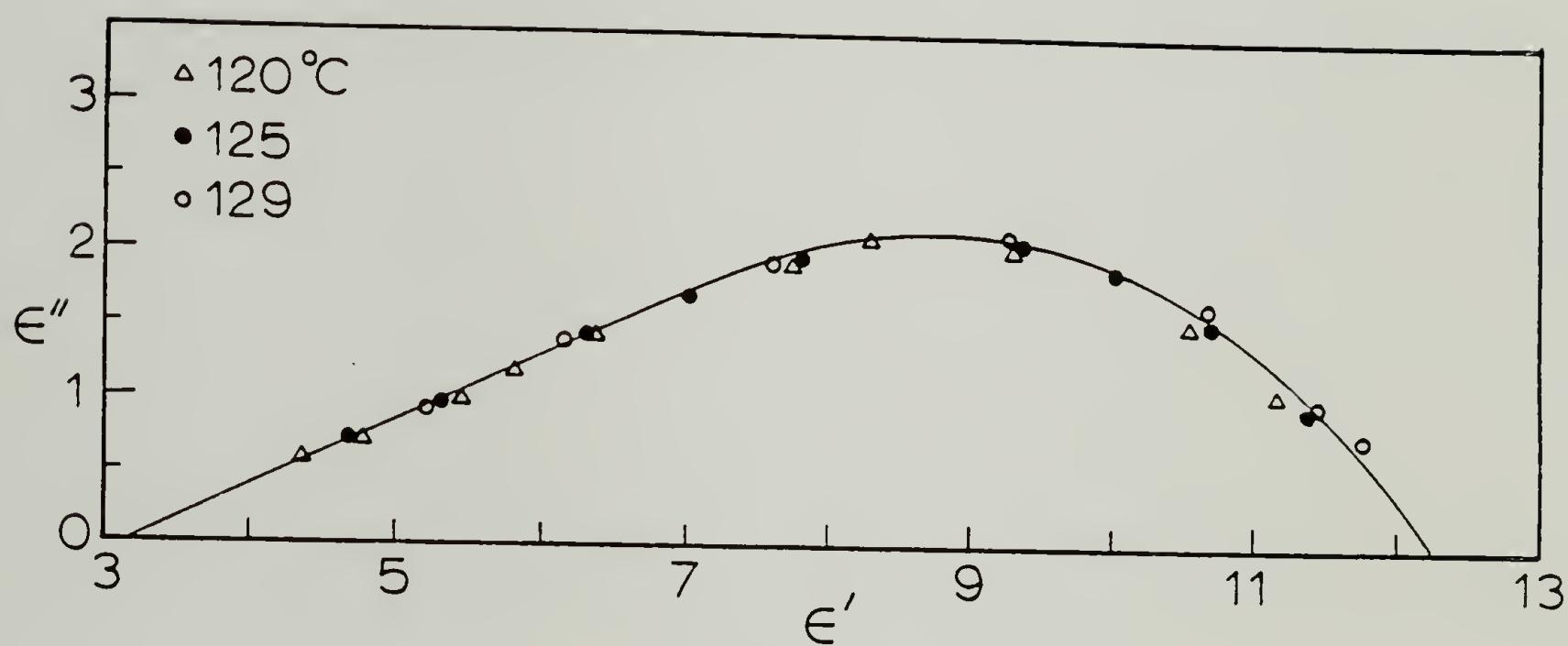


Figure 4.3. Argand diagram for SAN 32 in the  $\alpha$  relaxation region

temperatures is observed. The limiting low frequency ( $\epsilon_R$ ) and high frequency ( $\epsilon_u$ ) dielectric constants were obtained from Figure 4.3.

Considering only long-range dipolar interactions, Onsager<sup>11</sup> derived the relation which predicts the effective dipole moments per repeat unit ( $\mu_e$ ) :

$$\mu_e^2 = [9kT(2\epsilon_R + \epsilon_u)(\epsilon_R - \epsilon_u)]/[4\pi N\epsilon_R(\epsilon_u + 2)^2] \quad (4.1)$$

where  $k$  is the Boltzman constant,  $T$  is the absolute temperature, and  $N$  is the number of monomer units per unit volume which is calculated by

$$N = A\rho/(X_1M_1 + X_2M_2) \quad (4.2)$$

where  $A$  is Avogadro's number,  $X_i$  is the mole fraction and  $M_i$  is the comonomer repeat unit molecular weight. The room temperature density values ( $\rho$ ), as displayed in Figure 4.4, and a temperature of 400K were employed throughout all calculations.

The dielectric relaxation strength,  $\epsilon_R - \epsilon_u$ , and  $\mu_e^2$  are listed in Table 4.2. Figure 4.5 shows the dipole moments of the copolymers as a function of composition. Data shown by open circles

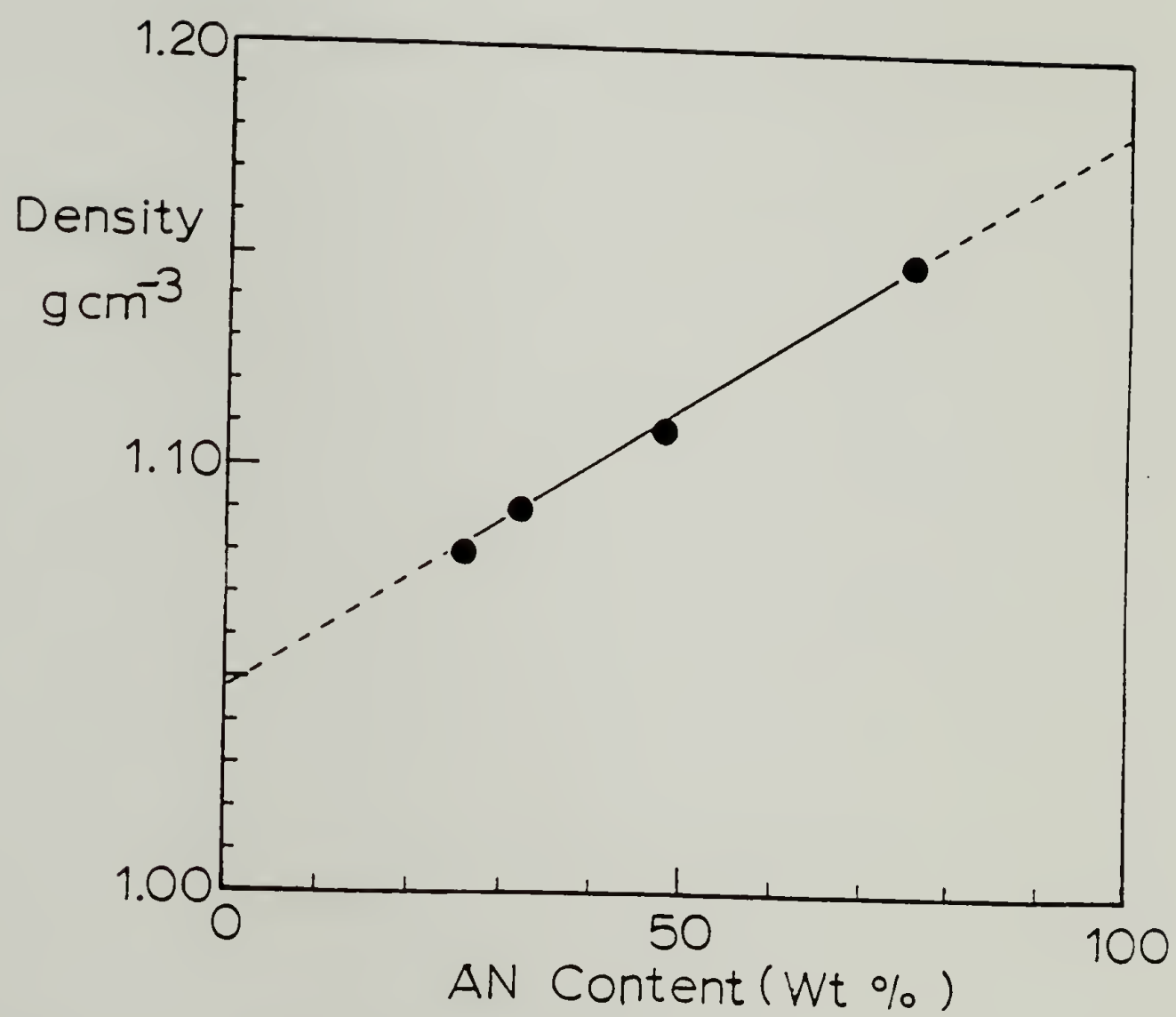


Figure 4.4. Density of copolymers as a function of AN content

Table 4.2

Dielectric Parameters for Poly(styrene-co-acrylonitrile)

Sample	$\epsilon_R - \epsilon_u$	$\mu e^2$	g	$\alpha$	$\Delta H / \Delta L$	y	Width (Decades in Frequency)	
							0.5	0.75
SAN 5	1.45	0.85	0.62	0.42	1.42	0.64	2.18	1.36
SAN 18	3.75	1.96	0.52	0.34	1.30	0.52	2.30	1.40
SAN 21	4.85	2.15	0.50	0.36	1.38	0.50	2.14	1.30
SAN 26	6.15	2.85	0.56	0.32	1.24	0.56	2.24	1.43
SAN 32	9.10	3.55	0.61	0.30	1.24	0.62	2.24	1.37
SAN 48	9.10	3.40	0.45	0.31	1.45	0.30	2.45	1.44
SAN 76	19.9	5.61	0.58	0.40	-	0.55	-	2.04

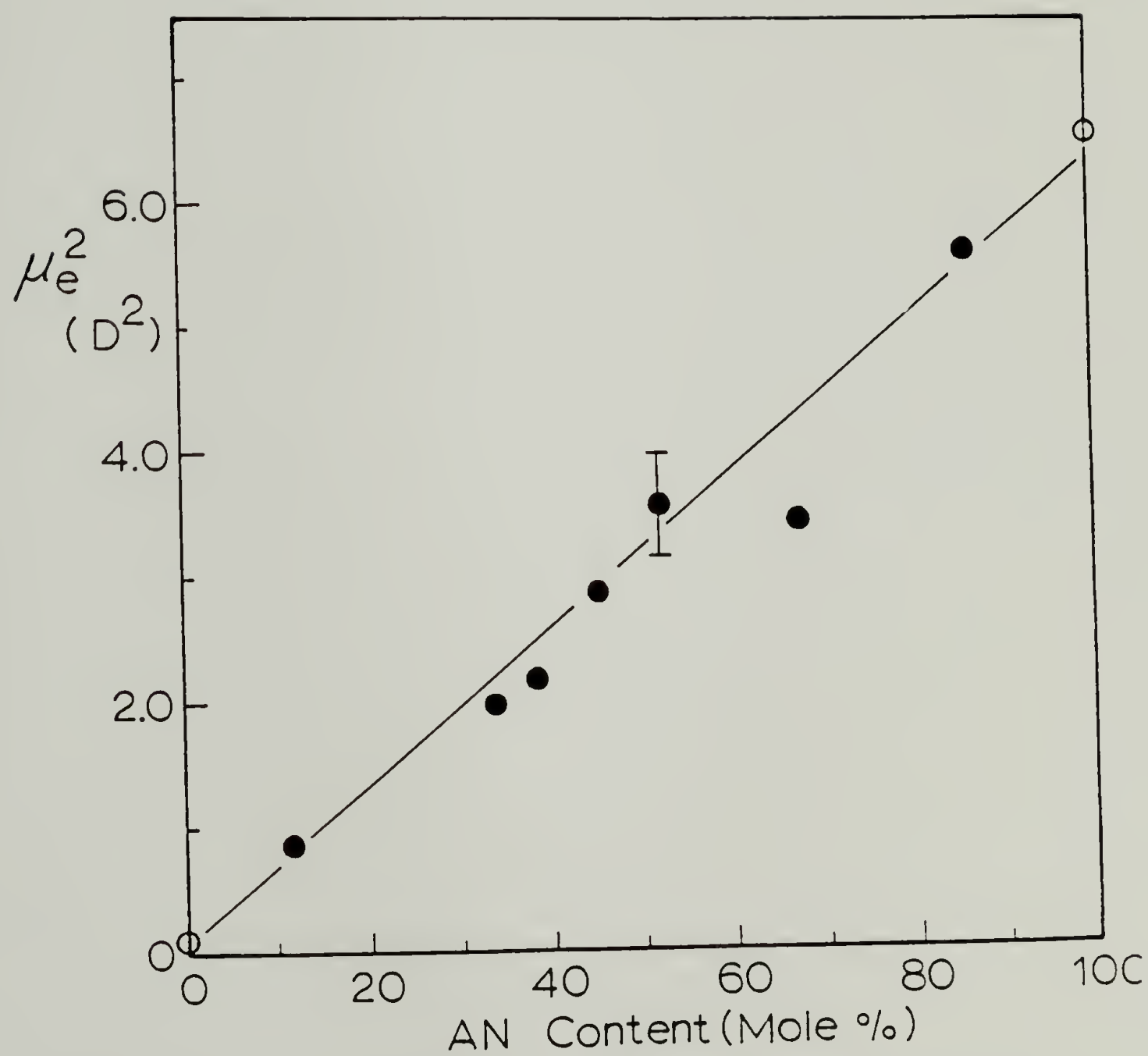


Figure 4.5. Effective dipole moments of copolymers

were obtained from refs. 17 and 18. It can be seen that SAN 48 exhibits a somewhat lower dipole moment; possible explanations will be discussed later.

Kirkwood-Frohlich<sup>12</sup> introduced the orientation correlation function,  $g$ , which takes into account short-range intrachain interactions between a reference molecule and its nearest neighbors.  $g$  is defined by

$$g = \mu_e^2 / \mu_o^2 \quad (4.3)$$

where  $\mu_o^2$  is the square of the dipole moment of an isolated monomer unit. For copolymers

$$\mu_o^2 = x_1(\mu_{1,0})^2 + x_2(\mu_{2,0})^2 \quad (4.4)$$

where  $\mu_{1,0}$  and  $\mu_{2,0}$  are the dipole moments of model compounds 1 and 2, respectively.  $\mu_{1,0} = 0.36D^{13}$  (dipole moment of toluene) and  $\mu_{2,0} = 3.34D^{13}$  (dipole moment of propionitrile) were used in the calculation. The  $g$  values thus obtained are plotted as a function of AN content in Figure 4.6 and are observed to increase slightly with decreased AN content because of dilution of the nitrile group through copolymerization which results in reduced barriers to internal

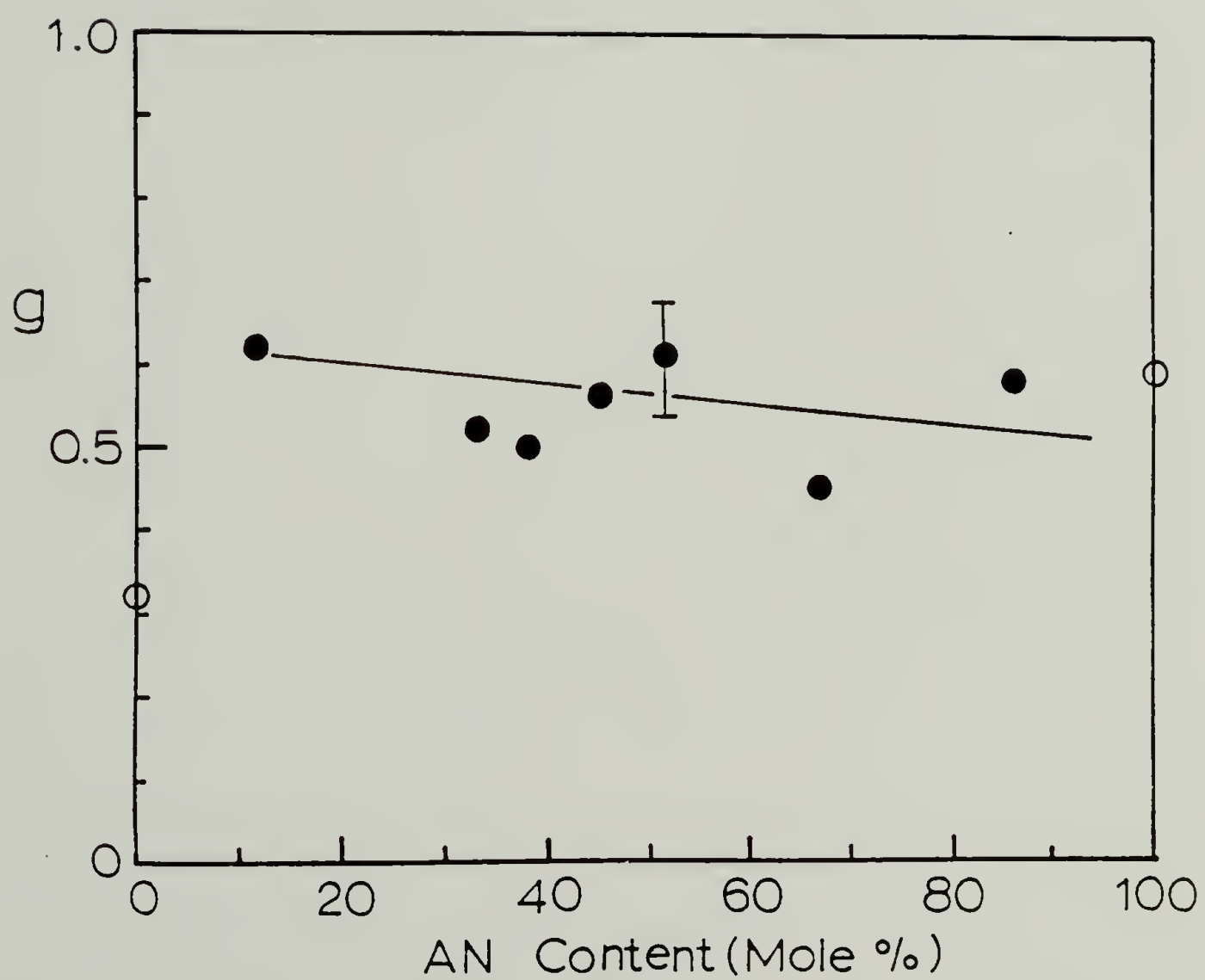


Figure 4.6. Composition dependence of the correlation parameter,  $g$ , for SAN copolymers

rotation. Nevertheless, the hindrance to internal rotation appears to be not much different for all the copolymers.

$(\epsilon_R - \epsilon_U)$ , which is a measure of the orientation polarization, can be calculated from the area under an  $\epsilon''$  versus  $1/T$  curve according to the relation<sup>14</sup>

$$(\epsilon_R - \epsilon_U) = (2E/\pi R) \int_{-\infty}^{\infty} \epsilon'' d(1/T) \quad (4.5)$$

where  $E$  is the activation energy. For SAN 76 the variations of  $\epsilon''$  with temperature at three frequencies are shown in Figure 4.7, in which two relaxation regions are observed similarly to the results of Cook et al<sup>15</sup> for SAN copolymers with 25% AN content. The high temperature  $\alpha$  process is related to the large scale Brownian motion of the dipoles. The lower temperature  $\beta$  process around  $-25^\circ\text{C}$  is due to limited motions of dipoles in the glassy state. Due to the presence of DC conductivity effects<sup>14</sup> in the data at lower frequencies, the data at 50 KHz were used in the calculation. The areas under the  $\epsilon''$  vs  $1/T$  plots were determined after symmetric extrapolation of the loss peaks, as seen in Figure 4.8. By using the activation energy ( $E = 80$  kcal/mole) calculated from the slope of the linear portions of Arrhenius plots,  $(\epsilon_R - \epsilon_U)$  was calculated to be 20.7, which is consistent with the value obtained from the Argand diagram for SAN 76.

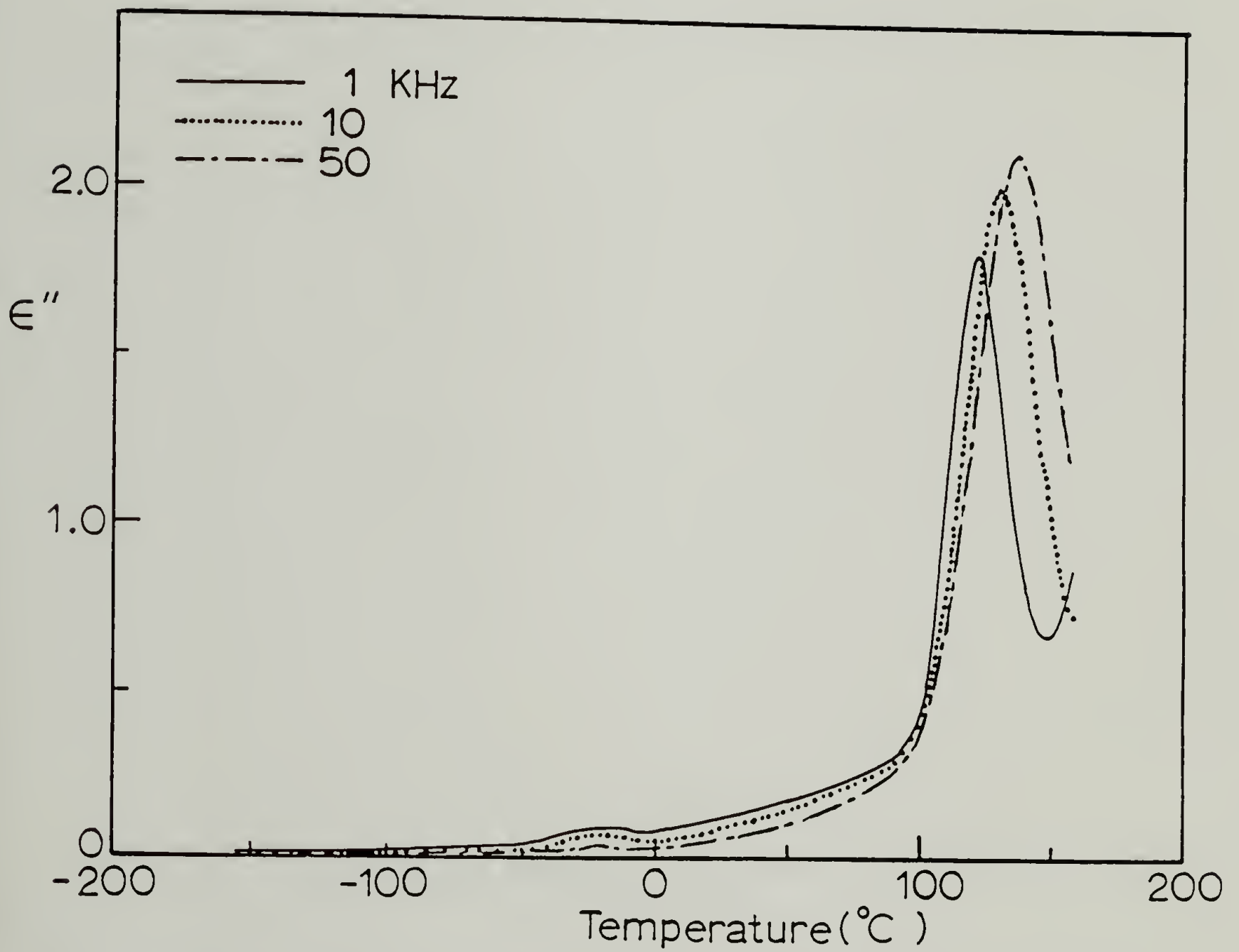


Figure 4.7. Temperature dependence of dielectric loss factor,  $\epsilon''$ , for SAN 76

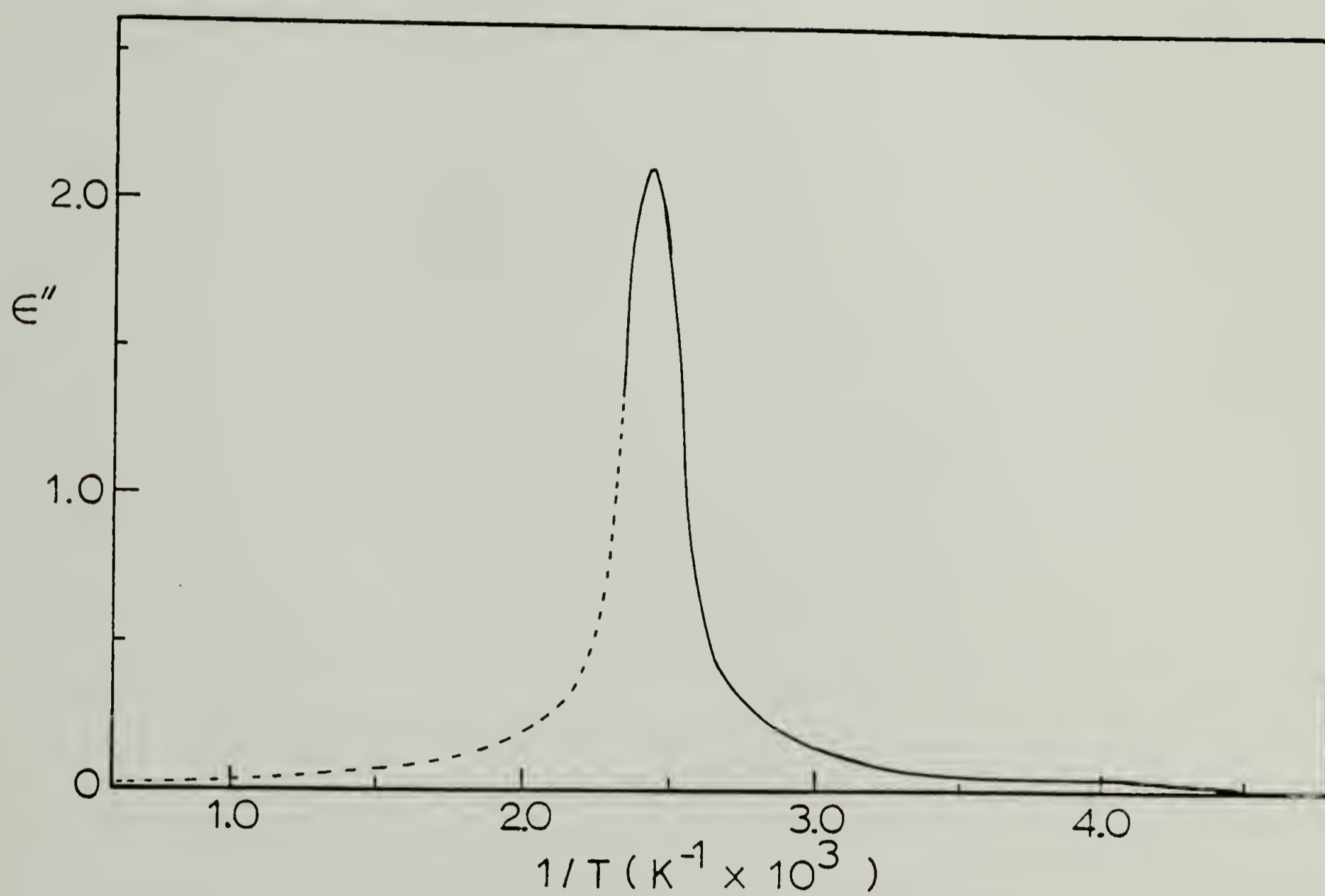


Figure 4.8. Dielectric loss factor  $\epsilon''$  as a function of reciprocal temperature at 50 KHz for SAN 76

Figure 4.9 shows the frequency dependence of the normalized dielectric loss of SAN 32, which indicates that the temperature-frequency superposition is applicable over the temperature range studied. Table 4.2 also lists the loss half widths which are the distances in decades of frequency between the right and left hand branches of normalized curves at half-height. The half widths span the range of 2.1 to 2.5. These values are similar to those obtained by Williams et al for SAN copolymers<sup>15</sup> (25 and 32.5 wt% AN) and other amorphous polymers<sup>16</sup>. The normalized loss widths are plotted as a function of composition in Figure 4.10. It is noted that the width of the loss curves remains essentially constant except for copolymer SAN 76, which exhibits a far broader relaxation than the other copolymers. However, its  $g$  value is not significantly different from those of the others.

The ratios  $\Delta H/\Delta L$  representing the ratio of the distance of the high frequency branch at half-height from  $\log (f/f_m) = 0$  to that of the low frequency branch at half-height from  $\log (f/f_m) = 0$  (thus reflecting the asymmetry of the dispersion curve) are collected in Table 4.2. Table 4.2 also lists the Cole-Cole parameter  $\alpha$ , which is obtained from the linear portion of a plot of  $\epsilon''$  versus  $\epsilon'$  at high frequencies at an angle of  $\alpha\pi/2$  with the  $\epsilon'$  axis, whose magnitude is inversely related to the departure from a single relaxation time associated with semi-circular arc in the Argand diagram.

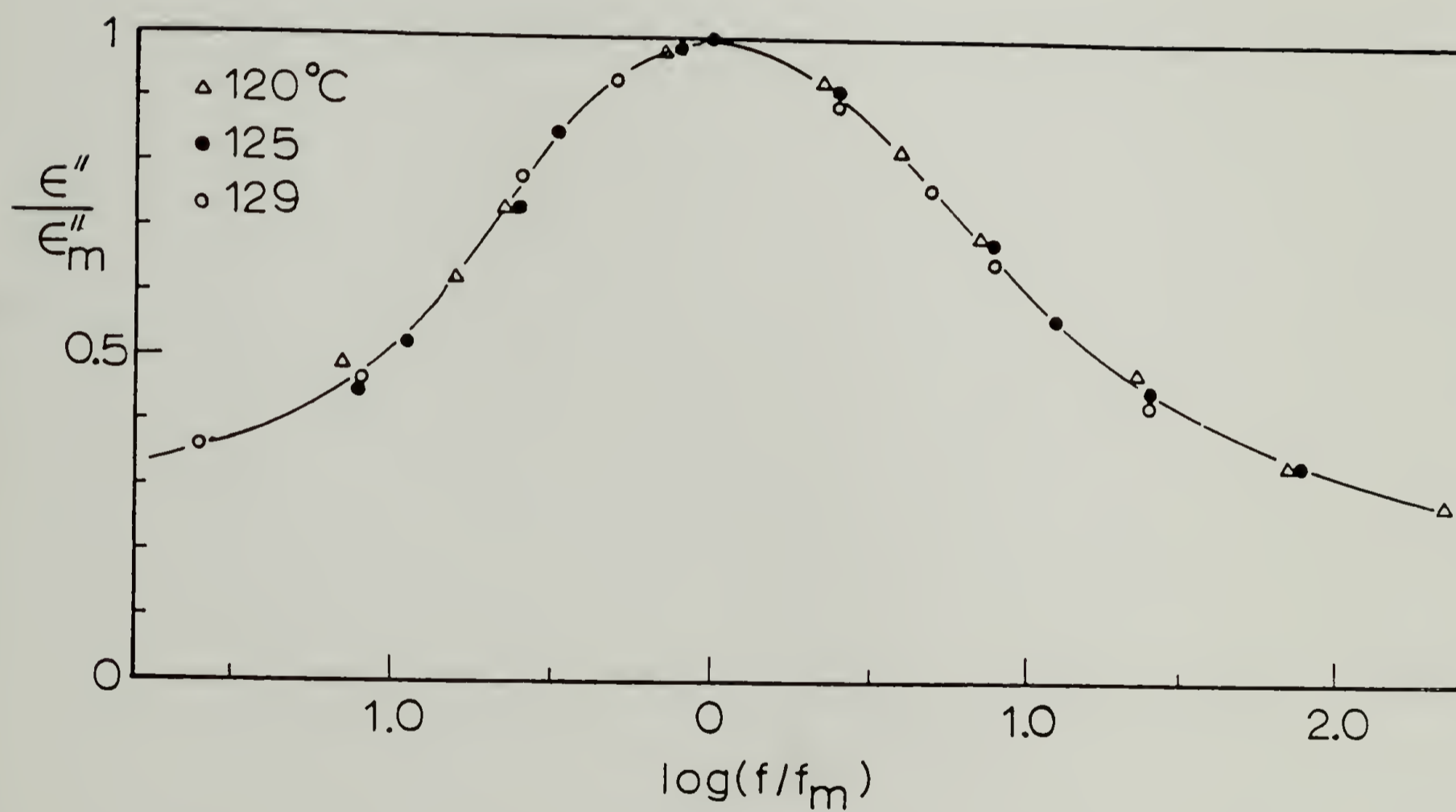


Figure 4.9. Frequency dependence of the normalized dielectric loss for SAN 32

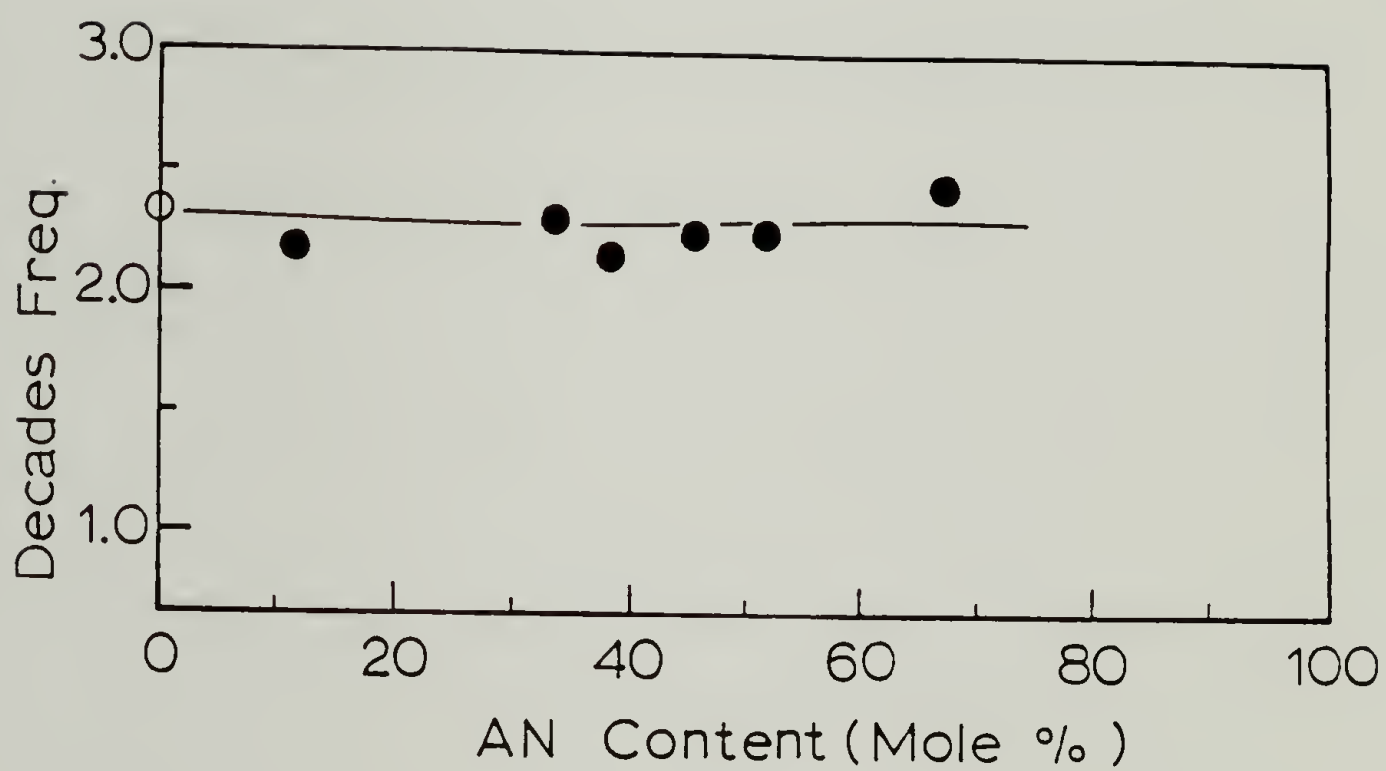


Figure 4.10. Composition dependence of the half width of the dielectric loss for SAN copolymers. The point shown by the open circle was obtained from ref. 17

It can be seen that all the shape parameters of the relaxation spectra collected in Table 4.2 are similar, indicating small differences in the conformational characteristics of the relaxing chains and the random nature of the copolymers. Although information on the details of polymerization for each copolymer is not available at present, it appears likely that an addition of a more reactive styrene monomer is continued throughout the polymerization at a rate designed to maintain a constant ratio of styrene to acrylonitrile monomers thus resulting in random SAN copolymers with less compositional heterogeneity.

The composition dependence of  $g$  i.e., the angular correlations between comonomer units in these copolymers can be correlated with a very simple model in which dipolar cancelling is assumed to arise from the geometry of dyads alone<sup>9,17</sup>. The dyad fractions,  $F_{11}$ ,  $F_{22}$ , and  $F_{12}$  can be determined for random copolymers from the conditional probability  $P_{ij}$  (the probability that the given unit "i" is followed by unit "j"), which is calculated from copolymer compositions and reactivity ratios. As described thoroughly by Alexandrovich<sup>9</sup>, the instantaneous copolymerization equation is given by :

$$n = (r_1 N + 1) / (r_2 / N + 1) \quad (4.6)$$

$$n = X_i/X_j = \text{copolymer monomer ratio}$$

$$N = X_I/X_J = \text{feed monomer ratio}$$

The conditional probability,  $P_{ij}$ , is given by :

$$P_{ij} = 1/(r_1 N + 1) = 1 - P_{ii} \quad (4.7)$$

Combination of Eqn. (4.6) and (4.7) leads to the following relation for  $P_{ii}$ , in terms of the known copolymer composition,  $n$ , and the reactivity ratio product  $R = r_1 r_2$ .

$$[n(1 - R)]P_{ii}^2 + [1 + n(2R - 1)]P_{ii} - nR = 0 \quad (4.8)$$

If  $P_{ii}$  is determined for a given copolymer, the other conditional probabilities can be obtained from the copolymer compositions in terms of mole fractions  $X_i$  and  $X_j$  ;

$$P_{ij} = 1 - P_{ii}$$

$$P_{ji} = 1 - P_{jj}$$

$$X_i P_{ij} = X_j P_{ji} \quad (4.9)$$

Dyad fractions  $F_{ii}$ ,  $F_{jj}$  and  $F_{ij} = F_{ji}$  can be calculated :

$$F_{ii} = X_i P_{ii}$$

$$F_{ij} = X_i P_{ij}$$

$$F_{jj} = X_j P_{jj}$$

$$F_{ji} = X_j P_{ji}$$

$$F_{ii} + F_{jj} + 2F_{ij} = 1 \quad (4.10)$$

The reactivity ratios,  $r_1 = 0.52$  and  $r_2 = 0.03^2$  were used in the calculations.

The dipole moments are then calculated from the expression<sup>9</sup>

$$\begin{aligned} \mu_e^2 = & g_1 F_{11} (\mu_{1,0})^2 + g_2 F_{22} (\mu_{2,0})^2 \\ & + y 2F_{12} \{[(\mu_{1,0})^2/2] + [(\mu_{2,0})^2/2]\} \end{aligned} \quad (4.11)$$

where  $g_1$ ,  $g_2$  refer to the appropriate homopolymer values and  $y$  is the correlation factor for the mixed dyad. In the calculation  $g_1 =$

$0.32^{17}$  and  $g_2 = 0.59$  were employed. The latter was calculated using Eqn. (4.1) - (4.4) from the dielectric relaxation strength ( $\epsilon_R - \epsilon_u = 32$ )<sup>18</sup> and the density of  $1.18 \text{ g/cm}^3$  for the polyacrylonitrile homopolymer. Table 4.2 also lists the  $y$  values thus determined which are consistent with Kirkwood-Frohlich orientation correlation function  $g$ . However, SAN 48 may contain some alternating sequences as indicated by the  $T_g$  measurements.

Considering the effect of adjacent dissimilar monomer units on steric and intramolecular interactions in the copolymer backbone, Johnston<sup>10</sup> reported a relation predicting the copolymer glass transitions from the conditional probability  $P_{ij}$  which takes into account the copolymer sequence distribution.

$$\begin{aligned} 1/T_{gp} = & (W_i P_{ii}/T_{gii}) + [(W_i P_{ij} + W_j P_{ji})/T_{gij}] \\ & + (W_j P_{jj}/T_{gjj}) \end{aligned} \quad (4.12)$$

where  $T_{gp}$  is the  $T_g$  of a copolymer containing weight fraction  $W_i$  and  $W_j$  of two monomer units  $i$  and  $j$  which have the conditional probabilities  $P_{ii}$ ,  $P_{ij}$ ,  $P_{ji}$ , and  $P_{jj}$  of having various linkages contributing the  $T_g$ 's of  $T_{gii}$ ,  $T_{gij} = T_{gji}$ , and  $T_{gjj}$  to the copolymer. Here,  $T_{gii}$  and  $T_{gjj}$  can be regarded as the  $T_g$ 's of

polystyrene and polyacrylonitrile, respectively and  $T_{gij}$  is taken as the  $T_g$  of SAN alternating copolymers. The  $T_g$  of polystyrene measured in this work is  $107^\circ\text{C}$ , which is higher than that reported in the literature<sup>10</sup>. The  $T_g$  of polyacrylonitrile is determined to be  $105^\circ\text{C}$ . The experimentally determined  $T_g$ 's of the copolymers and the  $T_g$ 's predicted by employing either  $111.5^\circ\text{C}$ <sup>10</sup> or  $117^\circ\text{C}$ <sup>19</sup> as  $T_{gij}$  taken from different sources are plotted as a function of AN content in Figure 4.11 where the calculated fraction of S-AN dyads is also displayed. These data exhibit positive deviation from those predicted using the Fox equation and the deviation increases as the fraction of S-AN dyads increases as noted by Johnston<sup>10</sup>. This is ascribed, on the basis of Tonelli's calculation<sup>20</sup> of the conformational entropies of the various dyads in the SAN copolymer, to the fact that the conformational entropy of an S-AN dyad is smaller than half the sum of the entropies of S-S and AN-AN dyads if we assume that the  $T_g$  of a polymer is inversely related to the intramolecular equilibrium flexibility of a polymer chain.

The experimentally measured  $T_g$ 's are higher than those determined by Johnston<sup>10</sup>. However, the  $T_g$ 's fall between two predicted curves; a higher  $T_g$  was noted for SAN 48 which may be due to a large fraction of S-AN dyads resulting from a slightly higher

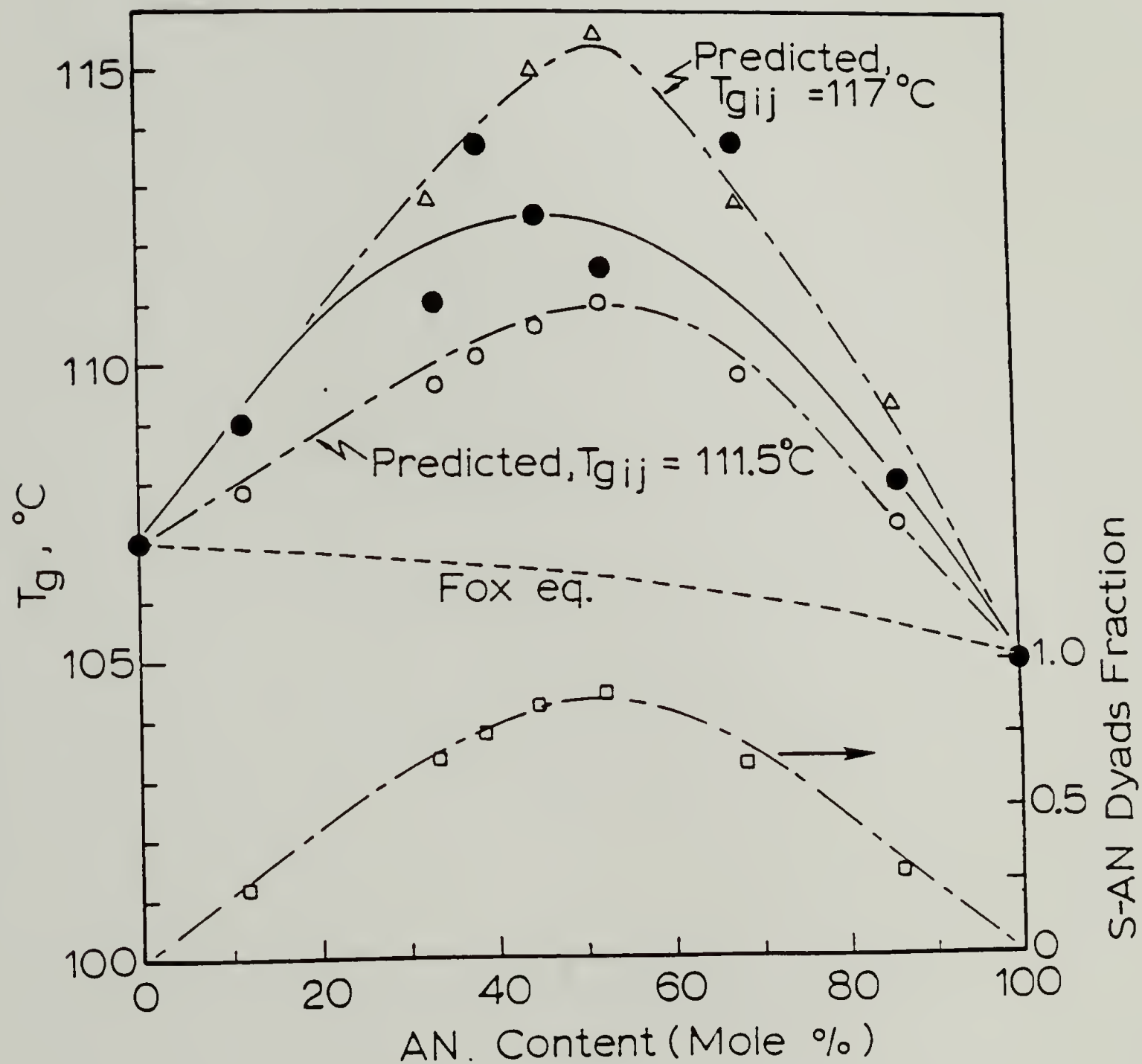


Figure 4.11.  $T_g$ 's determined experimentally and predicted by considering sequence distribution and the fraction of S-AN dyads calculated vs. mole% AN content

degree of alternating sequences than are present in the other copolymers.

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## CHAPTER V

### MISCIBILITY IN BLENDS OF POLY(STYRENE-CO-ACRYLONITRILE) WITH SPPO COPOLYMERS

This chapter describes studies of miscibility behavior in blends of poly(styrene-co-acrylonitrile) (SAN) with sulfonylated poly(2,6-dimethyl-1,4-phenylene oxide) (SPPO) copolymers, namely, blends of two random copolymers with four distinct repeat units. The isothermal composition-composition diagram displaying the miscibility-immiscibility boundary represented in Cartesian coordinates is interpreted on the basis of a mean field theory through which all the  $\chi_{ij}$ 's are determined. The primary experimental techniques employed to probe miscibility are DSC, dynamic mechanical spectroscopy and density measurements. Dielectric relaxation spectroscopy was also employed to explore the extent of miscibility on the basis of normalized dielectric loss spectra obtained from frequency plane measurements.

#### A. Experimental Section

Materials The preparation and properties of SPPO copolymers were described in Chapter II. The compositions and properties of SAN copolymers can be found in Chapter IV. The numerals following SPPO and SAN indicate its degree of sulfonylation by weight % and its AN content by weight %, respectively.

Blends involving SPPO copolymer for  $T_g$  measurements were prepared by dissolving the components in THF in the desired proportions and then casting in aluminum dishes. The solvent was allowed to evaporate slowly at ambient conditions for at least four days and the resulting films were further dried in a vacuum oven at 120°C for 72 hr to completely remove residual solvent. Blends of PPO with SAN copolymers were prepared by casting films from chloroform solutions.

For dynamic mechanical and dielectric measurements pellets of SAN copolymers were compression molded into films at 200°C under nitrogen and annealed above  $T_g$  in the DMTA or DETA furnace. The films of SPPO copolymers and their blends with either SAN 5 or SAN 18 were cast from chlorobenzene solution and dried in a vacuum oven followed by annealing above  $T_g$  in the DMTA or DETA furnace to remove residual solvent.

$T_g$  Measurements  $T_g$  measurements were performed similarly as described in Chapter II. All the samples were annealed in the DSC

pan at 290°C for 20 min before  $T_g$  measurements, unless otherwise noted.

Density Measurements Densities of cast films of blend samples were measured as described in Chapter II.

Dynamic Mechanical Measurements Dynamic mechanical measurements were carried out as described in Chapter II. The samples were measured under nitrogen at 1 Hz. The temperature range was from -150°C to 280°C at a heating rate of 4°C/min.

Dielectric Measurements Dielectric measurements were carried out with a General Radio model 1689M RLC Digibridge at 0.1, 1 and 10 KHz over a temperature range from -155°C to 280°C with a nitrogen purge. The temperature was raised at a rate of 2.0°C/min. Samples approximately 0.2 mm thick were employed with an active electrode cell diameter of 3.3 cm. Frequency plane measurements were also carried out as described in Chapter IV.

## B. Results and Discussion

Miscibility Map Figure 5.1 illustrates the DSC thermograms of SAN 26/SPP0 54 blends. The composition dependences of the  $T_g$ 's of these

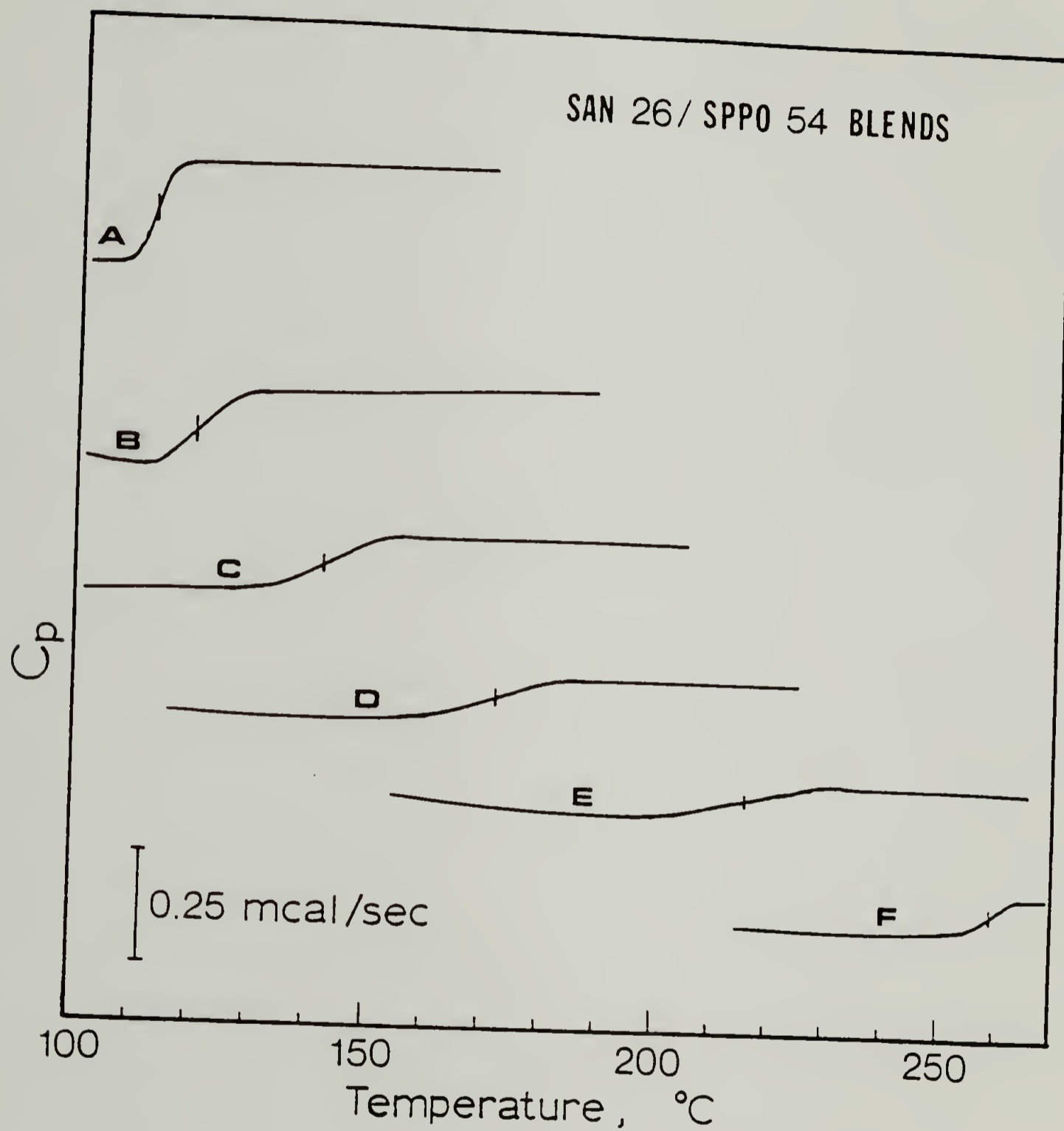


Figure 5.1. DSC thermograms of SAN 26, SPP0 54 and blends :

- (A) Pure SAN 26; (B) 25% SPP0 54; (C) 50% SPP0 54;  
 (D) 70% SPP0 54; (E) 85% SPP0 54; (F) Pure SPP0 54.

blends and a comparison to the  $T_g$ 's calculated using the Fox ( $k=0.4$ ) and Couchman equation<sup>1</sup> are shown in Figure 5.2. The pertinent parameters used in the calculation are  $\Delta C_p$  (SAN 26) = 0.32 J/g/deg and  $\Delta C_p$  (SPPPO 54) = 0.14 J/g/deg (refer to Chapter II). The experimental  $T_g$ 's are in reasonably good agreement with the values calculated. Figure 5.3 displays the composition dependences of the  $T_g$ 's of SAN 5/SPPPO 12 blends.

On the basis of a series of DSC analyses and by using the miscibility criterion of a single glass transition, the composition-composition diagram ("C-C plots") displaying the miscibility-immiscibility boundary for 50/50 wt% blends at 290°C was constructed and is shown in Figure 5.4.

Estimation of  $\chi_{ij}$ 's The blends of the type,  $(A_{1-x}B_x)_{n_1}/(C_{1-y}D_y)_{n_2}$ , involve six segmental interaction parameters where A, B, C and D refer to styrene, acrylonitrile, unsulfonylated phenylene oxide and sulfonylated phenylene oxide units, respectively. The  $\chi_{AC}^2$ ,  $\chi_{AD}$  and  $\chi_{CD}$  (refer to Chapter III) have been determined on the basis of a mean field treatment.

From the studies of Molau<sup>3</sup> on binary mixtures of SAN copolymers which differ only in chemical composition, the tolerable

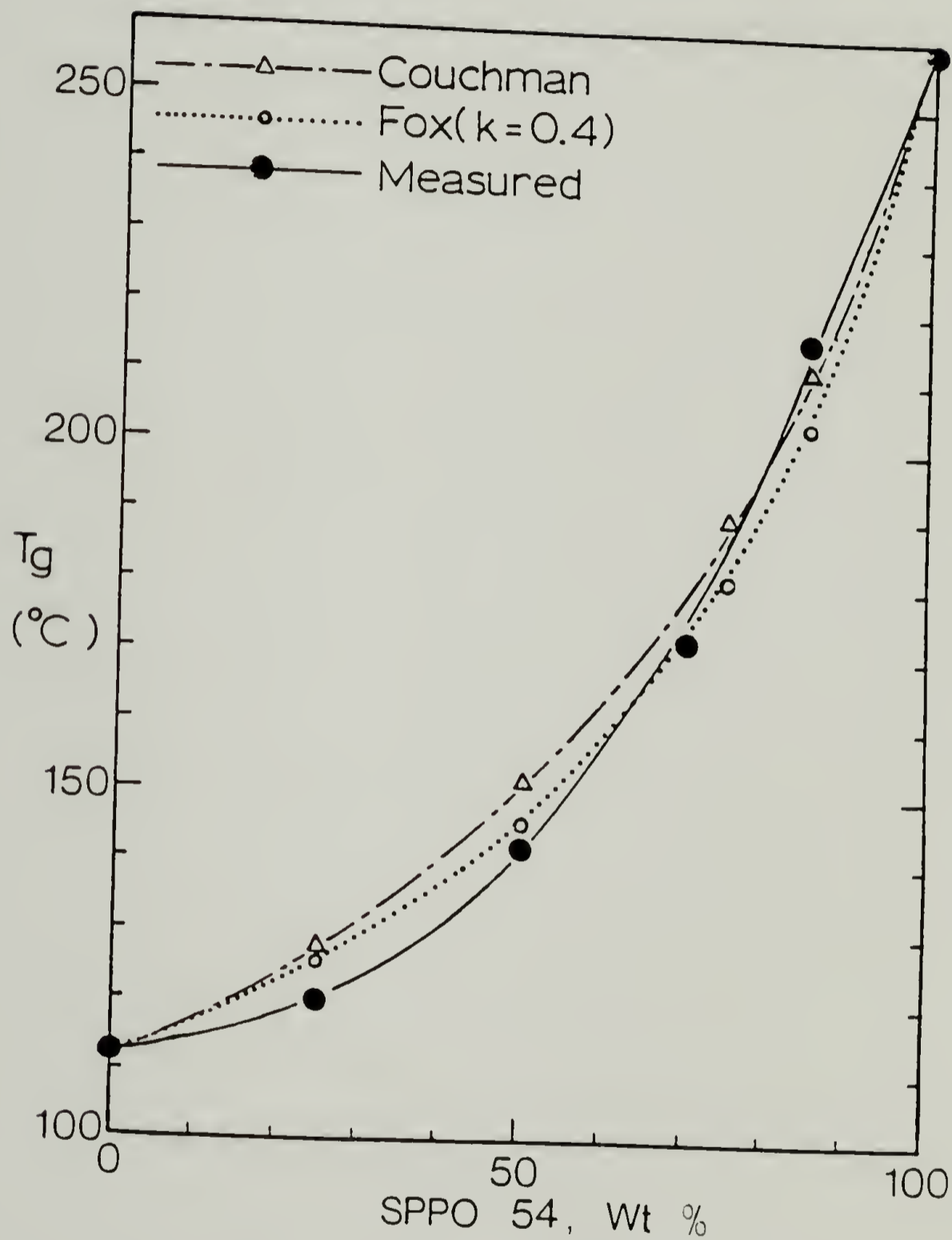


Figure 5.2.  $T_g$ 's vs. composition for SAN 26/SPPPO 54 blends.

Dashed lines represent the Couchman equation and dotted lines represent the Fox equation with  $k=0.4$ .

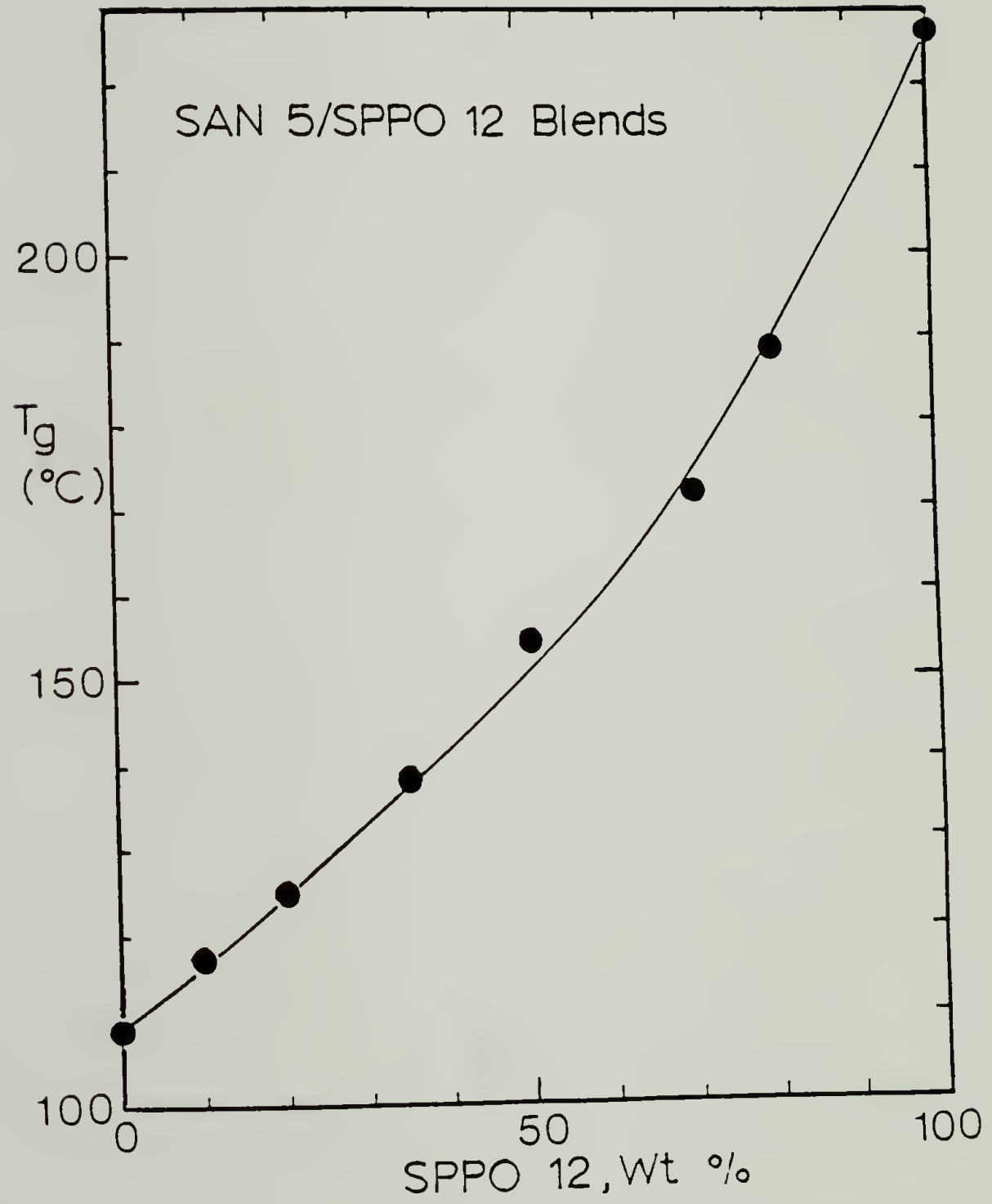


Figure 5.3.  $T_g$ 's vs. composition for SAN 5/SPPO 12 blends

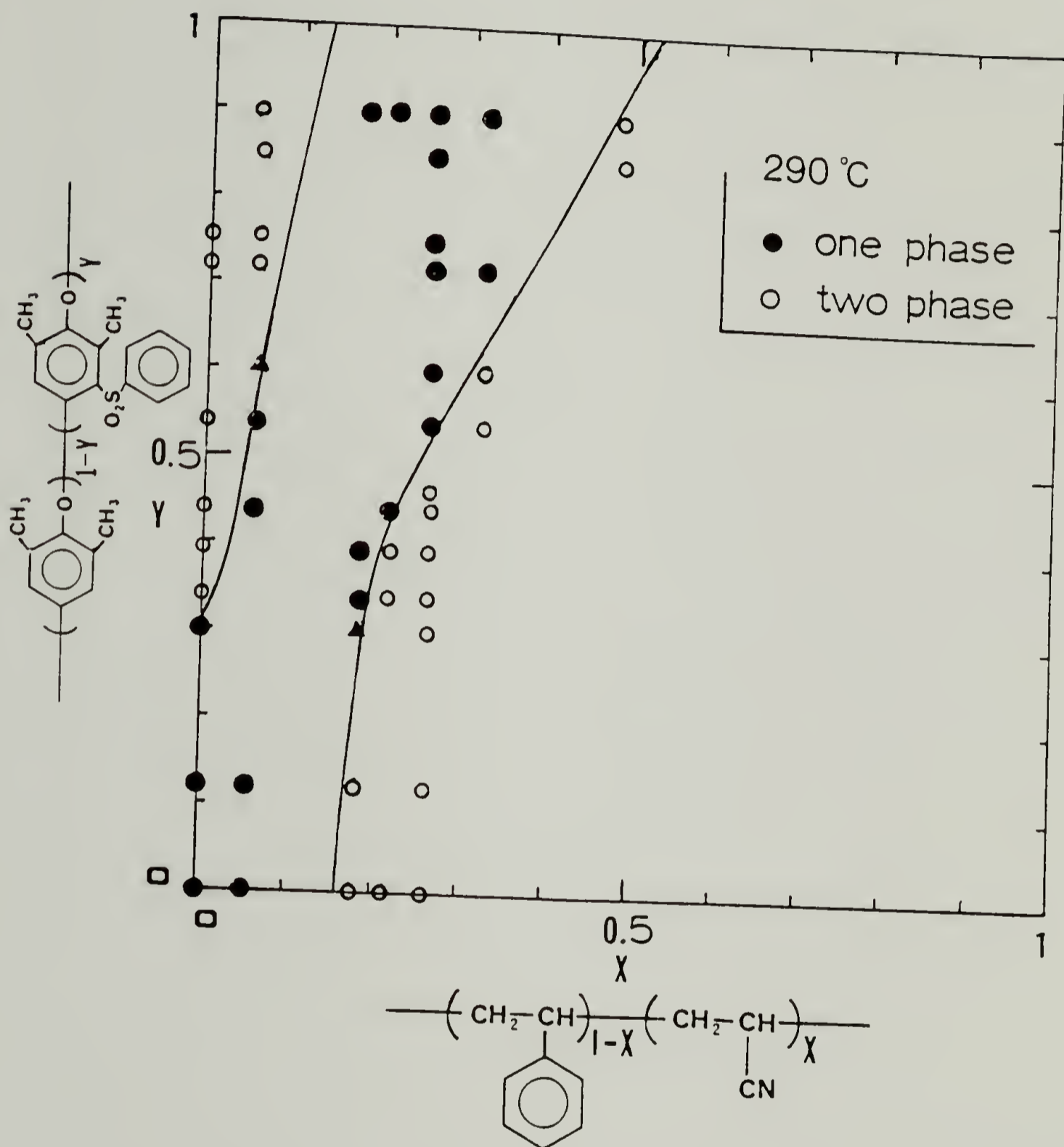


Figure 5.4. Miscibility domain for 50/50 wt% blends of SAN copolymers with SPPO copolymers at 290°C

difference in AN content ( $\Delta$ ) for miscibility was found to be 4%. On the basis of a mean field treatment, as described in Chapter I, the critical condition for these mixtures obeys the relation :

$$1/2(n_1^{-1/2} + n_2^{-1/2})^2 = \Delta^2 \chi_{AB} \quad (5.1)$$

From the Eqn. (5.1) and using  $n_1 = n_2 = 1800^3$   $\chi_{AB}$  is estimated to be 0.70.

Figure 5.4 indicates that the critical AN content for miscibility in blends of SAN copolymers with the PPO homopolymer is 17 wt%. The critical condition for these blends of the type,  $(A_{1-x}B_x)_{n_1}/C_{n_2}$ , holds the relation :

$$\chi_{blend}^{crit} = 1/2(n_1^{-1/2} + n_2^{-1/2})^2 = (1-x)\chi_{AC} + x\chi_{BC} - x(1-x)\chi_{AB} \quad (5.2)$$

For the present system,  $n_1 = 2800$  (from Chapter IV) and  $n_2 = 290$ ,

which yields  $\chi_{blend}^{crit}$  of 0.003. From the Eqn. (5.2)  $\chi_{BC}$  is determined to be 0.80.

By extrapolation, Figure 5.4 also indicates the presence of a "window of miscibility" for blends of SAN copolymers with the fully sulfonylated PPO homopolymer. The window of miscibility is found

over the AN content of 13-52 wt%.  $\chi_{BD}$  is estimated to be 0.14 by a procedure similar to that described above to determine  $\chi_{BC}$  except that blends of the type,  $(A_{1-x}B_x)_{n_1}/D_{n_2}$ , are considered.

It should be noted that the window of miscibility may be observed because of the very large intramolecular repulsive interaction between styrene and acrylonitrile segments comprising the copolymer, even though  $\chi_{AB}$ ,  $\chi_{AD}$ , and  $\chi_{BD}$  are all positive.

Volume of Mixing For immiscible blends the density is equal to or lower than the values calculated from the additivity relationship<sup>4</sup> :

$$\rho = \phi_1 \rho_1 + \phi_2 \rho_2$$

or

$$1/\rho = W_1/\rho_1 + W_2/\rho_2 \quad (5.3)$$

where  $W_i$  and  $\rho_i$  are the weight fraction and the density of the  $i$ th component, respectively. A negative volume change on mixing has been observed for several miscible blends<sup>5-7</sup>.

Figure 5.5 displays the blend composition dependence of the specific volume of SAN 26/SPP0 54 (miscible) blends and SAN 26/SPP0 44 (immiscible) blends. Since the densities have been measured below

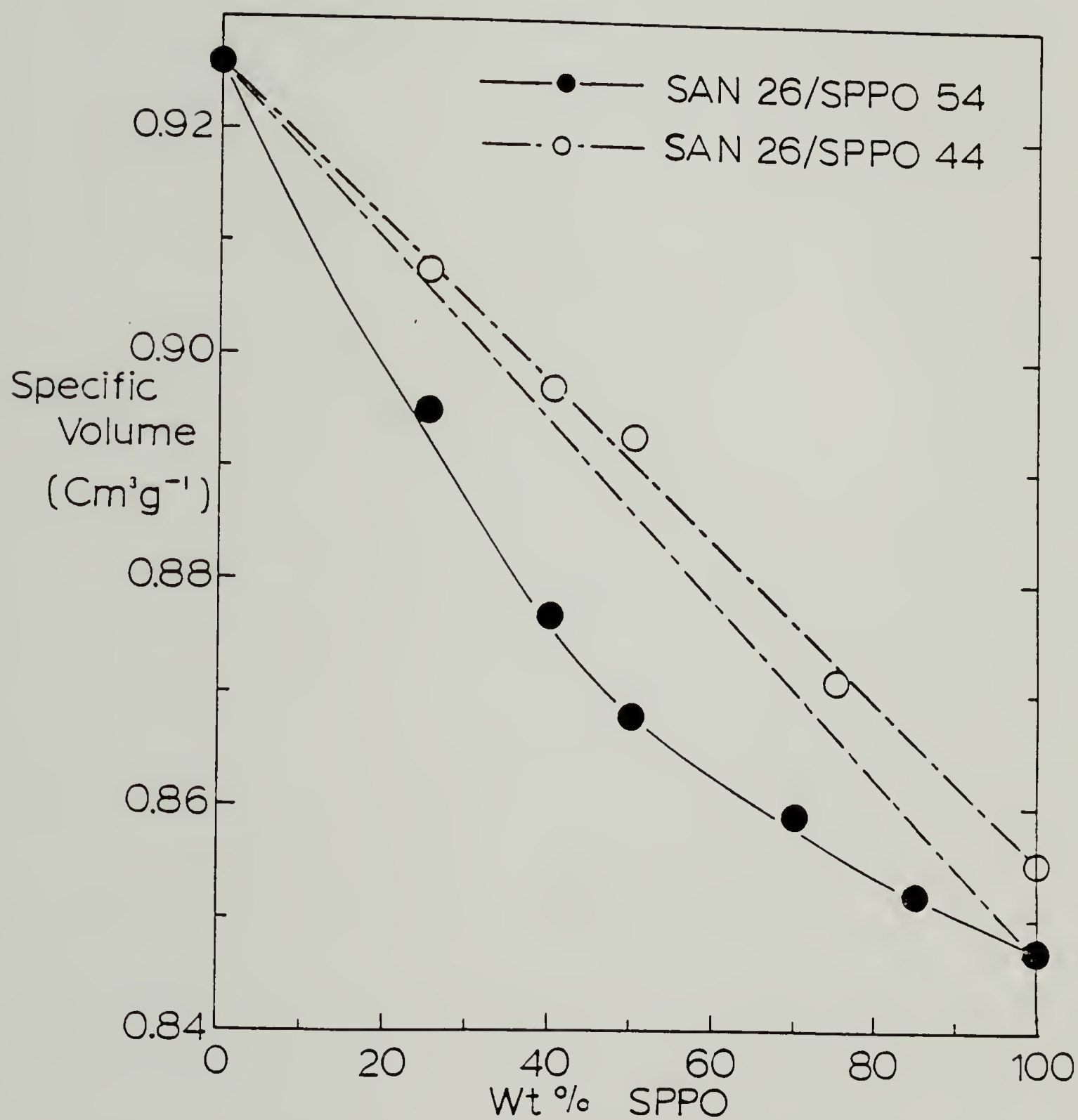


Figure 5.5. Specific volume vs. blend composition expressed as weight fraction SPPO. Dashed lines indicate specific volume calculated from the additivity relationship.

the  $T_g$ 's of each component and the blends, there may be a contribution to the specific volume associated with the excess free volume during solvent casting and drying<sup>7</sup>. The immiscible blends are seen to obey the additivity relationship, while the miscible blends exhibit a negative volume change on mixing of about 2% at 50/50 wt% composition, which infers that the miscible region shown in the "C-C plots" (Figure 5.4) involves better packing on mixing, even though all  $\chi_{ij}$ 's are positive except  $\chi_{AC}$ .

Dynamic Mechanical Measurements      Temperature dependences of  $\tan \delta$  for SAN 18, SPPO 39 and their 50/50 wt% blends, which are found to be miscible based on a single calorimetric glass transition temperature, are shown in Figure 5.6. The 50/50 wt% blend exhibits a single, well-defined mechanical loss peak with no apparent shoulder occurring at a temperature between the transitions of the pure components. However, peak broadening is noticeable because of a fluctuation in local composition within the blend.

Dielectric Measurements      Dielectric relaxation measurements of blends involving polymers with permanent dipole moments are suitable for probing the molecular environment, or more specifically, intramolecular and intermolecular interactions. And the wide range of frequency and time available allows us to conduct the representation on the basis of time-temperature superposition.

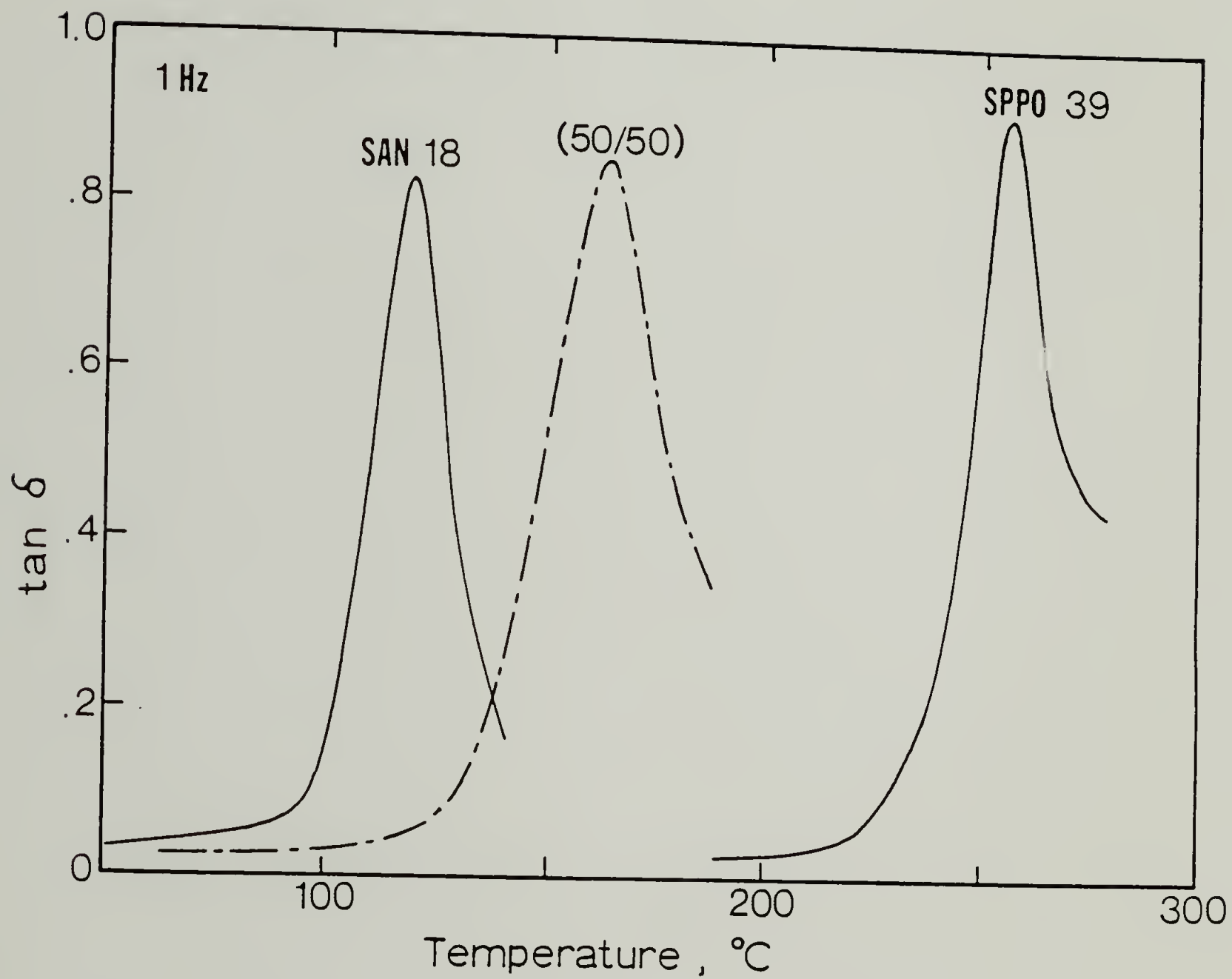


Figure 5.6. Dynamic mechanical  $\tan \delta$  as a function of temperature for SAN 18, SPP0 39 and 50/50 wt% SAN 18/SPP0 39 blends at 1 Hz

Temperature Plane Measurements The loss curves of SAN 5, SPP0 12 and their blends are plotted as a function of temperature in Figure 5.7. The 50/50 wt% blend exhibits a single, broadened dielectric  $\alpha$ -relaxation with no evidence of shoulders between the transitions of the pure components. An ionic conduction<sup>8</sup> can be seen from the sharp upturn in  $\tan \delta$  above the loss peak temperatures, particularly at lower frequencies. However, since the ionic conduction of pure SAN 5 appears to be almost negligible, it is assumed that impurities in SAN 5 cause little change in the high temperature loss peak of the 50/50 wt% blend even above the  $T_g$  of SAN 5. The charge carriers in the blend seem to originate mainly from SPP0 12. In the SPP0 copolymer a trace of residual catalyst, even after a careful purification of the copolymer, is regarded as the primary source of the ionic conduction.

Frequency Plane Measurements Temperature plane dynamic mechanical or dielectric relaxation measurements cannot provide information on phase equilibrium at a certain temperature because of the possible "freezing in" of a nonequilibrium structure and of their insensitivity to detect the very small dispersed phase<sup>9</sup>, if any. Thus, to investigate the nature of the molecular interactions, conformational states in the system and the extent of miscibility within the miscible blend, frequency plane measurements of blends of SAN 5/SPP0 12 were carried out isothermally. The blend compositions were limited to those with higher SAN 5 content since SPP0 12 exhibits significant ionic transport losses.

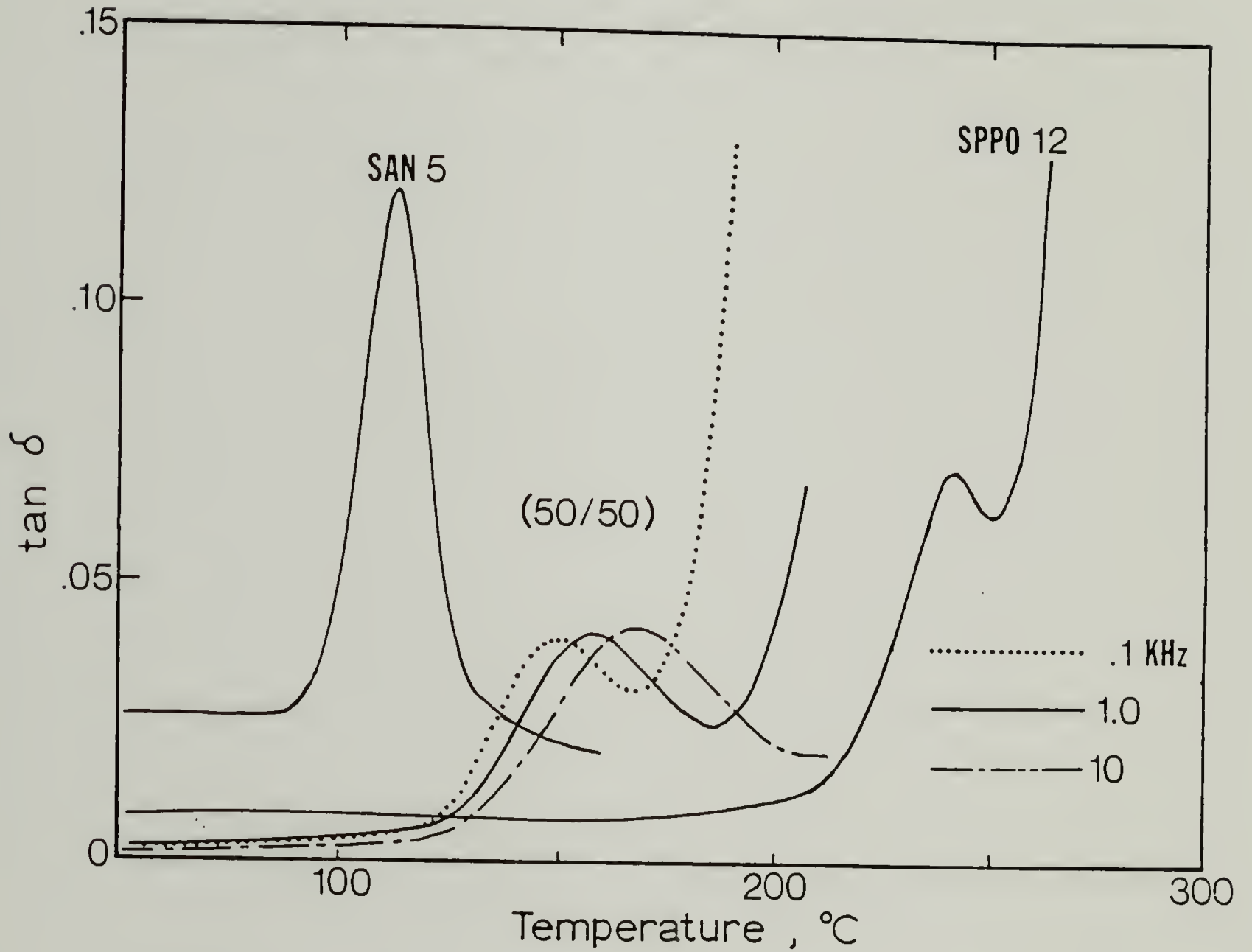


Figure 5.7. Dielectric  $\tan \delta$  as a function of temperature for SAN 5, SPP0 12 and 50/50 wt% SAN 5/SPP0 12 blends

Dielectric constants ( $\epsilon'$ ) and losses ( $\epsilon''$ ) for SAN 5 and its blends with SPPO 12 of varying compositions are displayed in the frequency plane in Figures 5.8 (a)-(h). Figures 5.9 (a)-(b) are the corresponding Argand diagrams. Good superposition over a range of temperatures can be seen.

Figure 5.10 shows the normalized dielectric loss curves, which indicates that the temperature-frequency superposition is applicable and that the shape parameters change negligibly over the temperature ranges studied. Table 5.1 summarizes the loss half widths, three-quarter widths,  $\Delta H/\Delta L$ , representing the ratio of the distance of the high frequency branch at half-height from  $\log(f/f_m) = 0$  to that of the low frequency branch at half-height from  $\log(f/f_m) = 0$  (thus, indicating the asymmetry of the dispersion curve), and the Cole-Cole parameter,  $\alpha$ , whose magnitude is inversely related to the departure from a single relaxation time.

As seen both from Figure 5.10 and Table 5.1, the blends exhibit a significant broadening in the dielectric loss spectra with increasing SPPO content compared with pure SAN 5 copolymer, reflecting the differences in local environments as a consequence of the cooperative nature of the relaxation as suggested by Glarum<sup>10</sup>. This broadening of relaxation spectra is ascribed to local concentration fluctuations which persist for longer times than those required for dipolar polarization. In other words, this would imply

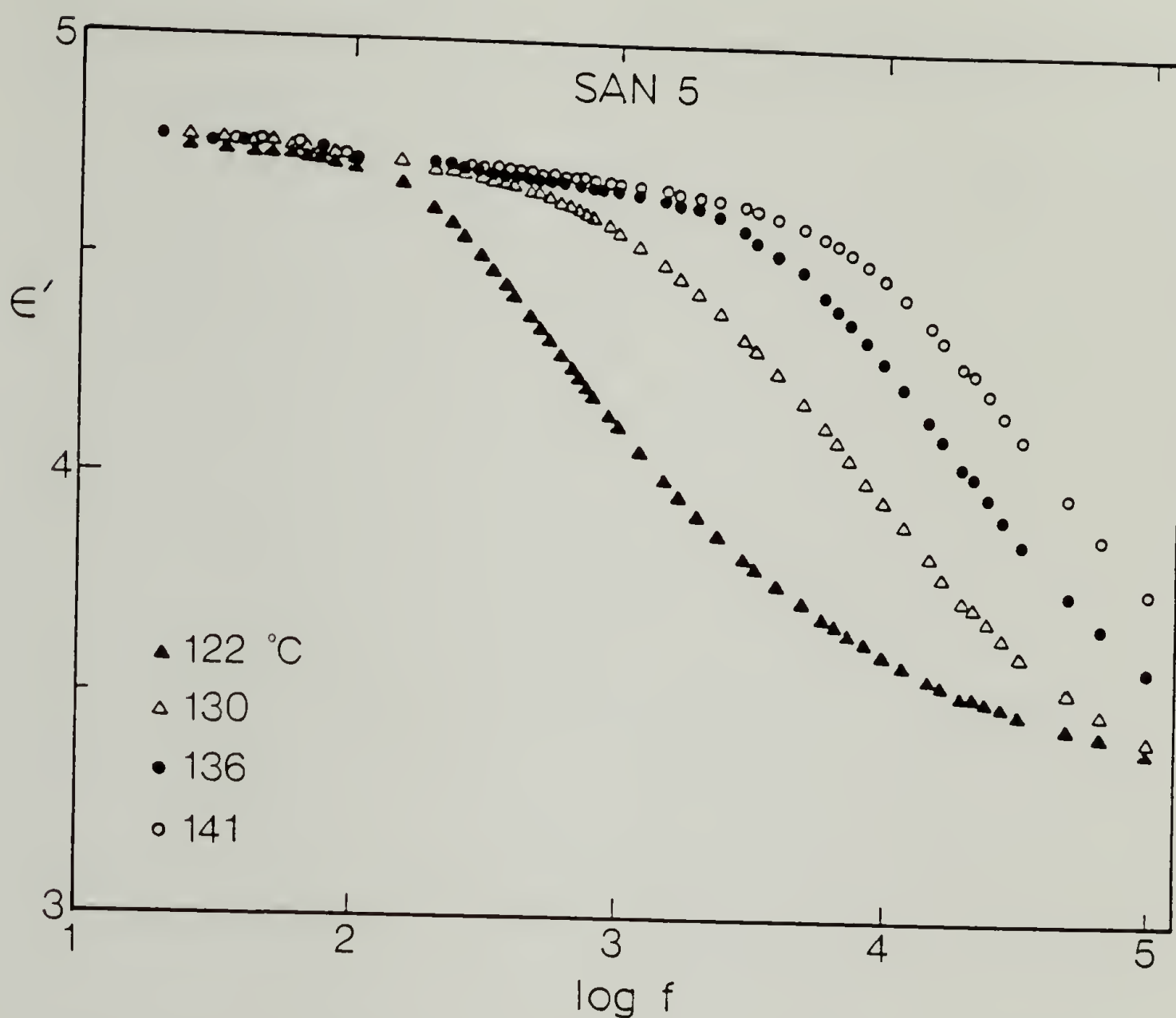


Figure 5.8. (a) Dielectric constant vs. frequency for SAN 5  
 (b) loss factor for SAN 5; (c) Dielectric constant vs.  
 frequency for 90/10 wt% SAN 5/SPPO 12 blends; (d) Loss  
 factor for 90/10 wt% SAN 5/SPPO 12 blends; (e) Dielectric  
 constant vs. frequency for 80/20 wt% SAN 5/SPPO 12  
 blends; (f) Loss factor for 80/20 wt% SAN 5/SPPO 12  
 blends; (g) Dielectric constant vs. frequency for  
 65/35 wt% SAN 5/SPPO 12 blends; (h) Loss factor for  
 65/35 wt% SAN 5/SPPO 12 blends.

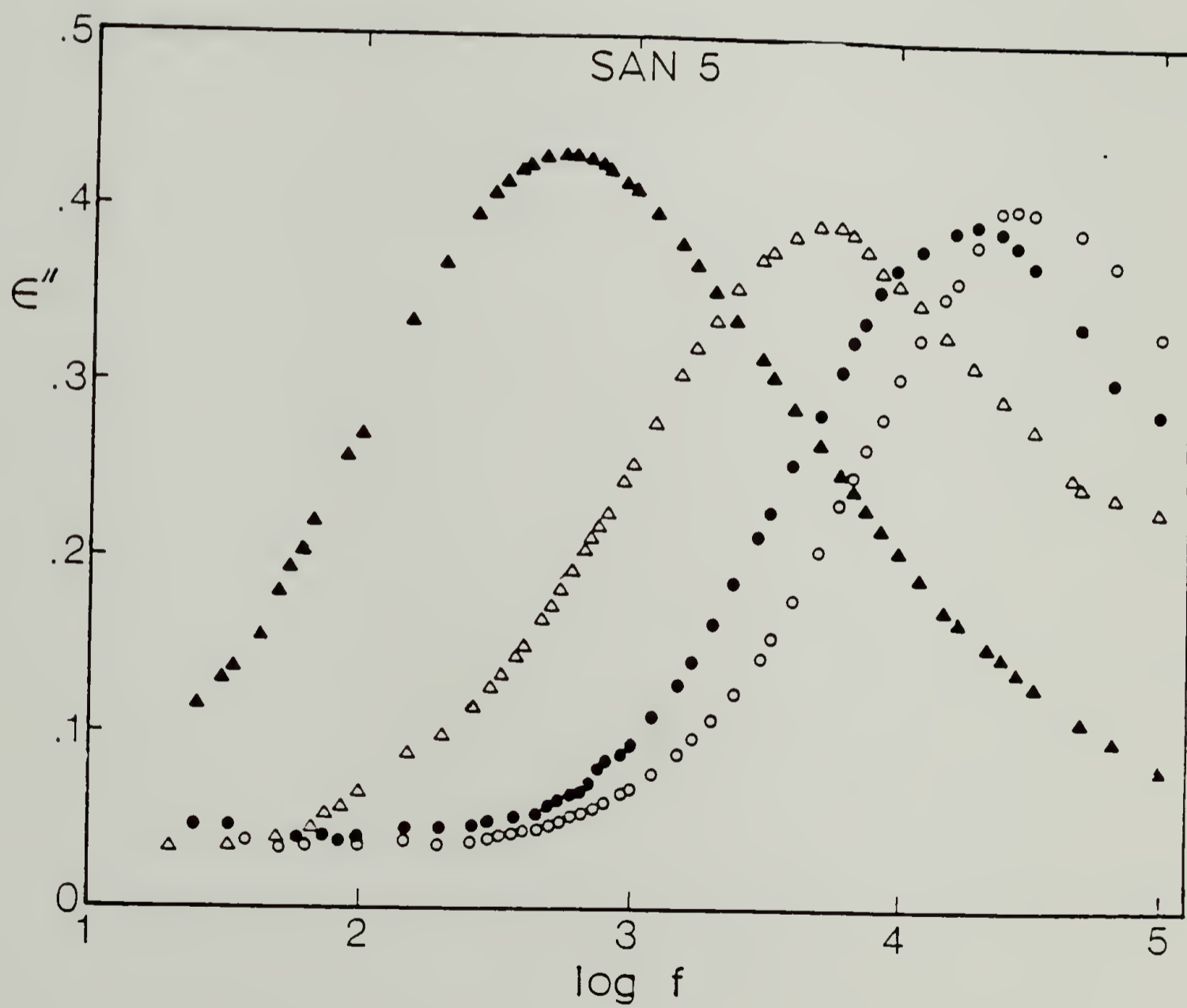


Figure 5.8. (b)

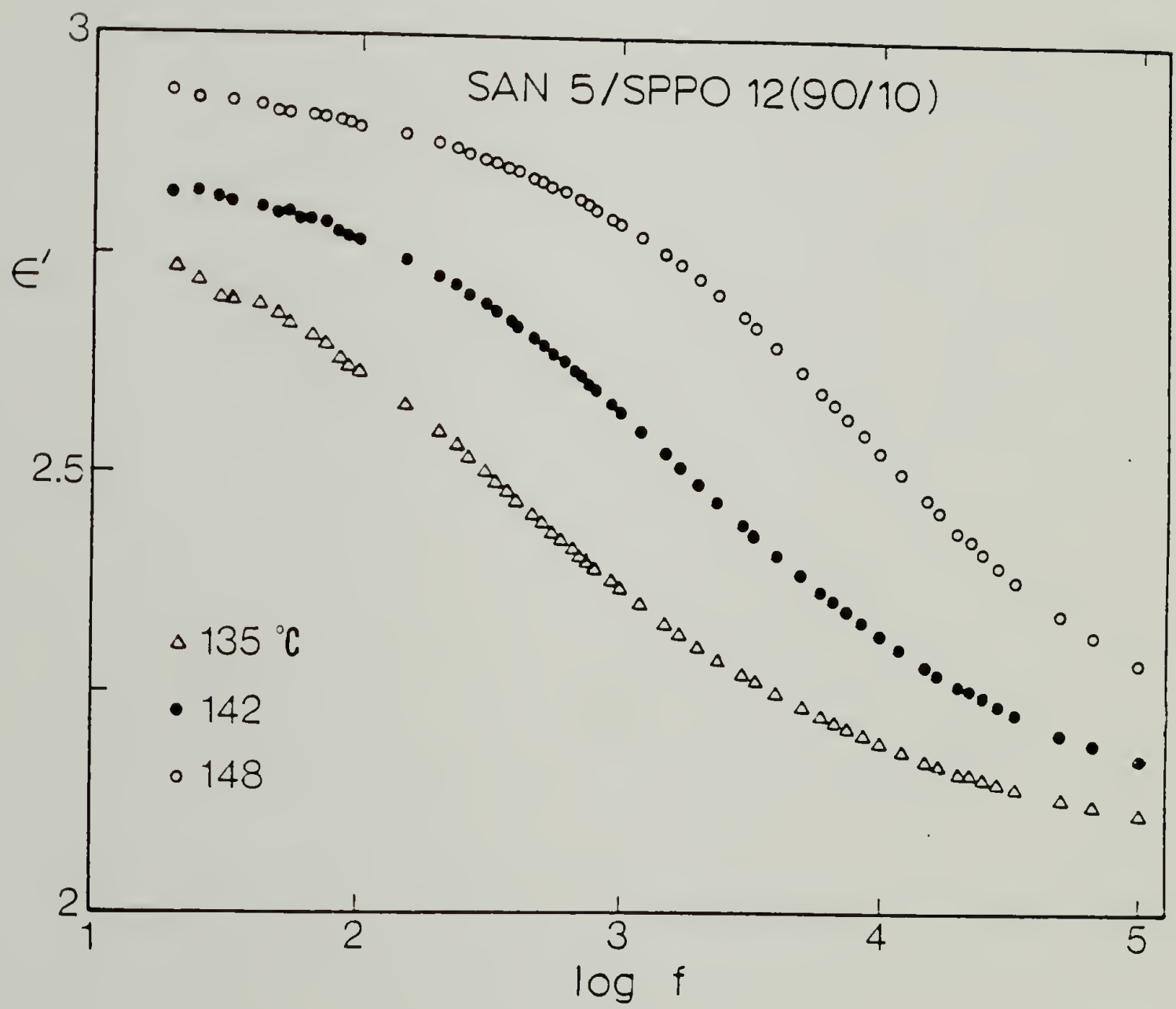


Figure 5.8. (c)

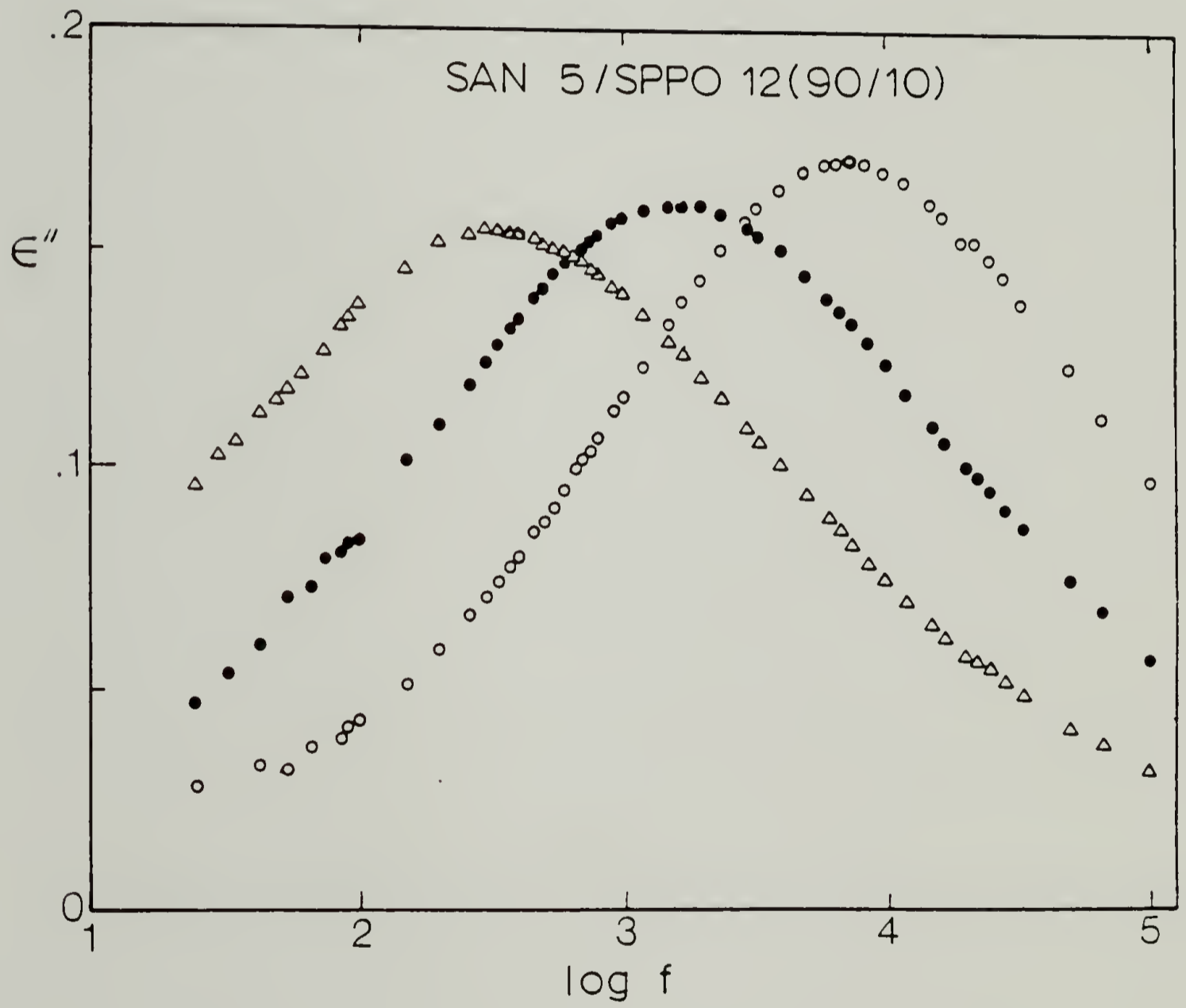


Figure 5.8. (d)

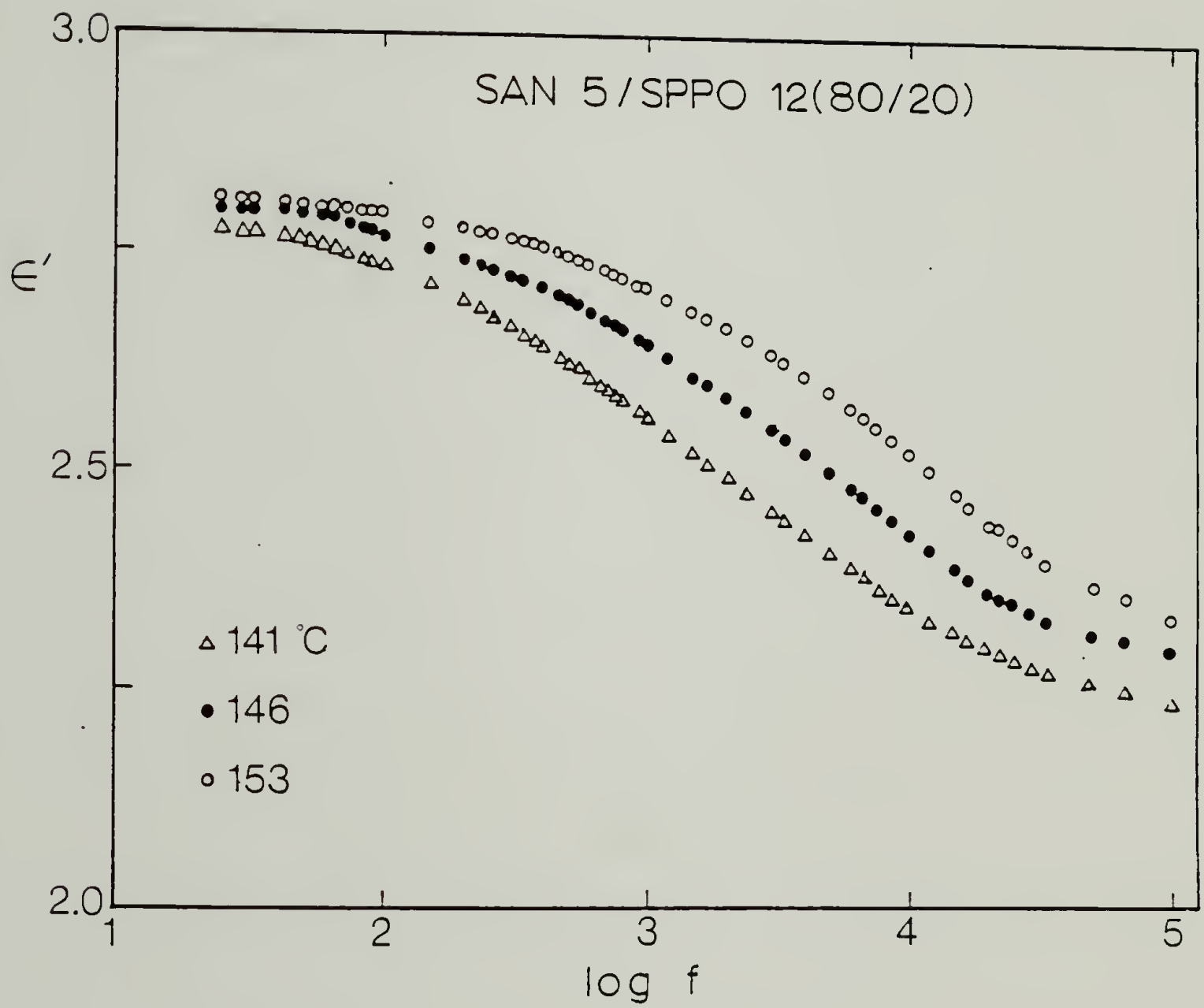


Figure 5.8. (e)

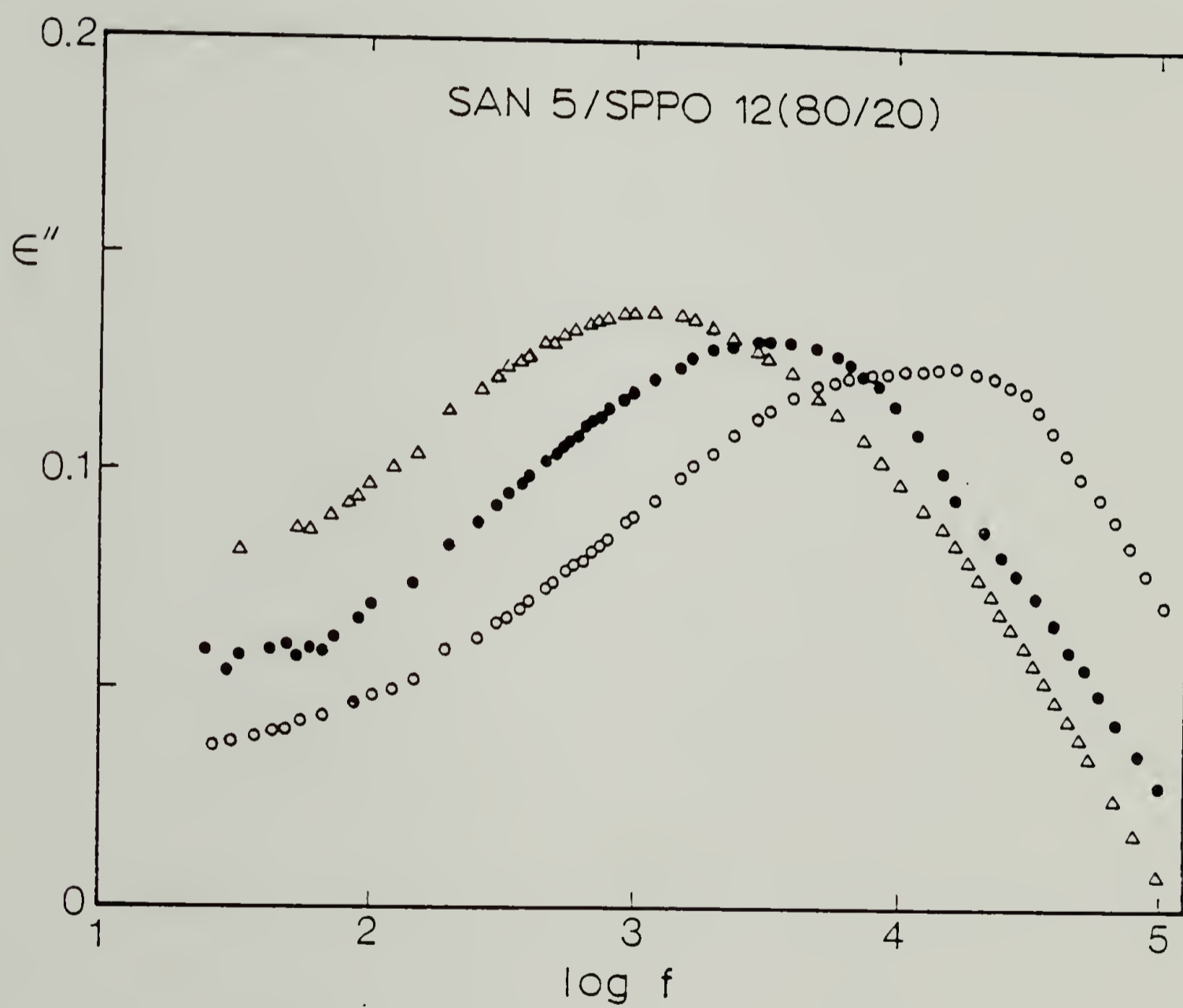


Figure 5.8. (f)

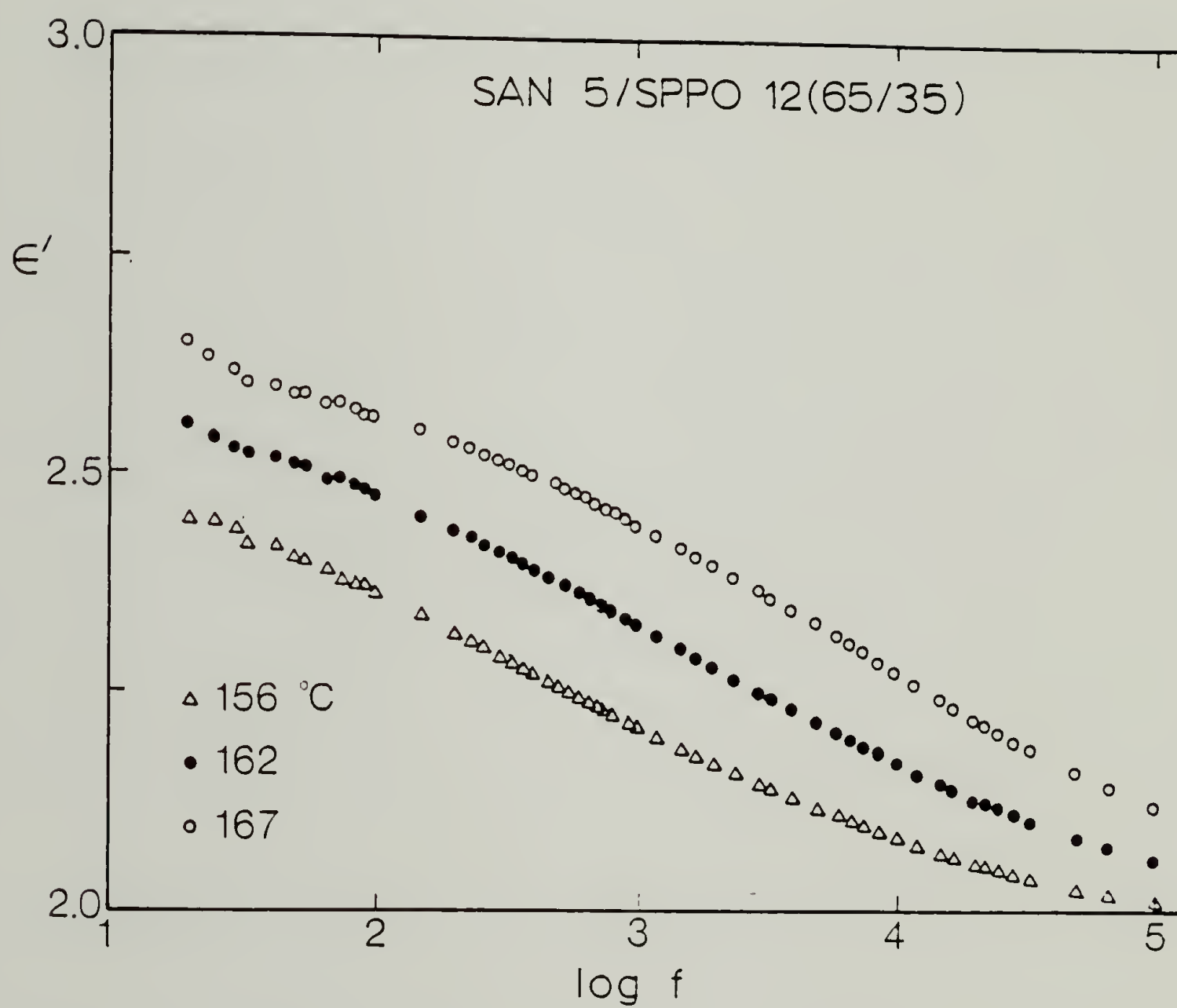


Figure 5.8. (g)

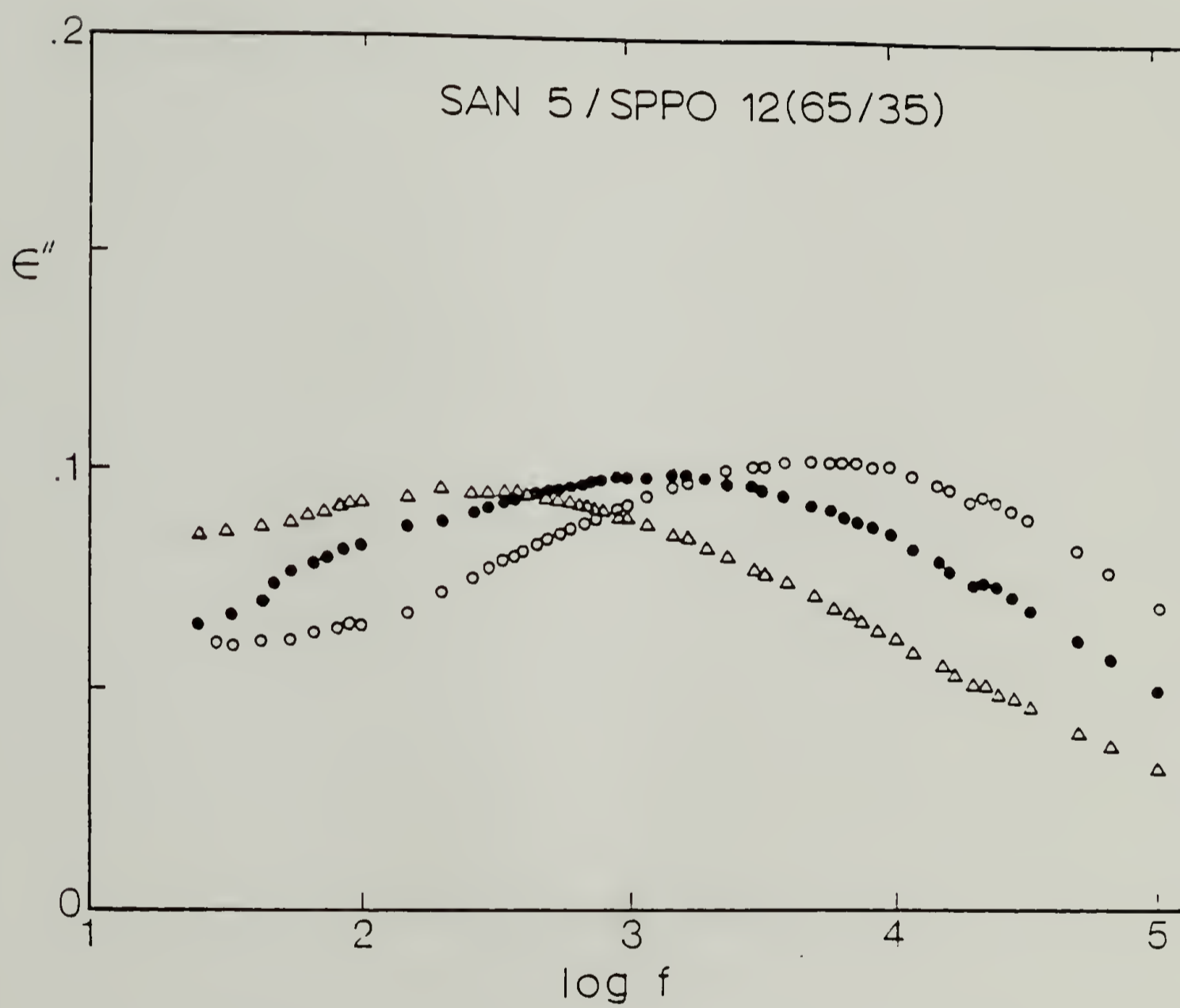


Figure 5.8. (h)

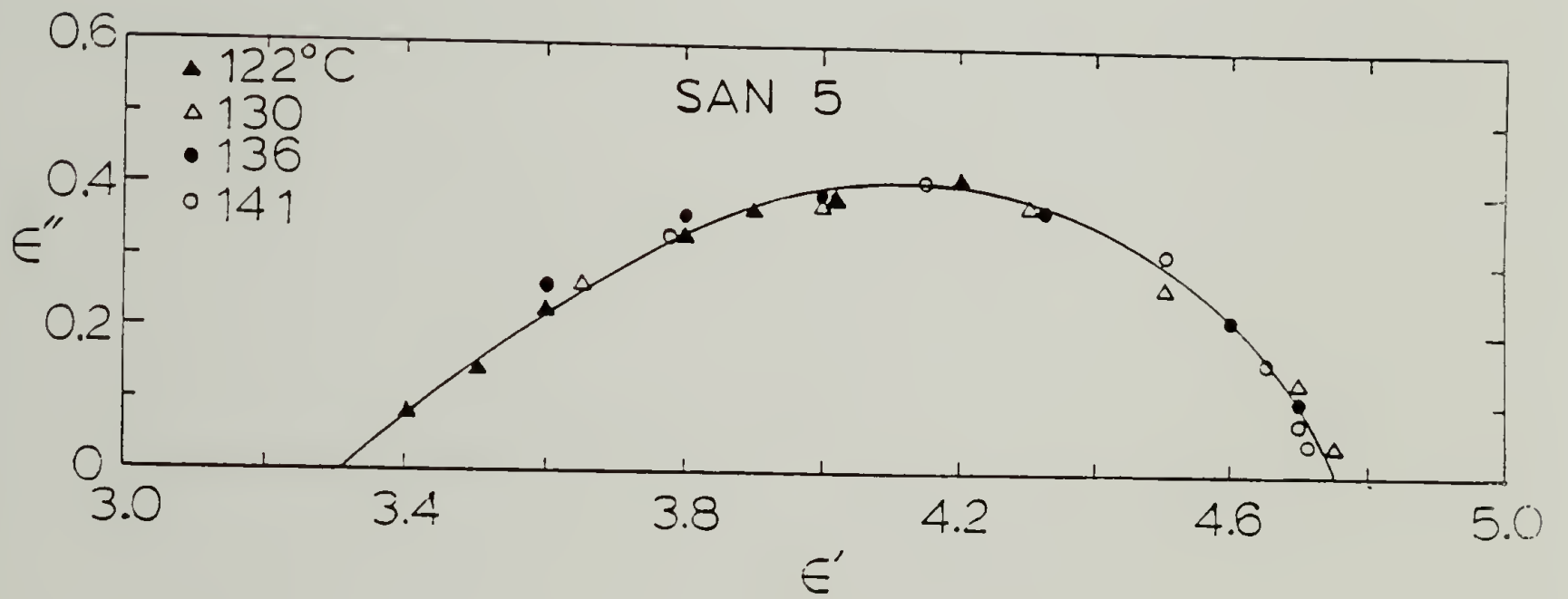


Figure 5.9. (a) Argand diagram for SAN 5; (b) Argand diagrams for the blends of SAN 5/SPP0 12 of varying compositions.

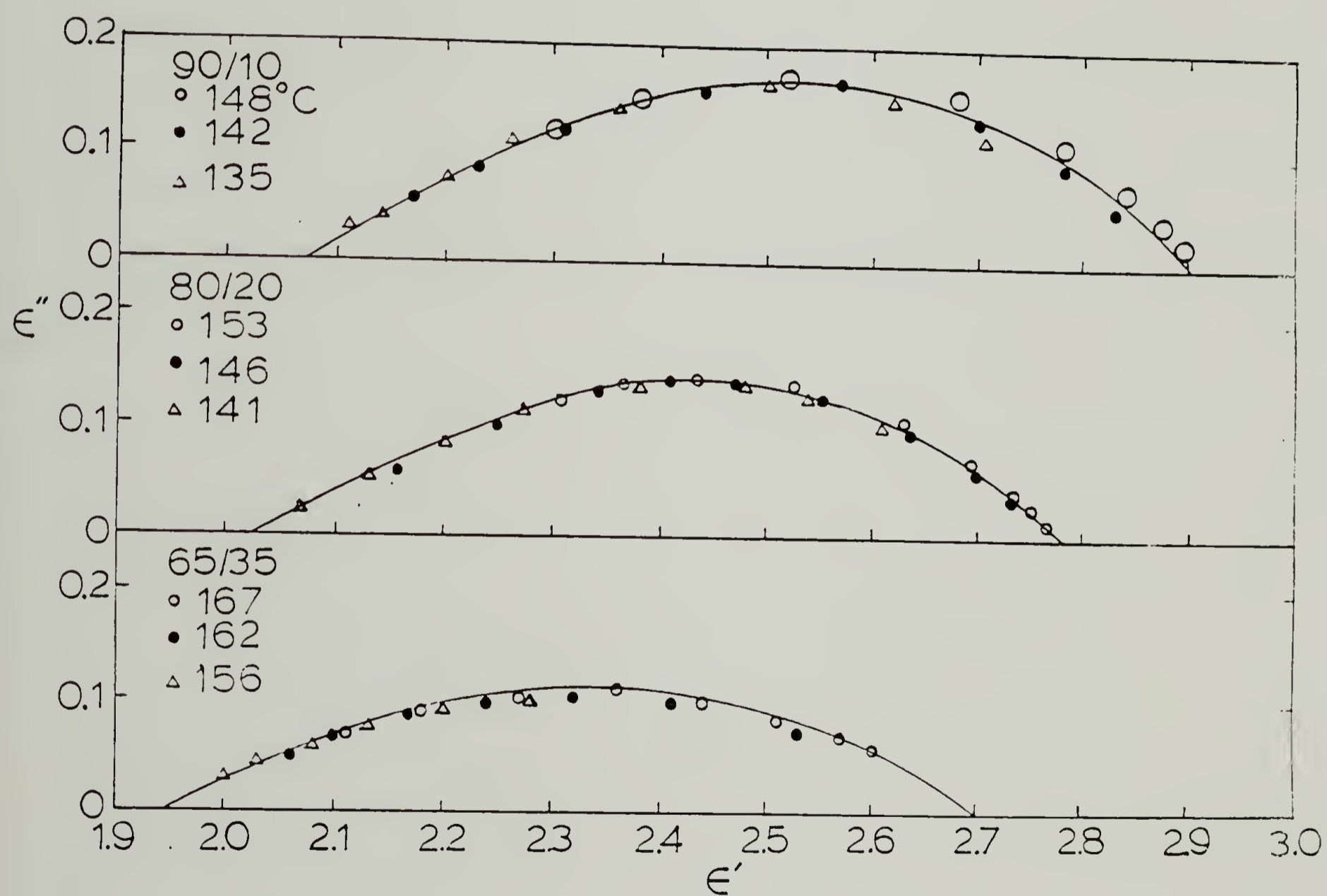


Figure 5.9. (b)

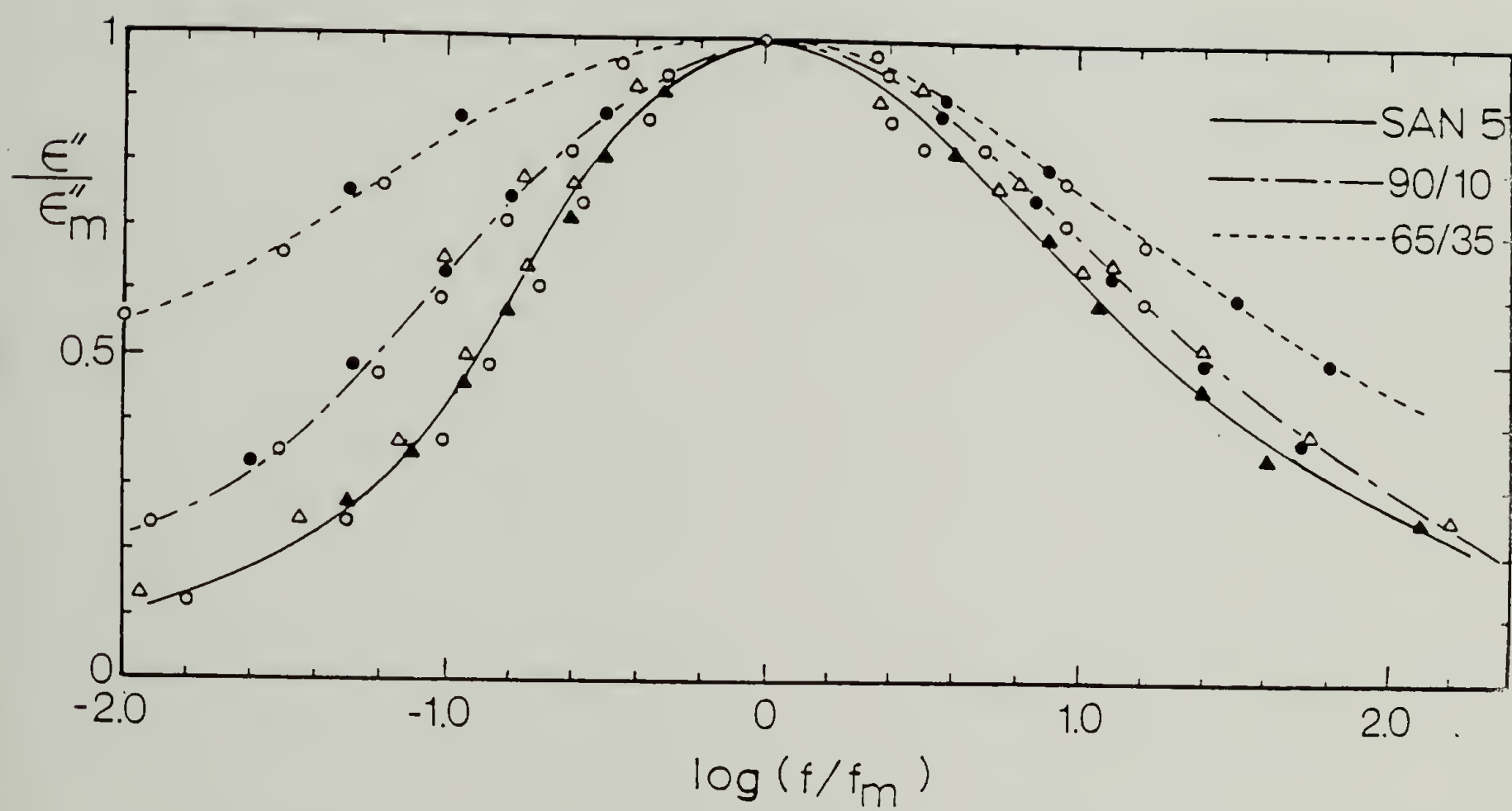


Figure 5.10. Normalized dielectric loss factor curves for SAN 5  
and its blends

Table 5.1

Dielectric Parameters for SAN 5 and Its Blends with SPPO 12

Sample	$\Delta H/\Delta L$	$\alpha$	0.5 Width (Decades Frequency)	0.75 Width
SAN 5	1.42	0.41	2.18	1.36
SAN 5/SPPO 12 (90/10)	1.18	0.33	2.62	1.64
SAN 5/SPPO 12 (65/35)	-	0.28	-	2.32

the presence of equilibrium conformational correlation lengths greater than or at least comparable to the dimension of the cooperative relaxing regions.

The Kirkwood-Frohlich correlation parameters <sup>11</sup>(g factors) can provide information on dipole-dipole interactions. Although calculation of g factors for these blends has not been attempted because the g factor for pure SPP0 12 copolymer is under question at present (more specifically, the dipole moment of the gas phase or its model compound of sulfonylated phenylene oxide unit is uncertain), dipole cancellation in the blend due either to the hindered rotation of a molecule relative to its neighbors or to the orientation correlations of the dipoles between polymer chains may be inferred qualitatively from the decreased dielectric strength  $\epsilon_r - \epsilon_u$ , as seen in Figures 5.9 (a)-(b), where  $\epsilon_r$  and  $\epsilon_u$  refer to the relaxed and unrelaxed dielectric constants corresponding to the low and high frequency limits, respectively. It should be noted that in FTIR spectra, no change in peak position at  $2236.74 \text{ cm}^{-1}$  corresponding to the absorption frequency of the nitrile group could be seen in SAN 5 and in the 50/50 wt% blend signifying that this dipolar correlation is of a different nature from the intermolecular interaction. Figure 5.11 and 5.12 display the Fourier transform infrared spectra of SAN 5 and its blends with SPP0 12, respectively. Plots of  $\log f_{\text{max}}$  (for the peak in  $\epsilon''$ ) vs. the reciprocal temperature are displayed for SAN

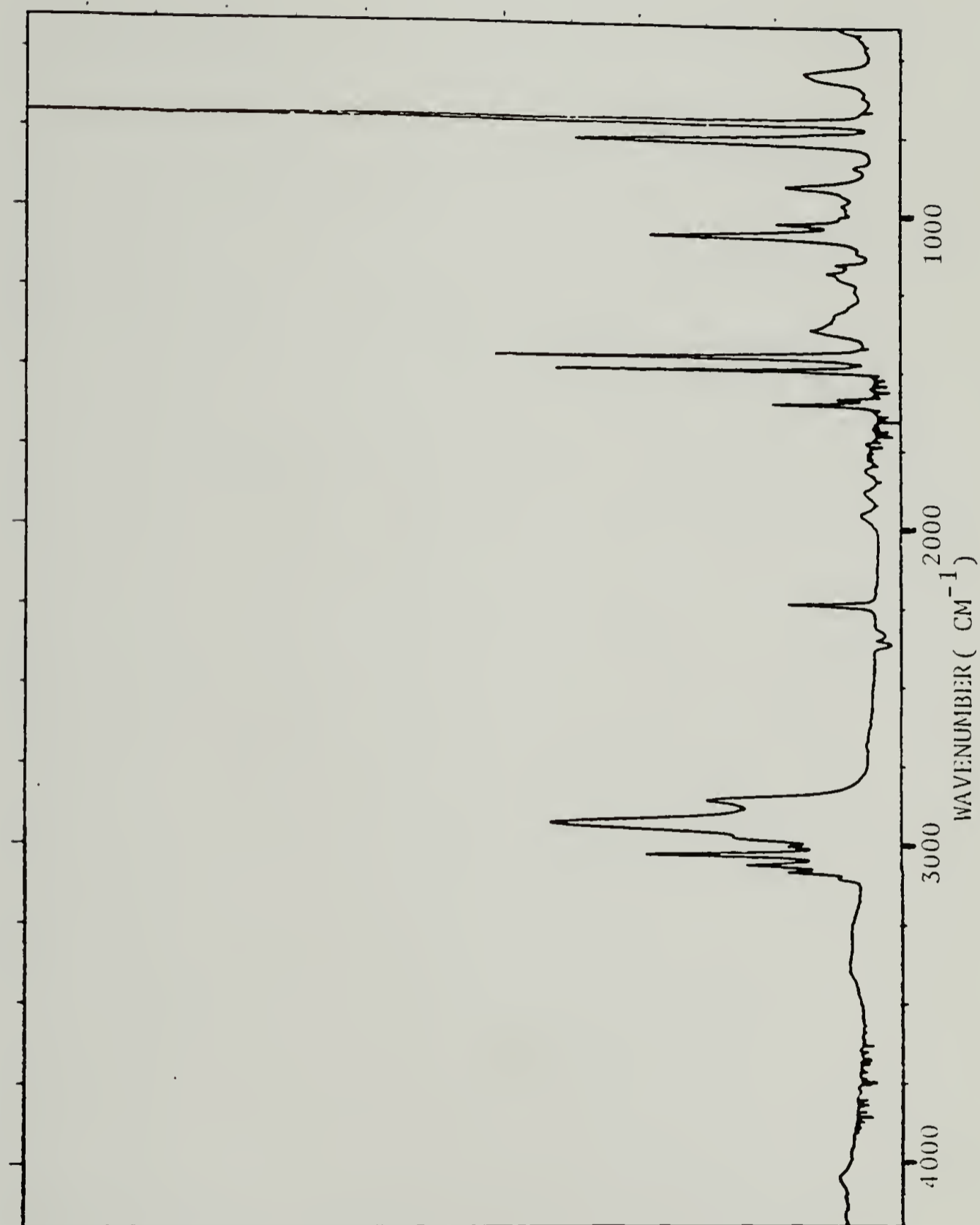


Figure 5.11. Fourier transform infrared spectrum of SAN 5

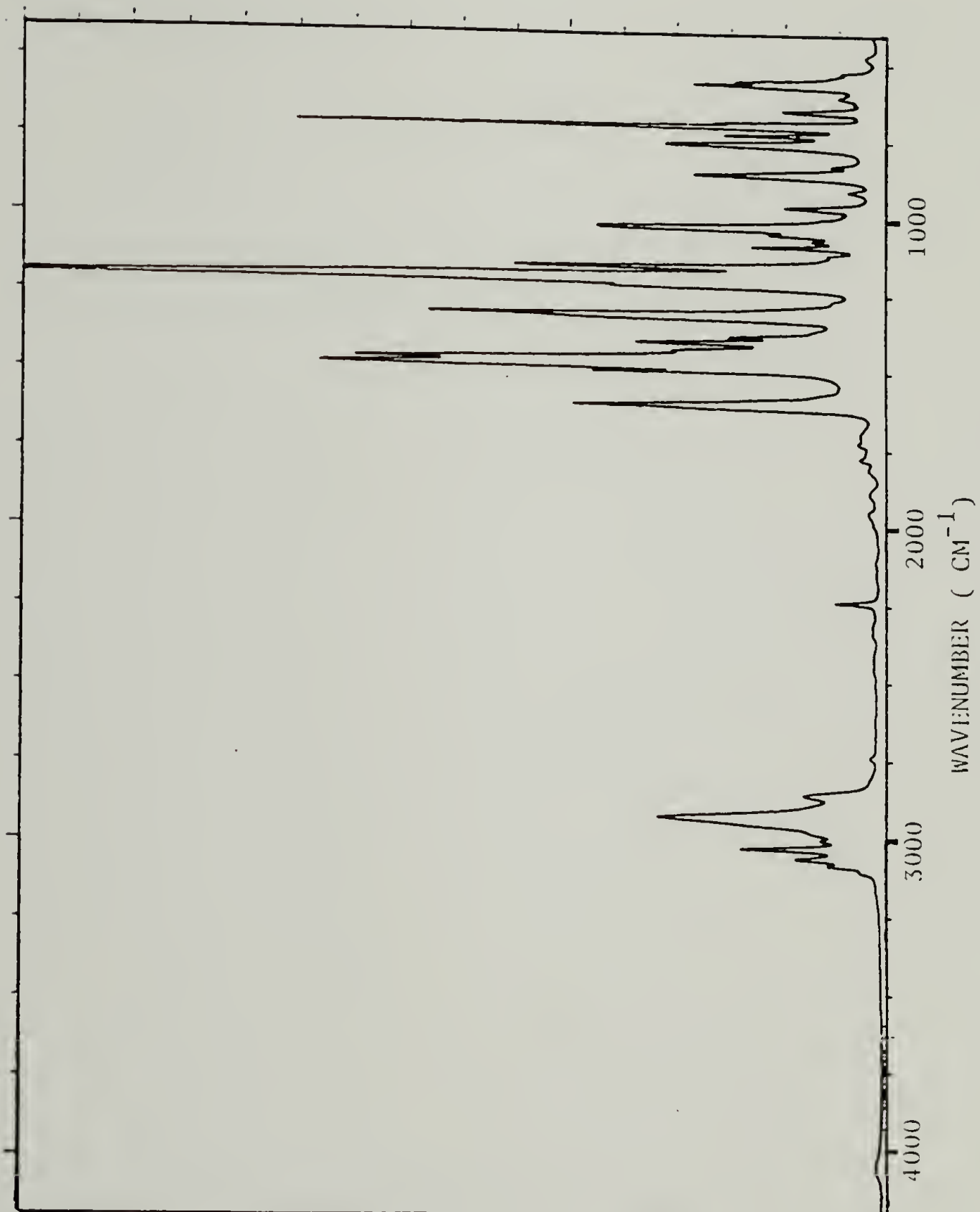


Figure 5.12. Fourier transform infrared spectrum of 50/50 wt% blend of SAN 5/SPPO 12

5 and its blends in Figure 5.13. The data can be represented by straight lines in this region giving higher activation energies with increasing SPP0 12.

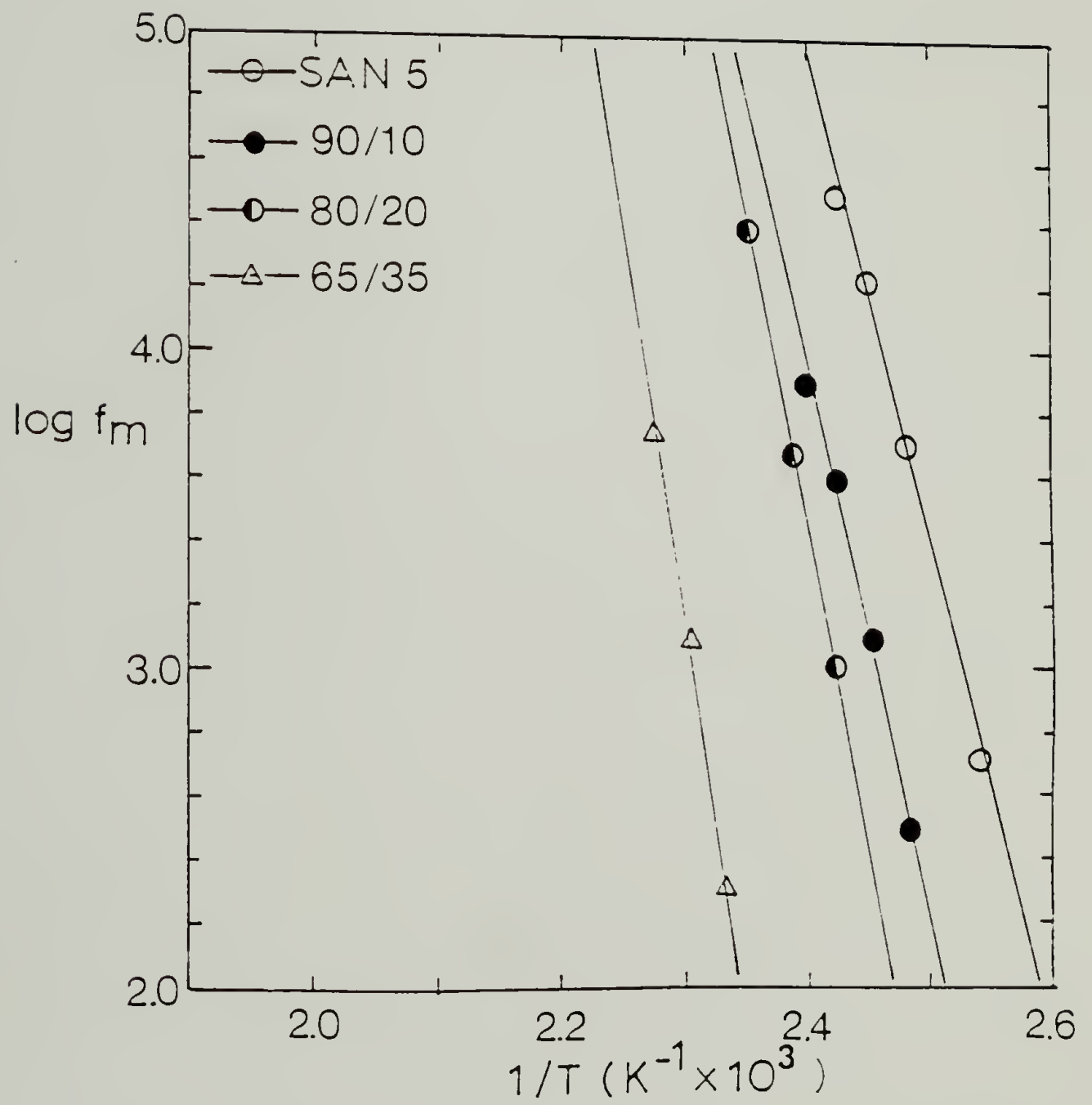


Figure 5.13. Arrhenius plots for SAN 5 and its blends

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## CHAPTER VI

### MISCIBILITY IN BLENDS OF POLY(STYRENE-CO-P(O)-FLUOROSTYRENE) AND POLY(STYRENE-CO-METHYL ACRYLATE) WITH SPPO COPOLYMERS

This chapter describes the studies of miscibility and phase behavior in blends of poly(styrene-co-p(o)-fluorostyrene) and poly(styrene-co-methyl acrylate) with sulfonylated poly(2,6-dimethyl-1,4-phenylene oxide) (SPPO) copolymers, i.e., the blends of the type,  $(A_{1-x}B_x)_{n_1} / (C_{1-y}D_y)_{n_2}$ . The isothermal composition-composition diagram displaying the miscibility-immiscibility boundary in Cartesian coordinates is interpreted on the basis of a mean field theory, as discussed in Chapter I, through which all  $\chi_{ij}$ 's are determined. The role of intramolecular interactions in inducing miscibility in copolymer blends without attractive interactions is reemphasized from the discovery of new systems which are miscible because of purely "repulsive interaction".

#### A. Experimental Section

Materials The preparation and properties of SPPO copolymers were described in Chapter II. Poly(p-fluorostyrene), poly(o-fluorostyrene) and a series of poly(styrene-co-p(o)-fluorostyrene) copolymers with differing compositions were synthesized by Vukovic<sup>1,2</sup> via a free radical polymerization technique. The polymer molecular weights and compositions, cited from this work, are listed in Table 6.1.

A series of poly(styrene-co-methyl acrylate) copolymers was prepared by free radical polymerization in toluene at 60°C, using azobisisobutyronitrile (AIBN) (0.3% based on total monomer weight) as the initiating species. Styrene and methyl acrylate monomers were purified by washing with 10% aqueous solution of sodium hydroxide and then distilled under vacuum. The initiator was purified by recrystallization from methanol. Spectral grade toluene was used without further purification.

The polymerization was stopped at a conversion of ~40% to prevent copolymer composition drift. To terminate polymerization the reaction mixtures were precipitated into a large excess of methanol. The samples were then dried under vacuum at 80°C to constant weight.

Molecular weights were obtained by GPC as described in Chapter II. The polymer compositions were determined by oxygen elemental analysis.  $T_g$  determinations were also performed as

Table 6.1

Molecular Weights of Poly(styrene-co-p(o)-fluorostyrene)

Polymer	$\bar{M}_n(\times 10^{-5})$	$\bar{M}_w(\times 10^{-5})$	$\bar{M}_w/\bar{M}_n$
PoFS	0.44	0.84	1.9
P(S-oFS, 18 <sup>*</sup> )	0.53	0.95	1.8
P(S-oFS, 40)	0.65	1.24	1.9
P(S-oFS, 68)	0.68	1.35	2.0
P(S-oFS, 77)	0.71	1.39	2.0
PpFS	0.67	1.27	1.9
P(S-pFS, 8)	0.54	0.97	1.8
P(S-pFS, 16)	0.56	0.99	2.0
P(S-pFS, 25)	0.51	0.97	1.9
P(S-pFS, 46)	0.52	1.00	1.9
P(S-pFS, 55)	0.51	1.04	1.95
P(S-pFS, 67)	0.53	1.04	2.0
P(S-pFS, 77)	0.50	1.00	2.0

\* Numerals represent mole percent of fluorostyrene.

described in Chapter II. Table 6.2 summarizes the relevant data for the copolymers used in this work.

Preparation of blend samples and measurements of glass transition temperatures were carried out as described in Chapter II, except that, in case of the blend of the PPO homopolymer with poly(o-fluorostyrene), blends were prepared by casting films from 2 wt% chloroform solutions. All blend samples were annealed at 290°C in the DSC pan, unless otherwise noted. The critical composition differences in blends of poly(styrene-co-methyl acrylate) which differ only in composition were determined using an optical microscope attached with hot stage (Mettler FP2) and DSC.

## B. Results and Discussion

### i). Blends of Poly(styrene-co-p-fluorostyrene) with SPPPO Copolymers

These systems are of the type  $(A_{1-x}B_x)_{n_1} / (C_{1-y}D_y)_{n_2}$  in which A, B, C and D represent styrene, p-fluorostyrene, unsulfonylated phenylene oxide and sulfonylated phenylene oxide units, respectively. Figure 6.1 shows DSC thermograms of blends of poly(styrene-co-p-fluorostyrene, 77) with SPPPO 34. A single composition dependent  $T_g$  is observed.  $T_g$ 's of these blends are plotted as a function of blend

Table 6.2

Compositions and Molecular Weights of  
Poly(styrene-co-methyl acrylate) Samples

Sample	Monomer feed	Copolymer Composition		$\bar{M}_n$	$\bar{M}_w$	$T_g$
	Methyl Acryl.	Methyl Acrylate				
	Mole %	Mole %	Wt%	(x 10 <sup>-4</sup> )		°C
SMA 15	16.3	17.0	14.5	3.77	7.03	91
SMA 19	25.7	22.2	19.1	3.74	7.30	85
SMA 25	34.7	29.0	25.3	3.95	6.52	80
SMA 31	43.5	34.8	30.7	3.97	7.10	75
SMA 34	50.0	38.2	33.9	4.26	6.90	70

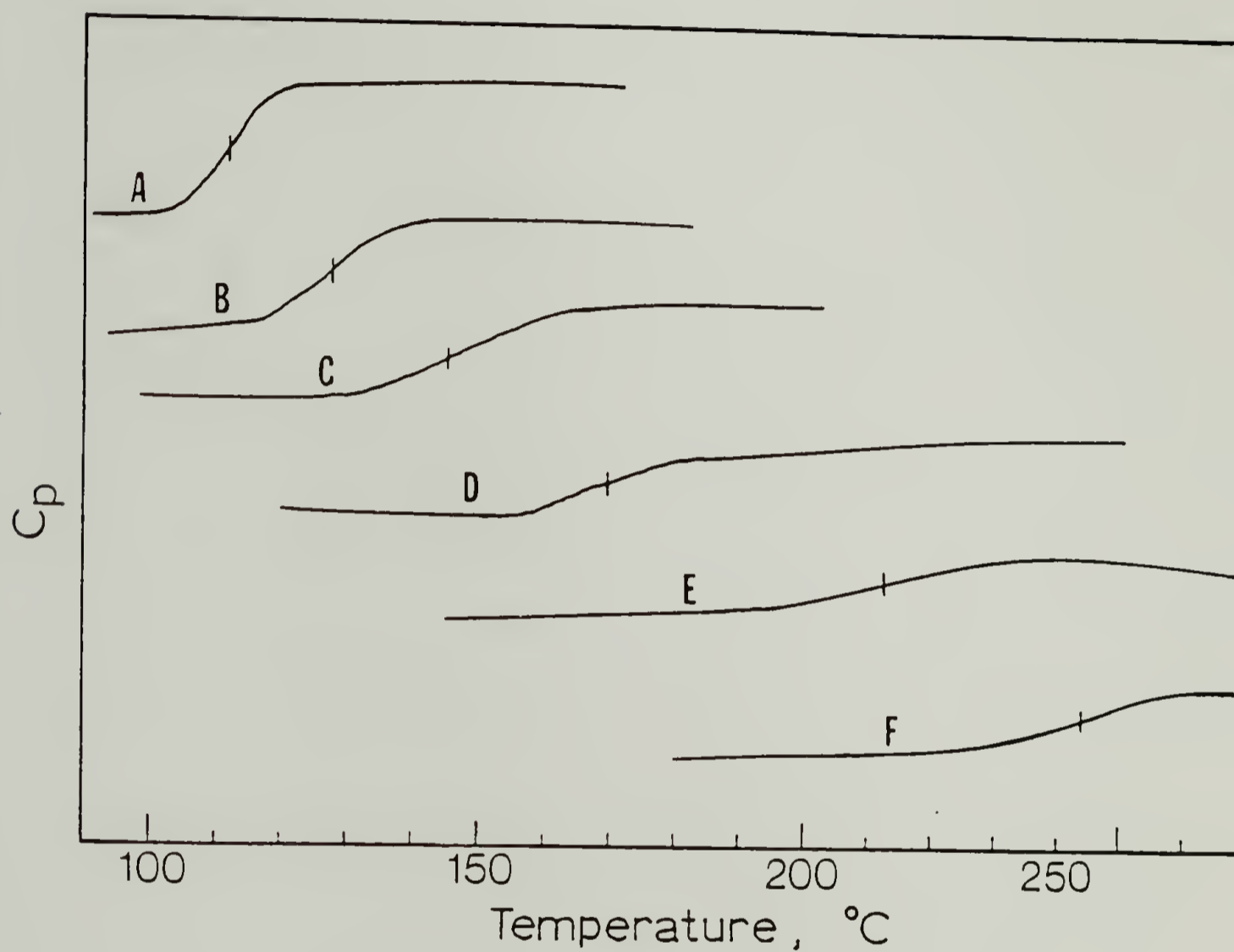


Figure 6.1. DSC thermograms of P(S-pFS, 77), SPP0 34 and blends :

- (A) pure P(S-pFS, 77); (B) 25 wt% SPP0 34;
- (C) 50 wt% SPP0 34; (D) 70 wt% SPP0 34;
- (E) 85 wt% SPP0 34; (F) pure SPP0 34.

composition in Figure 6.2 and fit the predicted values from the Couchman equation<sup>3</sup> reasonably well. The relevant parameters are  $\Delta C_p[p(S-pFS, 77)] = 0.26 \text{ J g}^{-1} \text{ deg}^{-1}$ ,  $T_g = 112^\circ\text{C}$ . The parameters for SPPO<sup>34</sup> were taken from Table 2.2.

Figure 6.3 shows the dependence of  $T_g$  on the degree of sulfonylation in 50/50 wt% blends of SPPO with varying degree of sulfonylation with poly(styrene-co-p-fluorostyrene, 77). As seen in Figure 6.3, poly(styrene-co-p-fluorostyrene, 77) copolymers are miscible with SPPO copolymers containing from 20 to 64 wt% sulfonylated units. In all cases the two  $T_g$  values observed do not correspond to those of the pure components indicating a separation into mixed phases.

Figure 6.4 shows the experimental isothermal composition-composition diagram displaying the miscibility-immiscibility boundary. In this diagram, the far right abscissa represents the blend of the poly(p-fluorostyrene) homopolymer with SPPO copolymers, a blend of the type  $B_{n_1} / (C_{1-y} D_y)_{n_2}$ . Setting  $x_{BC} = 0.055$  and  $x_{CD} = 0.15$  and by employing an analogous procedure as for the blend system of polystyrene with SPPO copolymers, as discussed in chapter III,  $x_{BD}$  was determined to be 0.02. In this system, even though all three  $x_{ij}$ 's are positive, since  $x_{CD} \gg x_{BC}$  and/or  $x_{BD}$ , the blends may have a

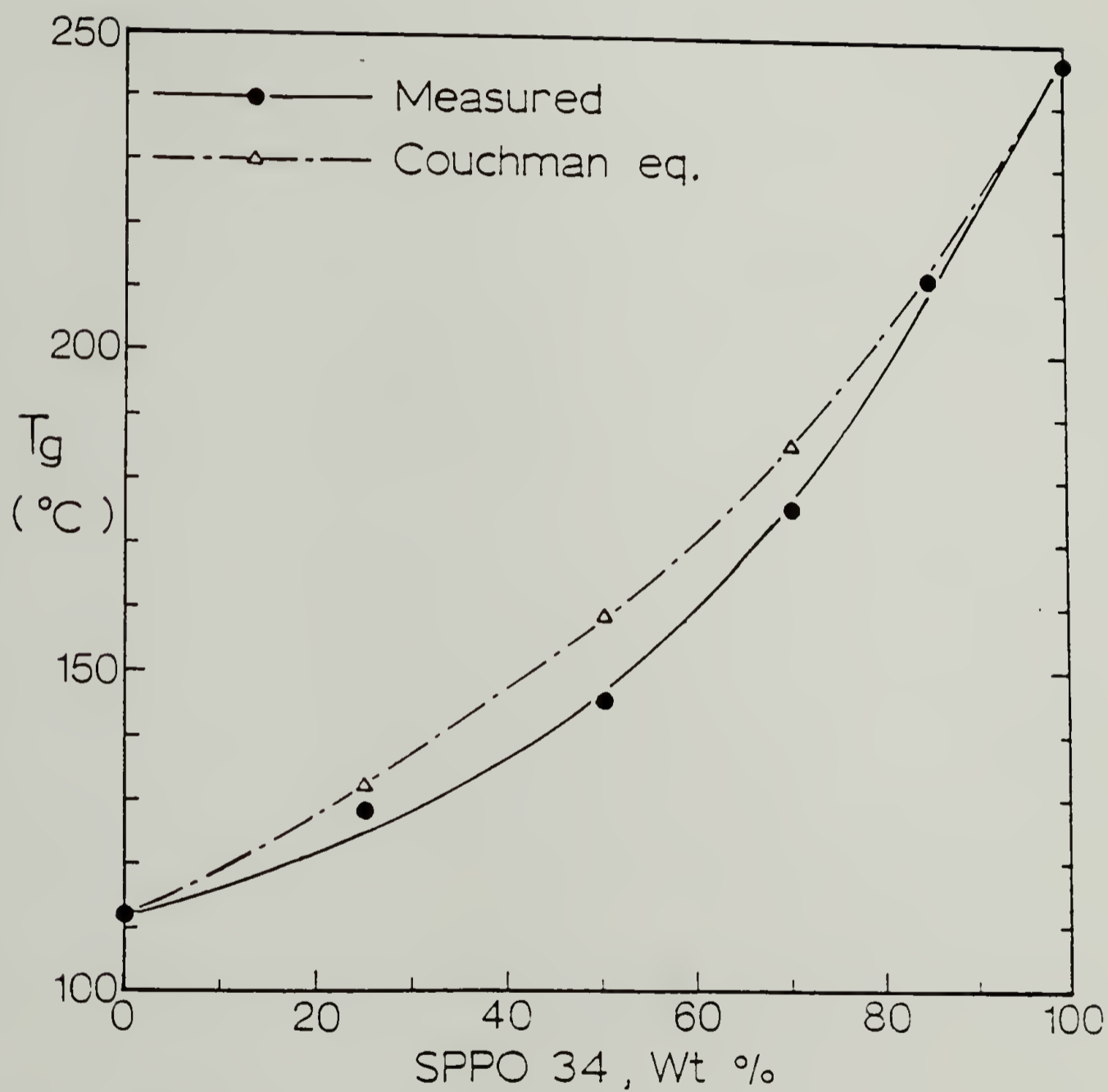


Figure 6.2. Composition dependences of  $T_g$ 's for the P(S-pFS, 77)/

SPPO 34 blends

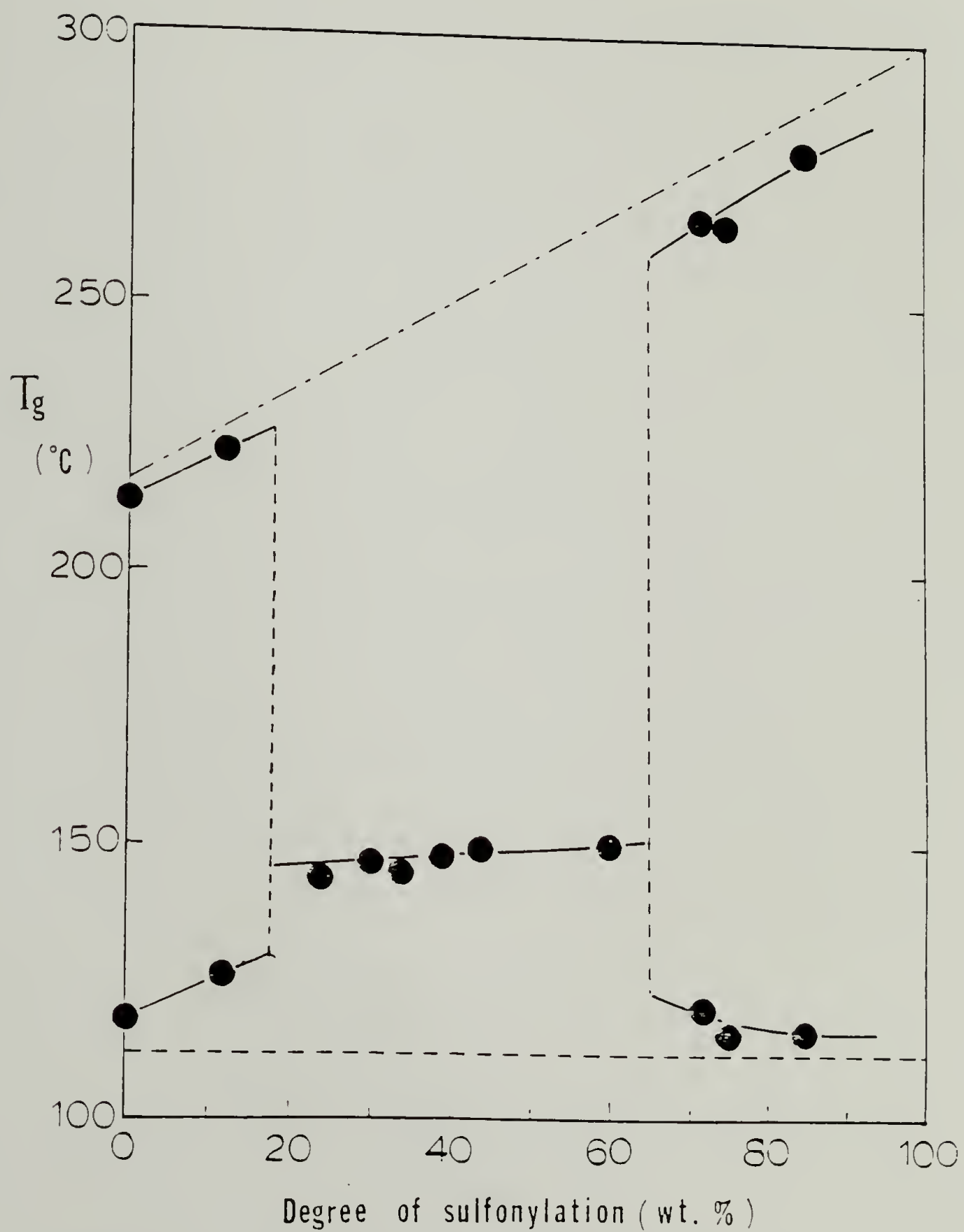


Figure 6.3.  $T_g$ 's for blends of P(S-pFS, 77)/SPPO copolymers

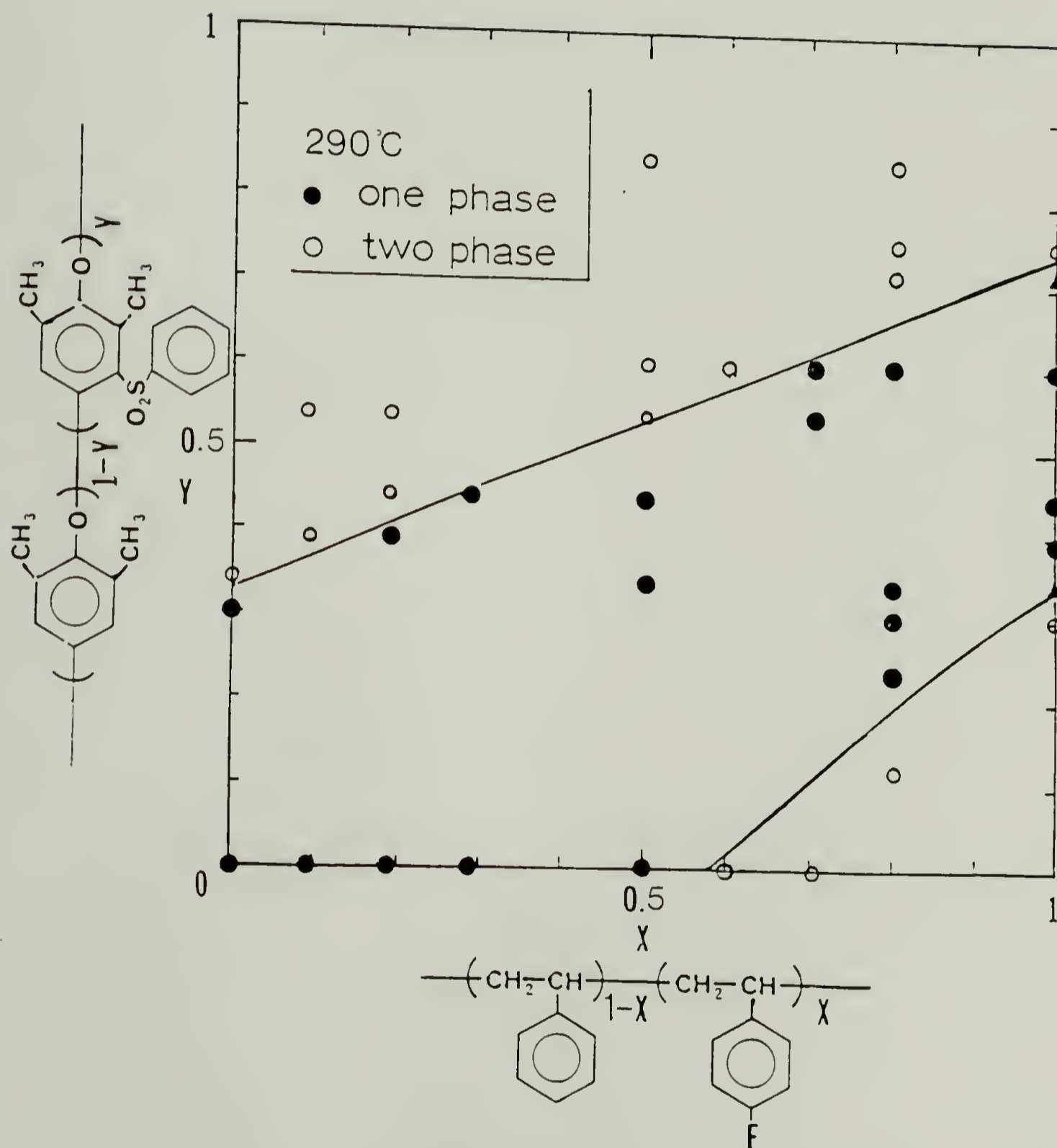


Figure 6.4. Miscibility domain for 50/50 wt% blends of P(S-pFS)/SPPO copolymers at 290°C

negative exchange interaction owing to "repulsion effects" without any specific interaction. Thus, a "window of miscibility" was observed for SPP0 copolymers with a degree of sulfonylation between 33-73 wt%.

Figure 6.5 shows the DSC thermograms illustrating the temperature induced phase separation associated with the existence of an LCST ; the results are collected in Figure 6.6. Figure 6.7 also shows the temperature induced phase separation in blends of poly(p-fluorostyrene) with SPP0 34.

In contrast to an argument presented by McMaster<sup>4</sup> that demixing of polymer-polymer mixtures at higher temperature must be expected when the nearest neighbor interaction parameter is negative, LCST phenomena were observed like in blends<sup>5</sup> of PPO/poly(p-chlorostyrene-co-o-chlorostyrene), even though all  $\chi_{ij}$ 's are positive. The LCST behavior may be explained by unfavorable compressibility contributions outweighing the negative exchange interaction due to "repulsive interactions" at higher temperature.

As seen in Figure 6.6, the greatest miscibility in the blends of poly(p-fluorostyrene) homopolymer with SPP0 copolymers can occur at a degree of sulfonylation of approximately 55 wt%. The function  $f(x,y)$  is defined by<sup>6</sup>

$$f(x,y) = \chi_{blend} - \chi_{blend}^{crit} \quad (6.1)$$

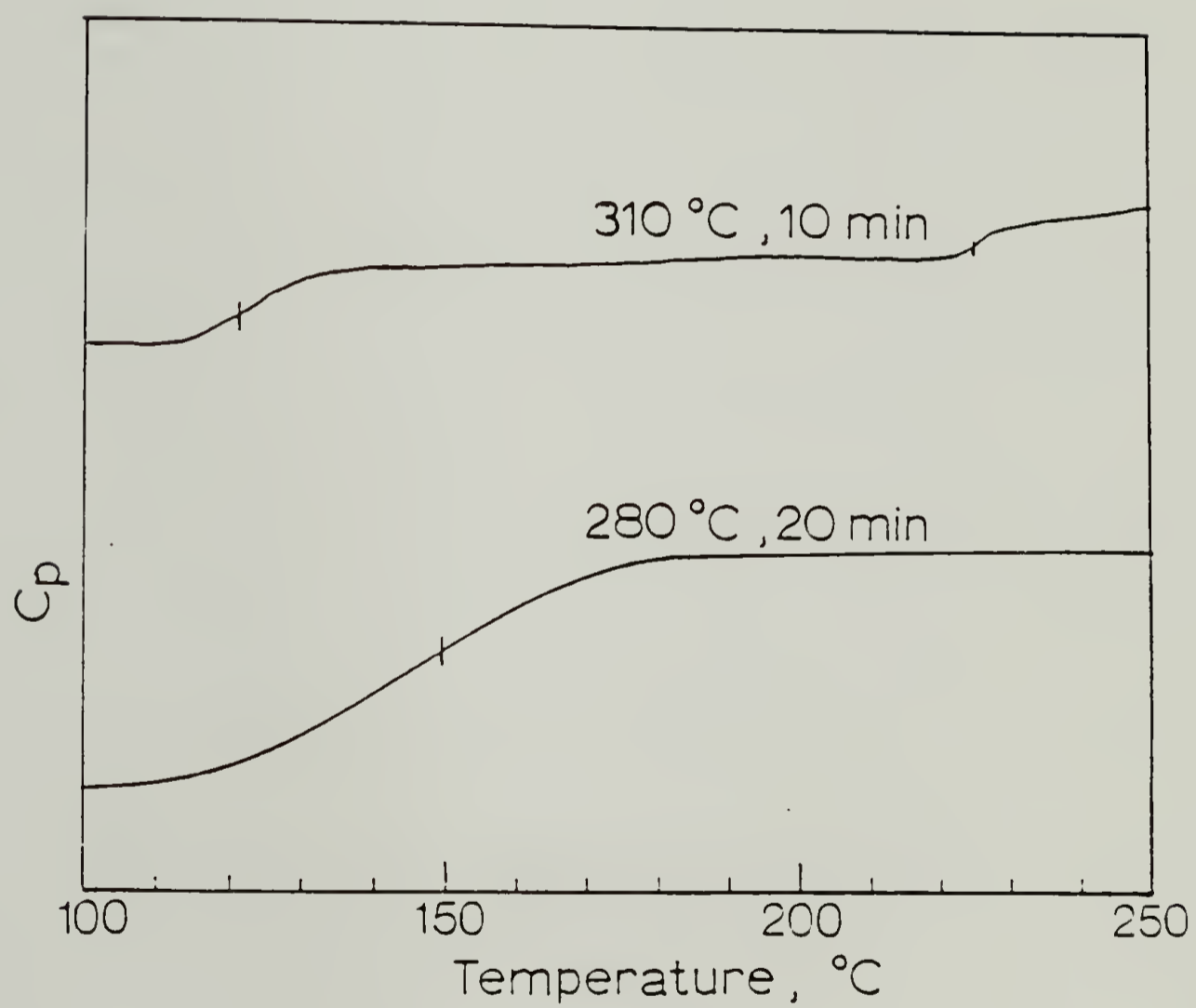


Figure 6.5. DSC thermograms for PpFS/SPP0 34 (50/50 wt% blend)

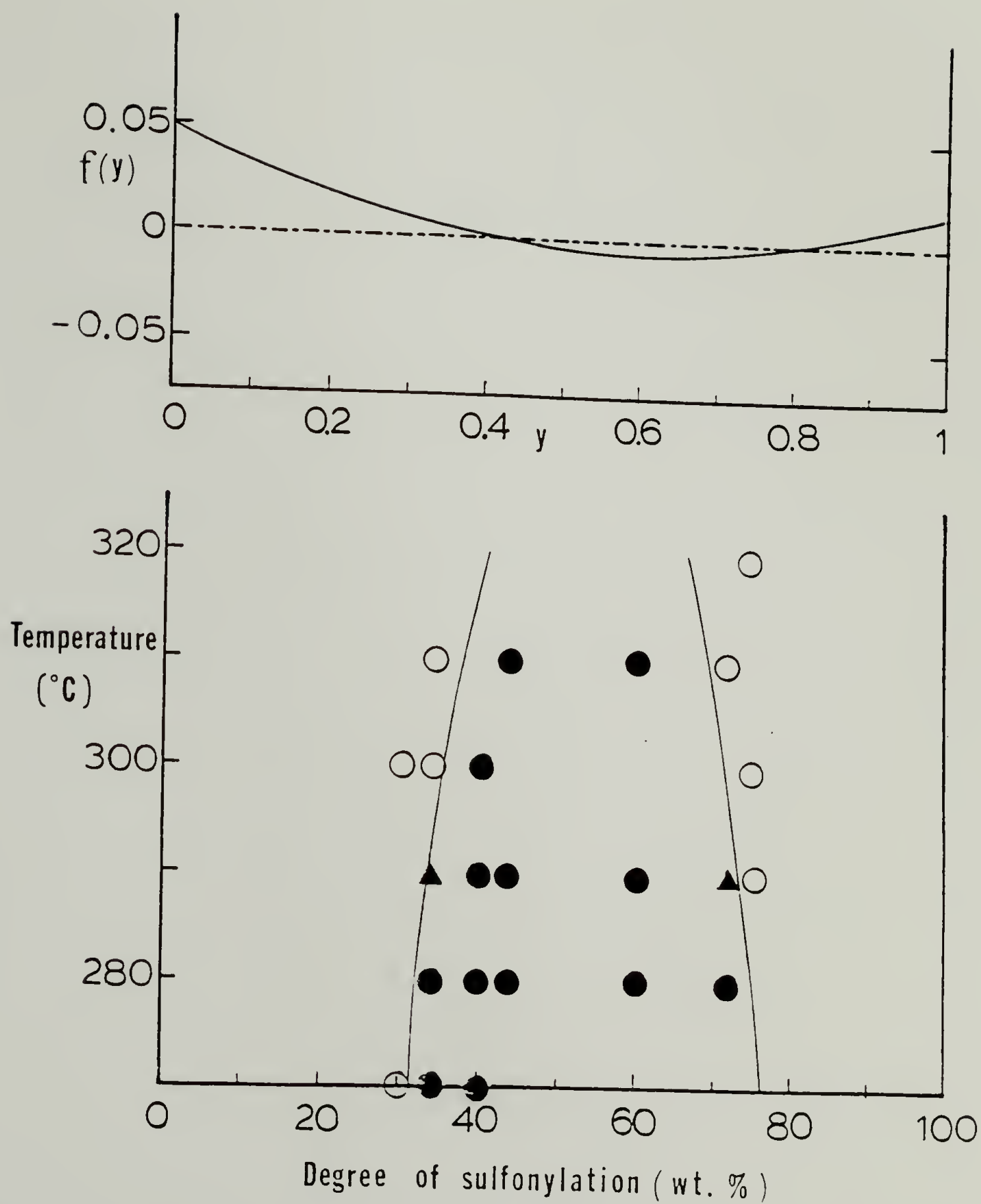


Figure 6.6. Miscibility of PpFS with SPPO copolymers. The insides of the curves represent the miscibility regions.

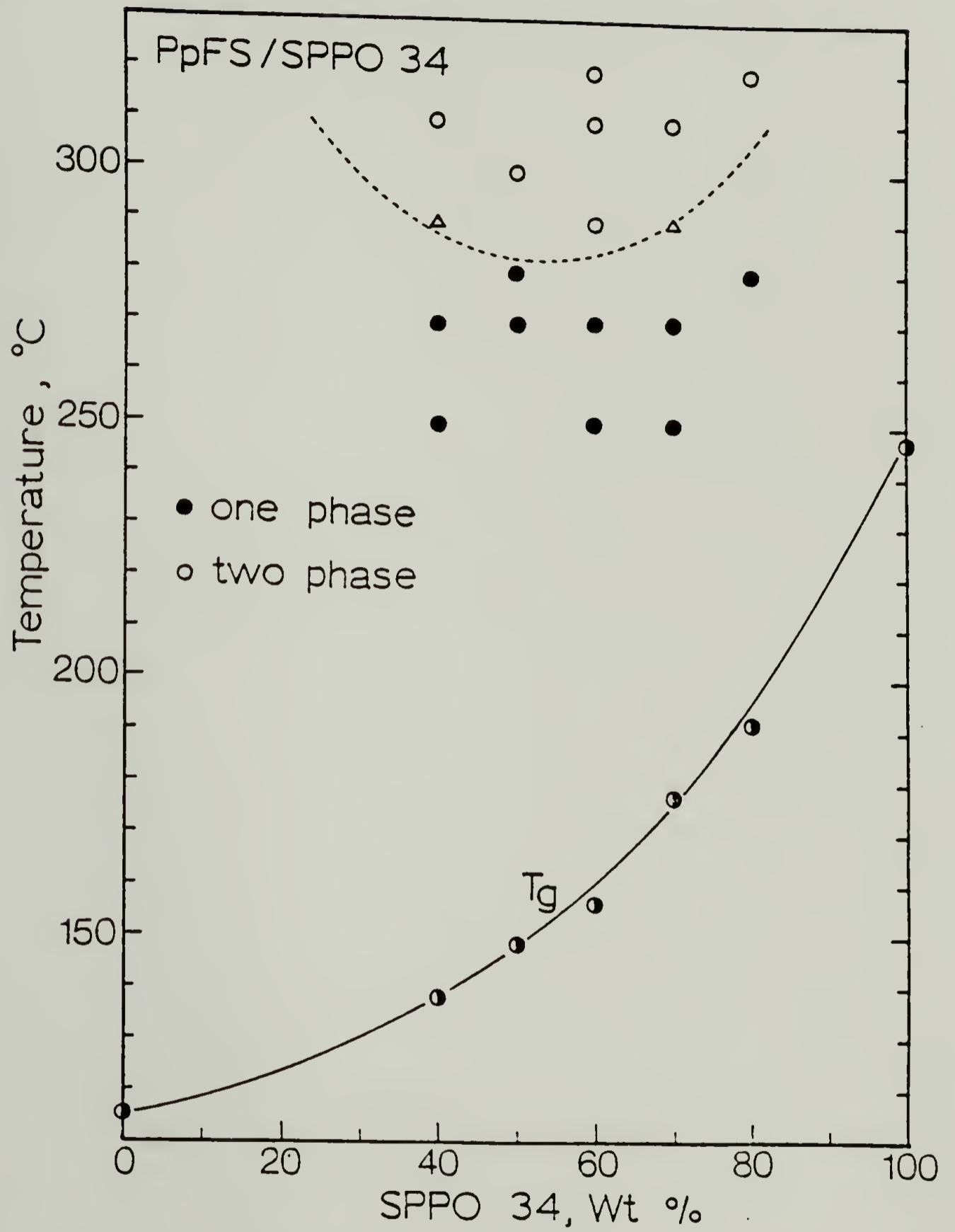


Figure 6.7. Phase diagram for blends of PpFS/SPPO 34

The sign of  $f(x,y)$  will determine miscibility or immiscibility in the range of  $0 \leq x, y \leq 1$ ; the region of miscibility will be found if  $f(x,y) < 0$  and that of immiscibility will be seen if  $f(x,y) > 0$ . The boundary line i.e., the consolute point of the particular blend with a given copolymer composition  $x$  and  $y$  is represented by  $f(x,y) = 0$ . In the case of the blends of poly(p-fluorostyrene) with SPP0 copolymers, the quadratic function  $f(y)$  is given by

$$\begin{aligned} f(y) &= (1-y)\chi_{BC} + y\chi_{BD} - y(1-y)\chi_{CD} - \chi_{blend}^{crit} \\ &= y^2\chi_{CD} + y(\chi_{BD} - \chi_{BC} - \chi_{CD}) + \chi_{BC} - \chi_{blend}^{crit} \end{aligned} \quad (6.2)$$

This function  $f(y)$  is a convex function of  $y$  for a given temperature. By introducing all the corresponding values into Eqn. (6.2), one obtains

$$\begin{aligned} f(y) &= 0.15y^2 - 0.185y + 0.051 \\ &= 0.15(y - 0.615)^2 - 0.0057 \end{aligned} \quad (6.3)$$

As seen in Figure 6.6, the minimum of  $f(y)$  i.e., the maximum miscibility is predicted at  $y = 0.62$ . This prediction based on a mean field treatment is in reasonable agreement with the experimental findings. As stated earlier, the maximum in the miscibility window occurs at a degree of sulfonylation of 55 wt%.

ii). Blends of Poly(styrene-co-o-fluorostyrene) with SPP0 Copolymers

These systems represent blends of the type

$(A_{1-x}B_x)_{n_1} / (C_{1-y}D_y)_{n_2}$  in which A, B, C and D represent styrene, o-fluorostyrene, unsulfonylated phenylene oxide and sulfonylated phenylene oxide units, respectively.

Initially, the miscibility behavior of blends of poly(o-fluorostyrene) with PPO was reexamined. In contrast to the results of Vukovic's<sup>1,2</sup>, these blends were found to be miscible using films cast from chloroform. It should be noted that Vukovic prepared the blend samples by coprecipitation into methanol from toluene solution. Discrepancies in the assessment of miscibility may be due to incomplete mixing. Figure 6.8 displays the composition dependence of  $T_g$ 's of the blends. No change in either transition width or  $T_g$  could be observed even after annealing up to 310°C. Accordingly, these results imply that  $\chi_{BC}$  is nearly equal to  $\chi_{blend}^{crit} = 0.004$  and, hereafter, a value of  $\chi_{BC} = 0.004$  will be adopted.

Figure 6.9 shows the composition dependence of the  $T_g$ 's for the blends of poly(styrene-co-o-fluorostyrene, 80) with SPP0 12. Figure 6.10 shows the experimental composition-composition diagram demarcating the miscibility and immiscibility boundary.  $\chi_{BD}$  was

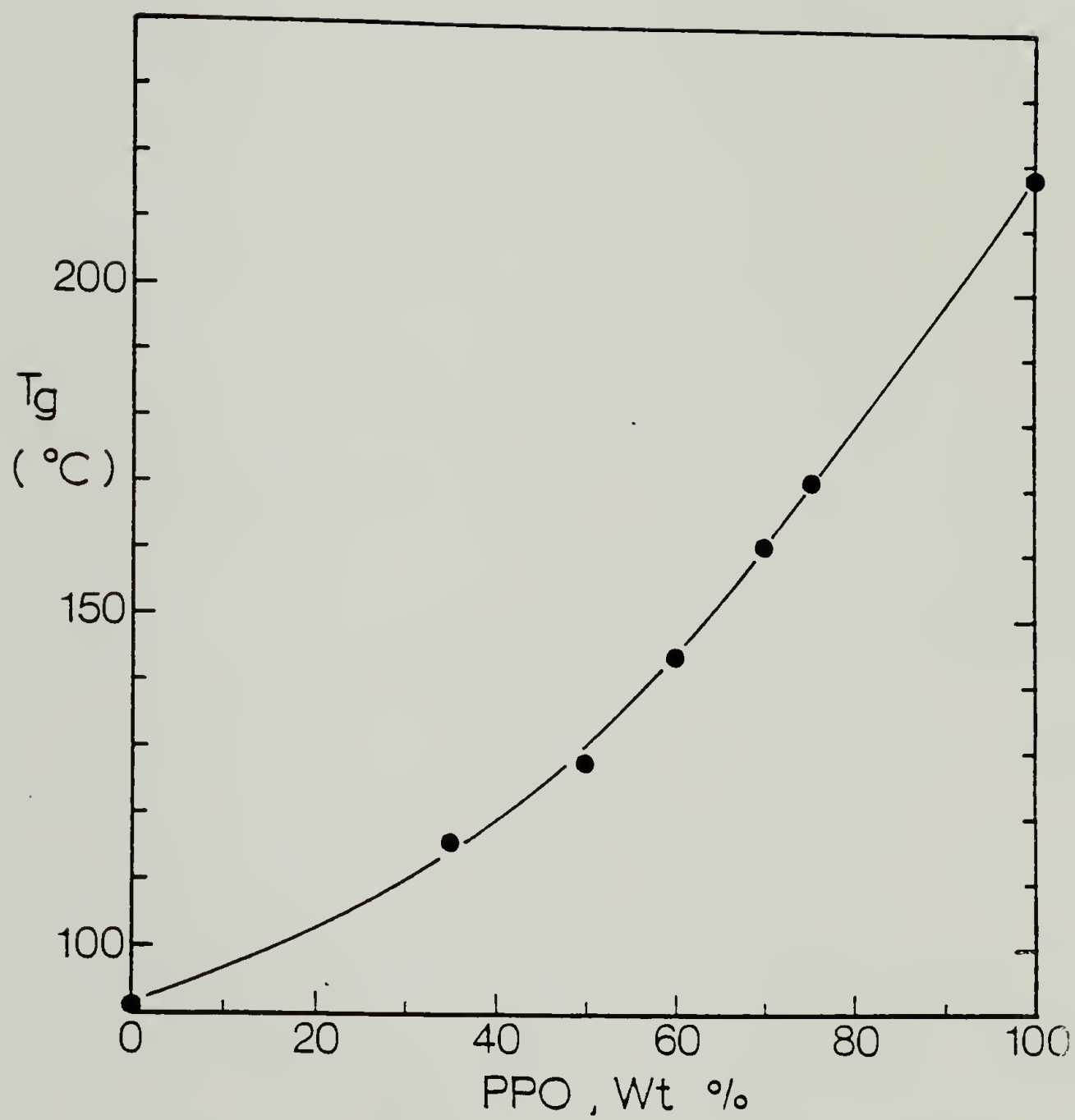


Figure 6.8. Composition dependences of  $T_g$ 's for blends of PoFS/PPO

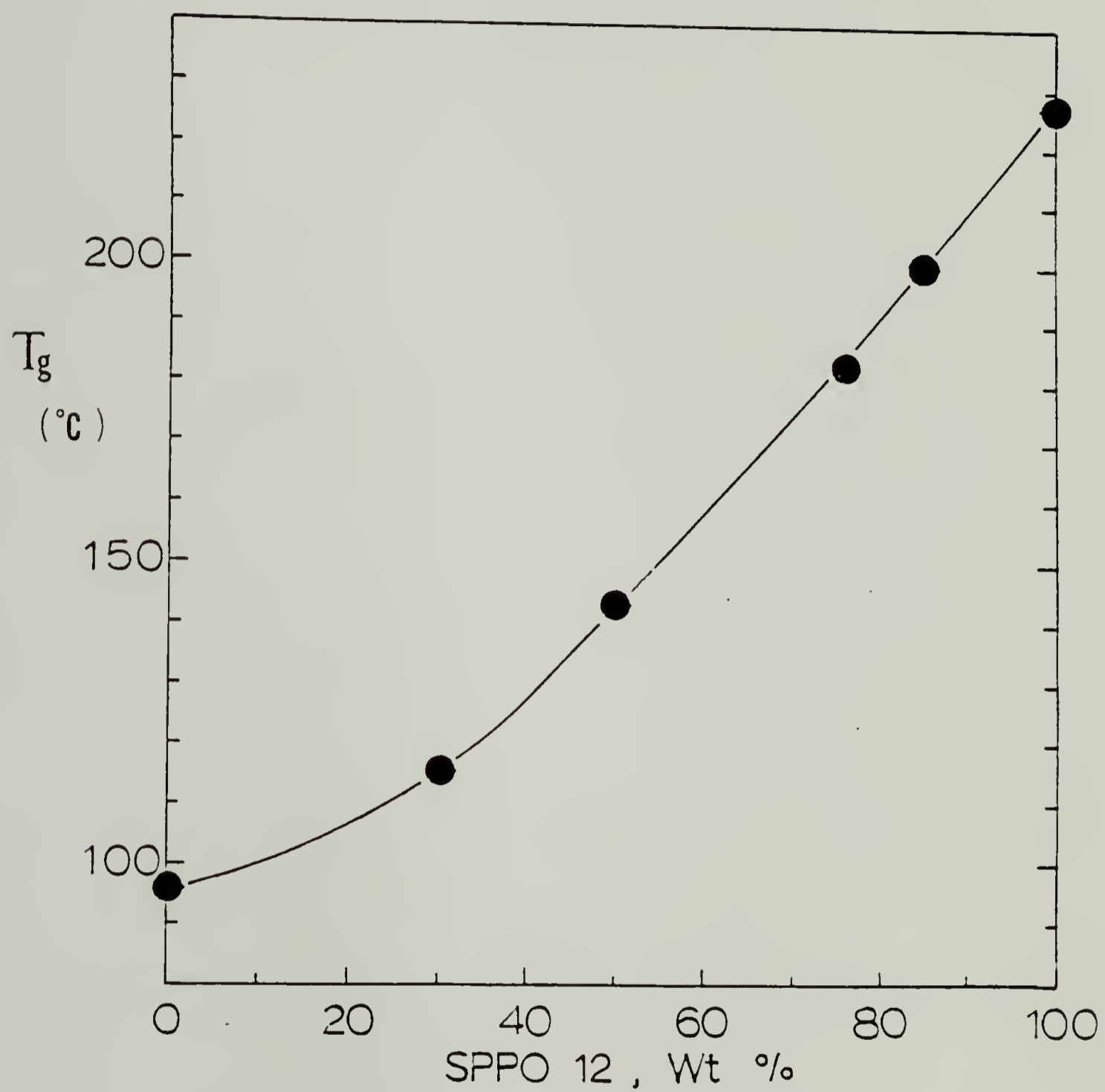


Figure 6.9. Composition dependences of  $T_g$ 's for blends of

P(S-oFS, 80)/SPPO 12

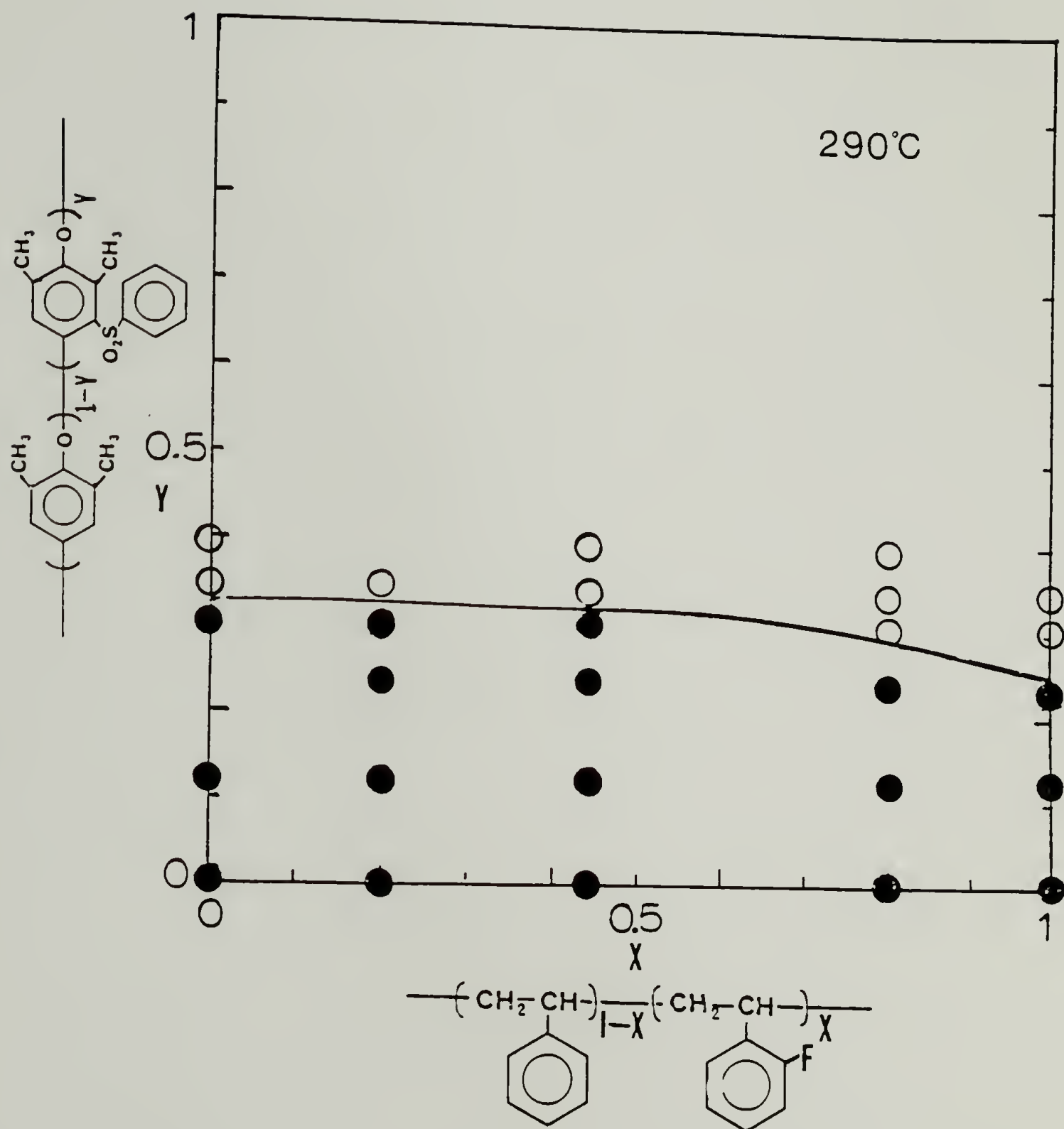


Figure 6.10. Miscibility domain for 50/50 wt% blends of P(S-oFS)/SPP0 copolymers at 290°C

determined to be 0.12 from the critical degree of sulfonylation in the far right abscissa of this diagram. It should be noted that  $x_{BD}$ 's in the systems (I) and (II) are greatly different indicative of the isomeric effect of the fluorine atom. This may be due to polar and size effects of the substituents which affect the polymer-polymer miscibility<sup>7</sup>. From the comparison of miscibility behavior in blends of PPO with copolymers of styrene with various halogenated styrene, Ryan<sup>7</sup> found that p-fluoro substituent of polystyrene has greater power in inducing immiscibility with PPO than an o-fluoro substituent. However, in the current system, the poly(styrene-co-p-fluorostyrene) has a much wider miscibility regime with SPPO copolymers than poly(styrene-co-o-fluorostyrene), which is ascribed to the role of "repulsive interactions" found in the blends of poly(p-fluorostyrene) with SPPO copolymers.

### iii). Blends of Poly(styrene-co-methyl acrylate) with SPPO Copolymers

These systems represent blends of the type

$(A_{1-x}B_x)_{n_1} / (C_{1-y}D_y)_{n_2}$  in which A, B, C and D represent styrene,

methyl acrylate, unsulfonylated phenylene oxide and sulfonylated phenylene oxide units, respectively. Figure 6.11 shows SMA copolymer versus feed composition. Although a series of copolymers over the whole composition range has not been prepared, the reactivity ratios of styrene (1) and methyl acrylate (2) have been evaluated according

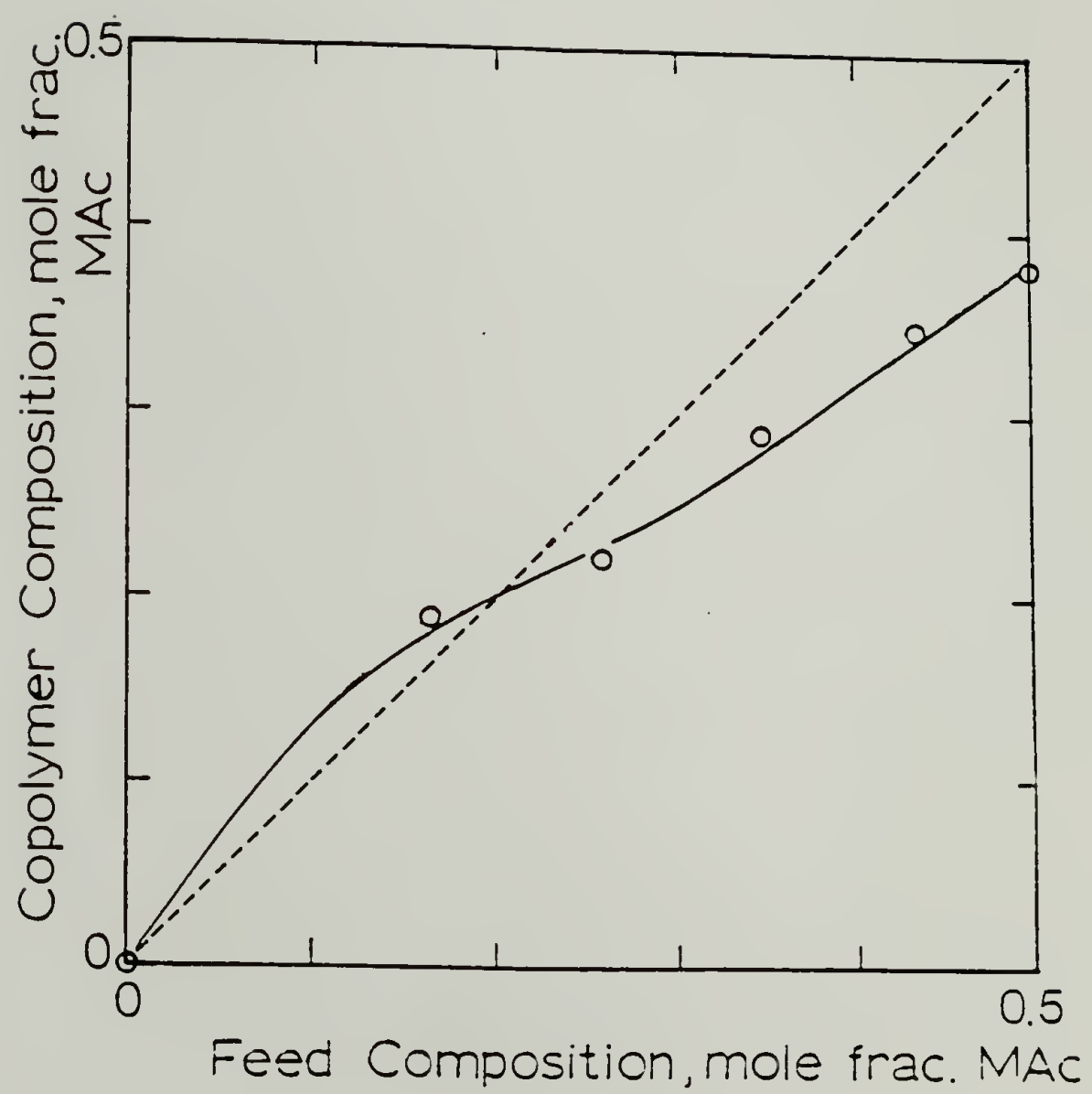


Figure 6.11. SMA copolymer vs. feed composition

to the methods of Fineman and Ross<sup>8</sup>. The reactivity ratios determined ( $r_1 = 0.95$ ,  $r_2 = 0.20$ ) are in reasonable agreement with the literature values ( $r_1 = 0.7$ ,  $r_2 = 0.15$ )<sup>9</sup>. Figure 6.12 displays the  $T_g$ 's of SMA copolymers and a comparison of the compositional variation of  $T_g$  to the Fox equation with  $k=1$ . The  $T_g$  of poly(methyl acrylate) was taken to be  $6^\circ\text{C}$ <sup>10</sup>. The calculated  $T_g$  values are in reasonable agreement with the experimental values.

To determine a segmental interaction parameter for styrene and methyl acrylate units ( $\chi_{AB}$ ), the miscibility behavior in blends of SMA copolymers which differ only in composition was studied. Figure 6.13 shows a DSC thermogram for 50/50 wt% blend of SMA 15/SMA 34, and indicates phase separation. These blends exhibited no change in phase stability i.e., homogenization of immiscible blends by annealing. On the basis of a series of DSC and optical microscopy studies a miscibility diagram for 50/50 wt% blends of SMA copolymers, as seen in Figure 6.14, could be constructed. The critical composition difference is seen to be 15 wt%. By employing Eqn. (3.2),  $\chi_{AB}$  is then determined to be 0.13. Figure 6.15 shows the composition-composition diagram ("C-C plots") displaying the miscibility-immiscibility boundary for 50/50 wt% blends at  $290^\circ\text{C}$ . Figure 6.15 indicates that the critical methyl acrylate content for

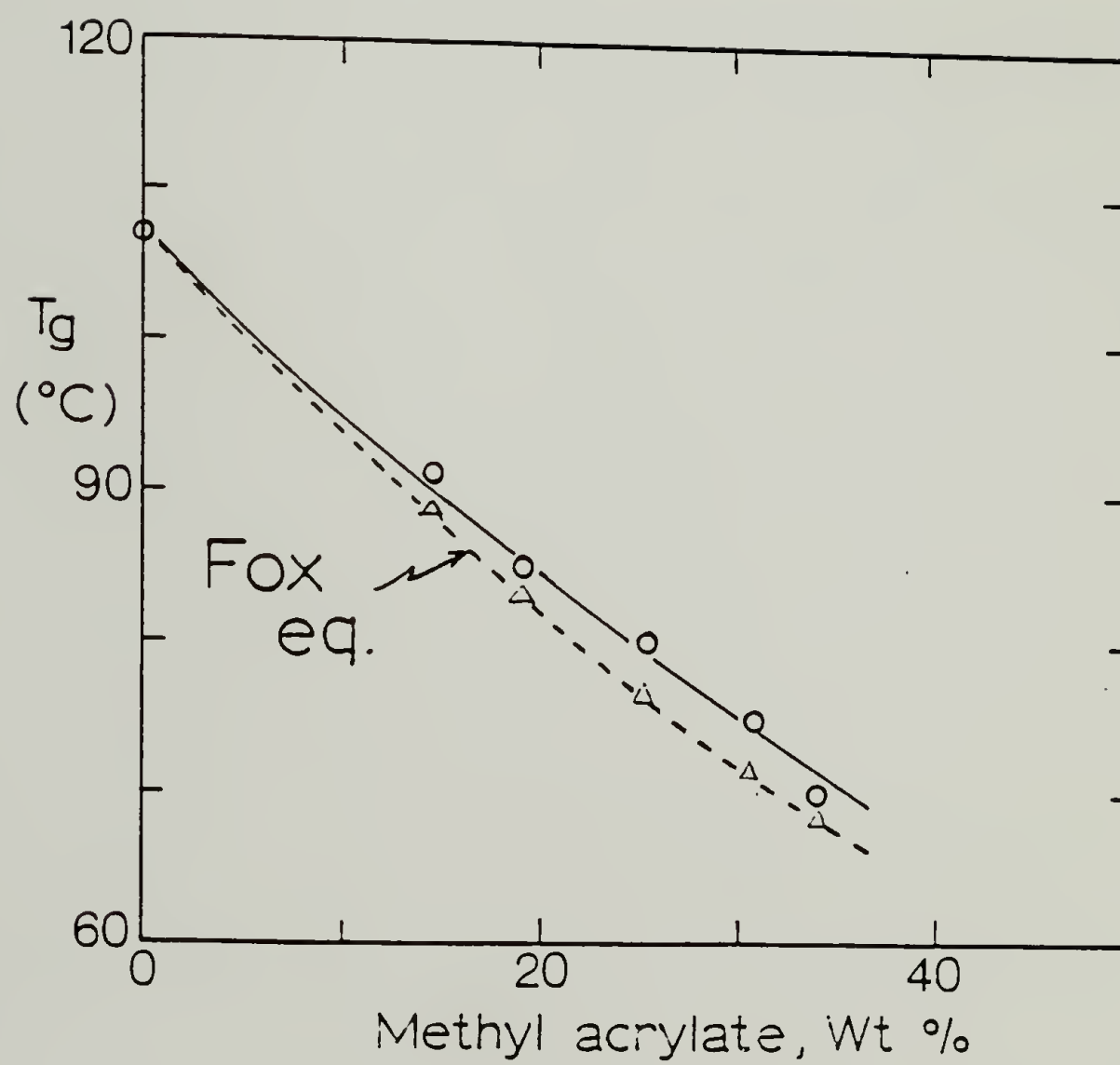


Figure 6.12.  $T_g$ 's of SMA copolymers

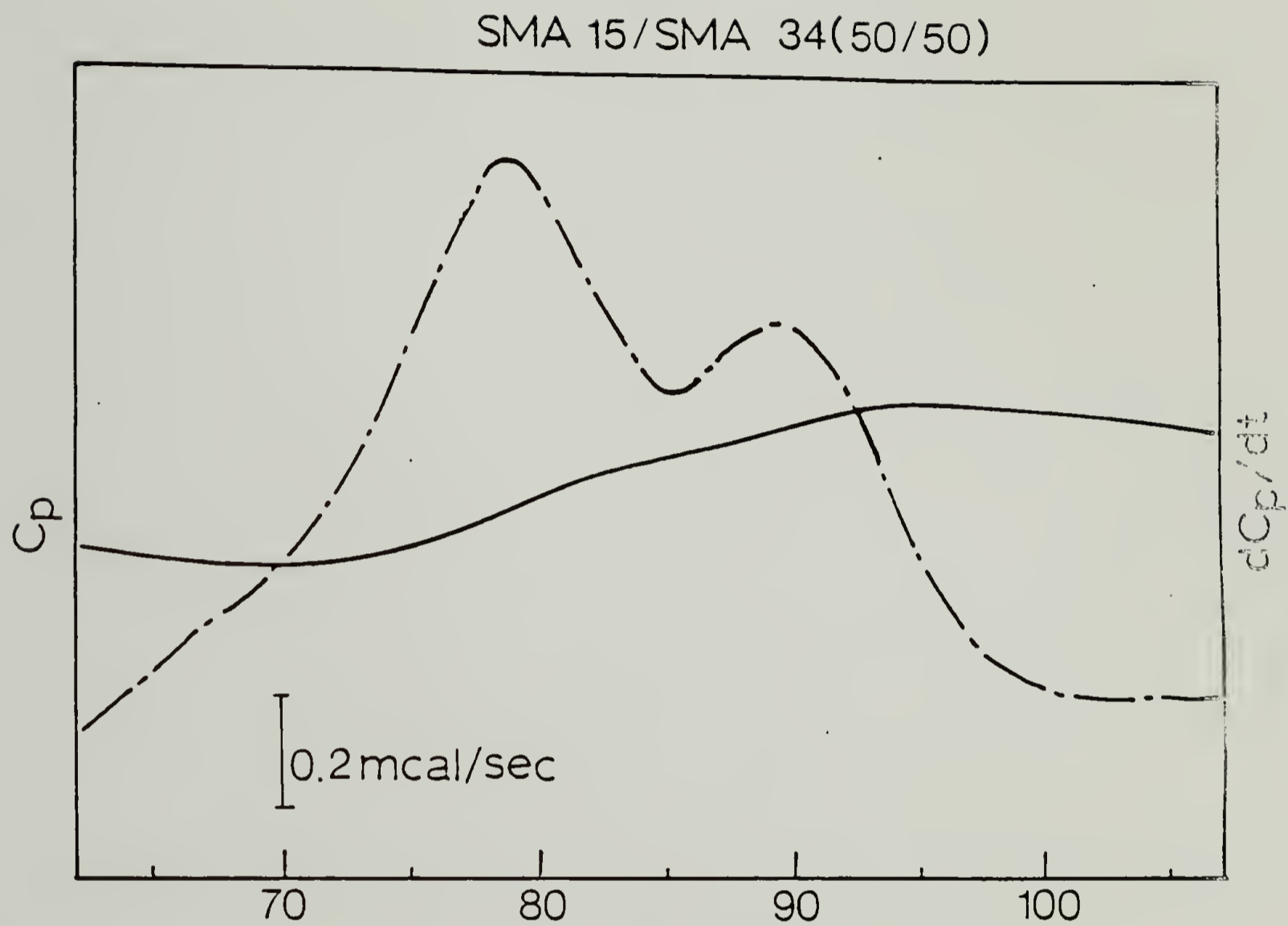


Figure 6.13. DSC thermogram for 50/50 wt% blend of SMA 15/SMA 34

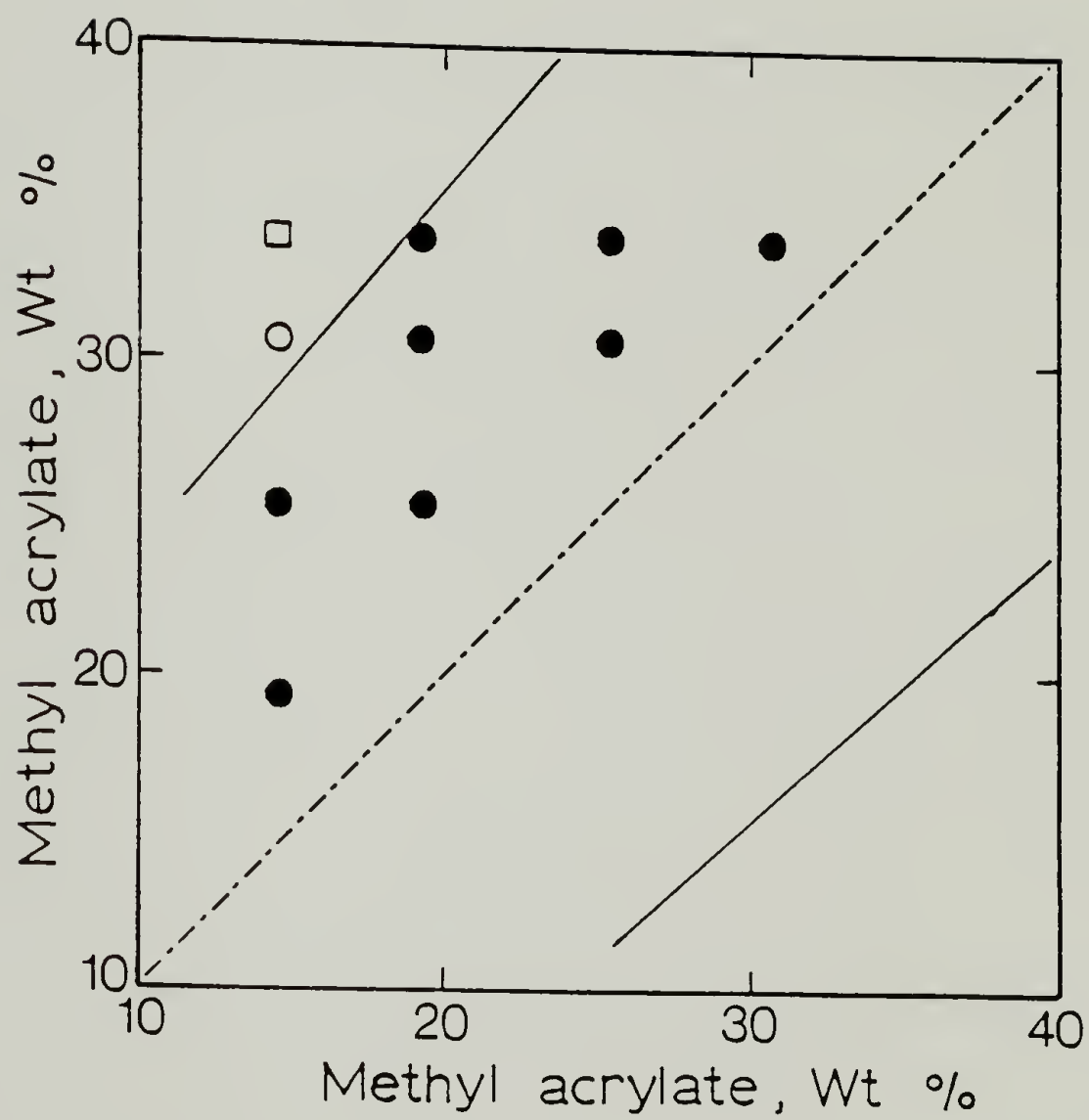


Figure 6.14. Miscibility diagram for 50/50 wt% blends of SMA copolymers

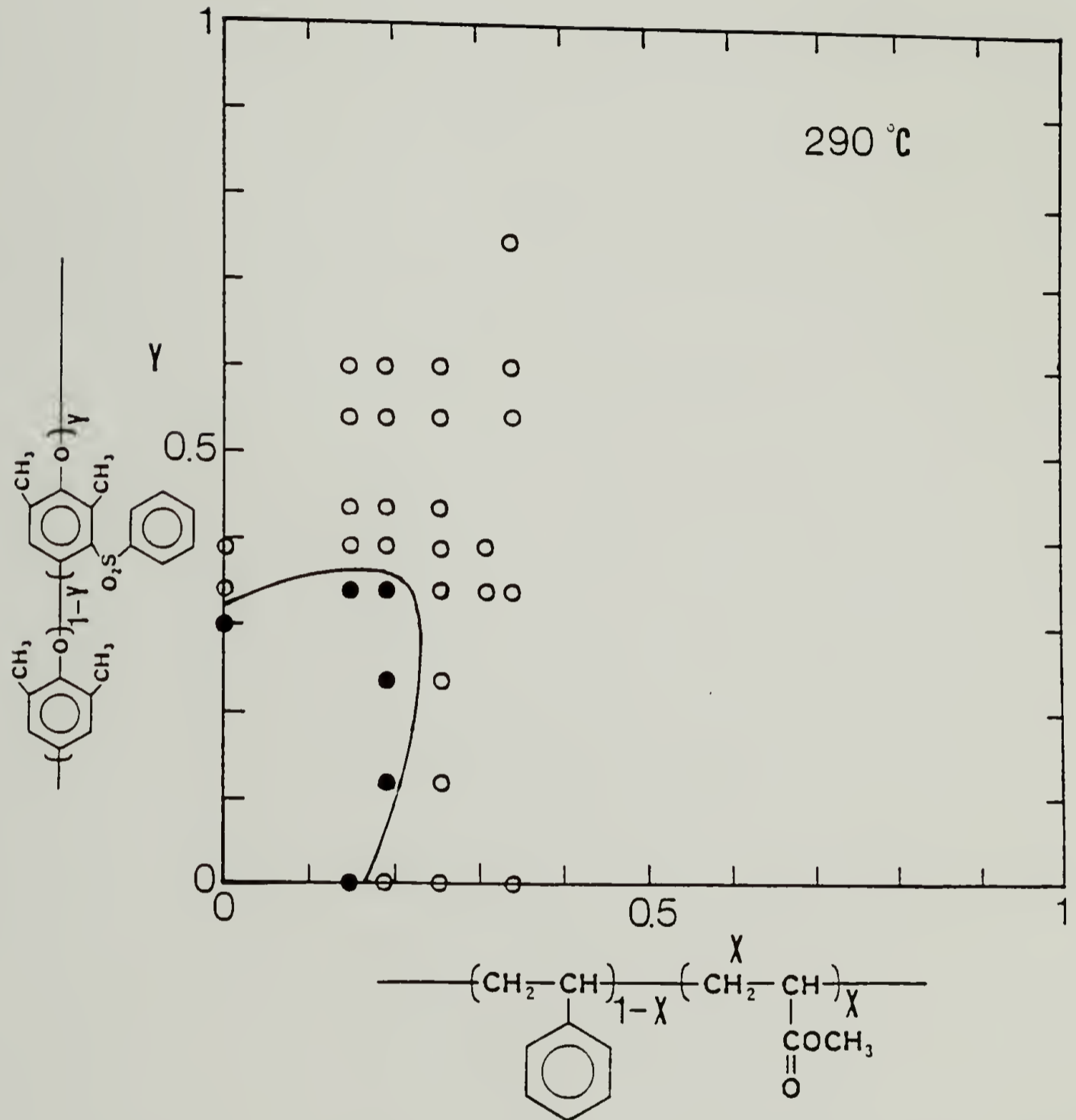


Figure 6.15. Miscibility domain for 50/50 wt% blends of SMA copolymers with SPP0 copolymers at 290°C

miscibility in blends of SMA copolymers with PPO homopolymer is 18wt%. By employing Eqn. (5.2)  $\chi_{BC}$  is determined to be 0.32.

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## CHAPTER VII

### CONCLUSIONS

#### A. Geometric Analysis of the Miscibility-Immiscibility Boundary

According to a mean field treatment, as described in Chapter I, from arrangement of Eqn. (1.14),  $x_{\text{blend}}$  is given by

$$\begin{aligned} x_{\text{blend}} = & x_{AB}x^2 + (x_{AC} - x_{BC} - x_{AD} + x_{BD})xy \\ & + x_{CD}y^2 + (x_{BC} - x_{AC} - x_{AB})x \\ & + (x_{AD} - x_{AC} - x_{CD})y + x_{AC} \end{aligned} \quad (7.1)$$

The function  $f(x,y)$  is defined by

$$f(x,y) = x_{\text{blend}} - x_{\text{blend}}^{\text{crit}} \quad (7.2)$$

In a miscibility regime displayed in a Cartesian coordinate system in which the abscissa and ordinate represent the compositions of the respective copolymers, the boundary line demarcating the miscibility-immiscibility region is given by  $f(x,y) = 0$ . This function is a generalized form of the quadratic equation. Depending upon the set

of segmental interaction parameters this function can describe a straight line, circle, ellipse, parabola or hyperbola. Table 7.1 summarizes coefficients of  $x$ ,  $y$  and the cross term,  $xy$ .  $x$  and  $y$  coefficients for all the systems except SMA copolymer systems are negligible compared with  $xy$  coefficients which are related to axial rotation. Figure 7.1 displays a comparison of the experimentally determined and calculated miscibility domains, employing values listed under each diagram and a computer program listed in the Appendix I. The calculated and experimental results are in reasonably good agreement and all the miscibility domains include  $x, y = 0$  corresponding to the miscibility of the homopolymers A and C. A diagnostic test to determine the shapes of curves may be helpful. In the generalized form of equation

$$ax^2 + bxy + cy^2 + dx + ey + f = 0 \quad (7.3)$$

if  $(b^2 - 4ac) < 0$ , then the curve will be an ellipse

$= 0$ , a parabola

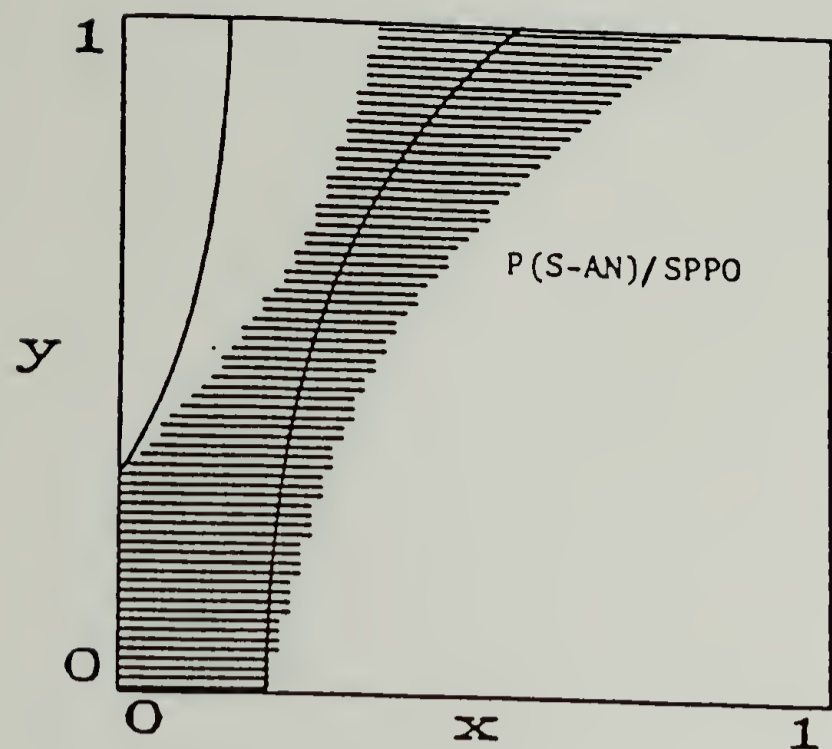
$> 0$ , a hyperbola

Table 7.1 also includes values of  $(b^2 - 4ac)$ . From these values the miscibility and immiscibility boundaries for p(S-AN) and P(S-pFS) systems are considered to have forms of a pair of hyperbolas. The miscibility regions for p(S-oFS) and SMA systems are considered to be contained by ellipses.

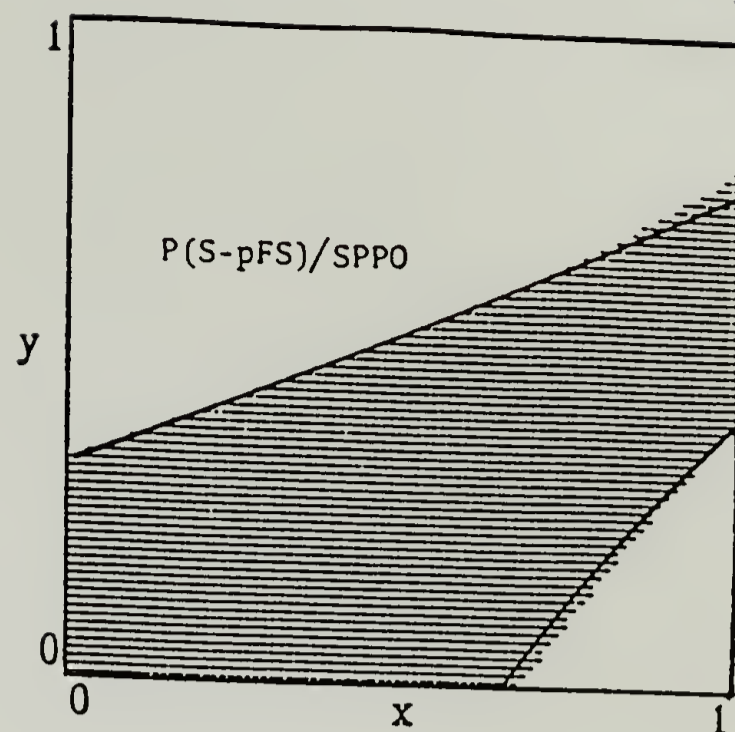
Table 7.1

Coefficients of  $x$ ,  $y$  and  $xy$  for Geometric Analysis

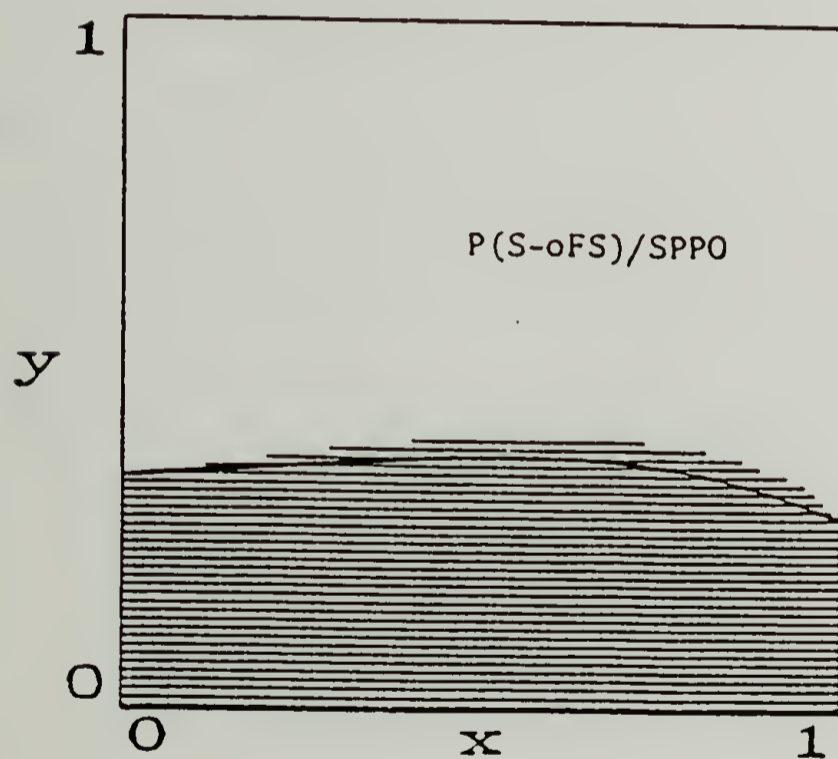
	$x$	$y$	$xy$	$b^2 - 4ac$
poly(styrene-co-acrylonitrile) system	0.088	0.093	-0.891	0.374
poly(styrene-co-p-fluorostyrene)	0.016	0.093	-0.274	0.027
poly(styrene-co-o-fluorostyrene)	0.007	0.093	-0.134	-0.006
poly(styrene-co-methyl acrylate)	0.183	0.093	-0.513	



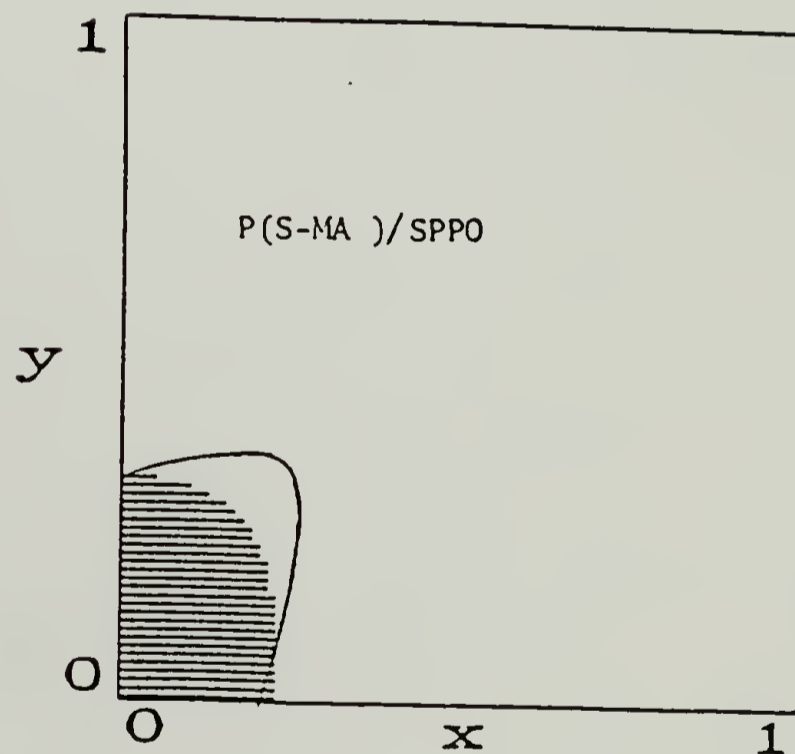
$$\begin{aligned} \chi_{AB} &= 0.700 & \chi_{AC} &= -0.043 & \chi_{AD} &= 0.200 \\ \chi_{BC} &= 0.745 & \chi_{BD} &= 0.097 & \chi_{CD} &= 0.150 \\ \chi_{blend}^{crit} &= 0.003 \end{aligned}$$



$$\begin{aligned} \chi_{AB} &= 0.080 & \chi_{AC} &= -0.043 & \chi_{AD} &= 0.200 \\ \chi_{BC} &= 0.053 & \chi_{BD} &= 0.022 & \chi_{CD} &= 0.150 \\ \chi_{blend}^{crit} &= 0.004 \end{aligned}$$



$$\begin{aligned} \chi_{AB} &= 0.040 & \chi_{AC} &= -0.043 & \chi_{AD} &= 0.200 \\ \chi_{BC} &= 0.004 & \chi_{BD} &= 0.113 & \chi_{CD} &= 0.150 \\ \chi_{blend}^{crit} &= 0.004 \end{aligned}$$



$$\begin{aligned} \chi_{AB} &= 0.150 & \chi_{AC} &= -0.043 & \chi_{AD} &= 0.200 \\ \chi_{BC} &= 0.290 & \chi_{BD} &= 0.020 & \chi_{CD} &= 0.150 \\ \chi_{blend}^{crit} &= 0.004 \end{aligned}$$

Figure 7.1. Comparison of calculated (shaded regions) and experimental (solid lines) miscibility domains

## B. Summary of Results

A series of new thermally stable sulfonylated poly(2,6-dimethyl-1,4-phenylene oxide) (SPP0) copolymers has been prepared and characterized. These copolymers were mixed with the styrenic copolymers; poly(styrene-co-acrylonitrile), poly(styrene-co-p-fluorostyrene), poly(styrene-co-o-fluorostyrene) and poly(styrene-co-methyl acrylate). The monomer sequence distribution in poly(styrene-co-acrylonitrile) samples has also been investigated to confirm that they are of random nature.

The extent of miscibility and the phase stability above the glass transition temperature have been explored. Critical phenomena observed in this work are of an LCST type. The role of intramolecular interaction in inducing miscibility has been identified. A mean field treatment has been successfully applied to blends system of type " $(A_{1-x}B_x)_{n_1} / (C_{1-y}D_y)_{n_2}$ " and the experimental miscibility-immiscibility boundaries are in reasonably good agreement with calculated boundaries.

### C. Suggestions for Future Work

It might prove interesting to study the effect of blending on the low-temperature secondary relaxation of the component polymers, particularly in the blends of poly(styrene-co-acrylonitrile) with SPP0 copolymers. These secondary relaxations are more sensitive to the small-scale local environment and such studies could provide valuable information. Many of the studies in this work involved only 50/50 wt% blends to determine the miscibility domain. If one uses the blend compositions corresponding to the critical solution temperatures, then the estimation of the  $\chi_{ij}$ 's will have much more significance. The employment of samples of lower polydispersity and lower  $T_g$ 's might also clarify the phase behavior and allow study of the temperature dependence of the  $\chi_{ij}$ 's.

The blends of poly(p-fluorostyrene) with SPP0 copolymers have been found to be miscible for degree of sulfonylation ranging from 33 to 73 wt%, even though none of the homopolymer pairs is miscible. Accordingly, thermodynamic manifestations of the miscibility in these blends with other techniques such as vapor sorption measurements would make a rewarding study.

Finally, in the blends of polystyrene with SPP0 copolymers, a comparison of the  $T_g$  transition width determined by DSC either with

direct morphological studies or with widths of dynamic loss spectra would be worthwhile.

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APPENDIX I

MISCIBILITY DIAGRAM COMPUTER PROGRAM

```

605 '--- Introduction display
610 CLS:SCREEN 0:X#=STRING$(73,45)
620 PRINT X#
630 PRINT "These programs are of two types : scanning &
        plotting. Scanning programs"
640 PRINT "produce crude but fast displays of the sign of
        Xblend values for various"
650 PRINT "x-parameter values. They can be used to search
        for x-parameter values for"
660 PRINT "which the Xblend function is negative and posi-
        tive in region that you"
670 PRINT "specify. Plotting programs generate higher -
        quality graphs that can be"
680 PRINT "displayed at a terminal or on the printer. "
690 PRINT:PRINT "To run a program type one of the options
        given below. For example, the"
700 PRINT "following will allow you to scan Xblend func-
        tion of x and y."
710 PRINT:PRINT "Enter an option, or 'q' to quit : s (cr)"
790 DIM X(50),Y(50),F(50),CHI$(7),CHIOPT(7,5),CHIVAL(7,20),
        CHIS(50,7),P$(13,12)
830 CHI$(1)="(1)Xab":CHI$(2)="(2)Xac":CHI$(3)="(3)Xad":
        CHI$(4)="(4)Xbc":CHI$(5)="(5)Xbd":CHI$(6)="(6)Xcd":
        CHI$(7)="(7)Xcrit"
1070 '
1080 '
1090 PRINT:PRINT X#
1093 FOR I=1 TO 7
1095 CHIOPT(I,1)=1:CHIOPT(I,2)=4:CHIOPT(I,3)=-.1:
        CHIOPT(I,4)=.1
1097 NEXT I
1100 PRINT SPC(11) "Dependent Number of"
1110 PRINT " Options Variables X-para Source
1120 PRINT X#
1130 PRINT " S or F x,y" SPC(8) "7" SPC(8) "Kang"
1140 PRINT X#:PRINT
1150 INPUT "Enter an option, or 'q' to quit : ",A$
1160 IF A$<>"S" AND A$<>"s" AND A$<>"F" AND A$<>"p" AND
        A$<>"Q" AND A$<>"q" THEN GOTO 1150
1170 IF A$="S" OR A$="s" THEN GOTO 1300 ELSE IF A$="F" OR
        A$="p" THEN GOTO 4000 ELSE STOP
1290 '
1300 REM --- Scanning menu display
1310 PRINT:PRINT X#:PRINT "Do you want to:"

```

```

1320 PRINT "      (f) change the type of function to search
      for,"
1330 PRINT "      (c) change the chi values to use during
      the search,"
1340 PRINT "      (s) do the search, or"
1350 PRINT "      (q) quit?":PRINT X$
1360 INPUT "Enter f,c,s or q : ",A$
1370 IF A$<>"F" AND A$<>"f" AND A$<>"C" AND A$<>"c" AND
      A$<>"S" AND A$<>"s" AND A$<>"Q" AND A$<>"q" THEN
      GOTO 1360
1380 IF A$="F" OR A$="f" THEN GOTO 1500 ELSE IF A$="C" OR
      A$="c" THEN GOTO 1800 ELSE IF A$="S" OR A$="s" THEN
      GOTO 2500 ELSE GOTO 1090
1390 STOP
1490 '
1500 REM ---- function option
1510 PRINT X$:PRINT "      Option 'function' chosen.":PRINT
1520 PRINT "Specify the type of function you are looking
      for by entering"
1530 PRINT "For example : .2,.2,-1"
1540 PRINT "                      .2,.8,1"
1550 PRINT "                      .8,.8,1"
1560 PRINT "                      .8,.2,1"
1580 PRINT "Would search for X values producing a negative
      region in near"
1590 PRINT "the origin of the graph.":PRINT X$:PRINT
1600 NF=0
1610 NF=NF+1:INPUT "Enter next x and y and 1 or -1  ",X(NF),
      Y(NF),F(NF)
1615 IF X(NF) < 0 OR X(NF) > 1 OR Y(NF) < 0 OR Y(NF) > 1 OR
      (F(NF) <> 1 AND F(NF) <> -1) THEN GOTO 1618 ELSE
      GOTO 1620
1618 PRINT "Your input is not correct.":NF=NF-1:GOTO 1610
1620 INPUT "Do you want to enter another set of data? Type
      (y)es or (n)o ",A$
1625 IF A$<>"Y" AND A$<>"y" AND A$<>"N" AND A$<>"n" THEN
      GOTO 1620
1630 IF A$="Y" OR A$="y" THEN GOTO 1610 ELSE GOTO 1300
1770 '
1800 REM ---- chi option
1801 'chiopt[i,1] (1-original, 2-random ,3-specific, 4-
      range)
1802 'chiopt[i,2] :number of value
1803 'chiopt[i,3] :minimum , chiopt[i,4] : max. ,
      chiopt[i,5] : step
1810 PRINT "      Option 'chi' chosen.":PRINT
1820 'chiopt[i,2] :number of value
1825 PRINT

```

```

1830 FOR I=1 TO 7
1840 ON CHIOPT(I,1) GOSUB 1900,1930,1960,2100
1850 NEXT I
1860 GOTO 2200
1890 '
1900 REM--- original
1910 PRINT CHI$(I) " 4 values chosen randomly between
    -0.100 and 0.100."
1920 RETURN
1930 REM--- random
1940 PRINT CHI$(I) CHIOPT(I,2) "values chosen randomly
    between "; CHIOPT(I,3) " and " CHIOPT(I,4) " ."
1945 PRINT USING "+###.###\ \+###.###\ \";CHIOPT(I,3);" and
    ";CHIOPT(I,4);"."
1950 RETURN
1960 REM --- specific
1970 PRINT CHI$(I) CHIOPT(I,2) "values ";
1980 FOR J=1 TO CHIOPT(I,2)-1
1990 PRINT USING "+###.###";CHIVAL(I,J);
2000 NEXT J
2010 PRINT USING "+###.###\ \";CHIVAL(I,CHIOPT(I,2));"."
2020 RETURN
2090 '
2100 REM --- range
2110 PRINT CHI$(I) CHIOPT(I,2) "values from "; CHIOPT(I,3)
    " and " CHIOPT(I,4) " in steps of " CHIOPT(I,5) " ."
2115 PRINT USING "+###.###\ \+###.###\ \+###.###\ \";
    CHIOPT(I,3);" and ";CHIOPT(I,4);" in steps of ";
    CHIOPT(I,5);"."
2120 RETURN
2180 '
2190 REM --- chi value changing
2200 PRINT:INPUT "Which do you want to change(1 to 7) or
    (b)ack";A$
2205 IF A$<>"1" AND A$<>"2" AND A$<>"3" AND A$<>"4" AND
    A$<>"5" AND A$<>"6" AND A$<>"7" AND A$<>"B" AND A$<>"b"
    THEN GOTO 2200
2210 IF A$="B" OR A$="b" THEN GOTO 1300 ELSE S=VAL(A$)
2220 PRINT "    Option " CHI$(S) " chosen.":PRINT
2230 PRINT CHI$(S) ": Do you want "
2240 PRINT "    (r) random"
2250 PRINT "    (s) specific values or"
2260 PRINT "    (g) range of values?"
2270 INPUT"Enter r,s or g: ",A$
2280 IF A$<>"R" AND A$<>"r" AND A$<>"S" AND A$<>"s" AND
    A$<>"G" AND A$<>"g" THEN GOTO 2270
2290 IF A$<>"r" AND A$<>"R" THEN GOTO 2320
2300 PRINT "    Option 'random' chosen.":CHIOPT(S,1)=2

```

```

2310 GOTO 2400
2320 IF A$<>"S" AND A$<>"s" THEN GOTO 2350
2330 PRINT "      Option 'Specific' chosen.":CHIOPT(S,1)=3
2340 GOTO 2400
2350 PRINT "      Option 'Range' chosen.":CHIOPT(S,1)=4
2400 PRINT:INPUT "How many values? ",CHIOPT(S,2)
2405 IF CHIOPT(S,2)-INT(CHIOPT(S,2))<>0 THEN GOTO 2400
2410 IF A$<>"S" AND A$<>"s" THEN INPUT "Enter a minimum
      and a maximum value. ",CHIOPT(S,3),CHIOPT(S,4)
2420 IF CHIOPT(S,4)-CHIOPT(S,3) <= 0 THEN 2410
2430 SEED=INT((CHIOPT(S,4)-CHIOPT(S,3))*100)
2440 IF A$="G" OR A$="g" THEN CHIOPT(S,5)=(CHIOPT(S,4)-
      CHIOPT(S,3))/(CHIOPT(S,2)-1)
2450 IF A$<>"S" AND A$<>"s" THEN GOTO 1825
2460 FOR I=1 TO CHIOPT(S,2)
2470 INPUT "What is it? ",CHIVAL(S,I)
2480 NEXT I
2490 GOTO 1825
2495 '
2500 REM --- Search option
2510 PRINT "      Option 'search' chosen.":PRINT
2520 IF SEED > 30000 OR SEED < -30000 THEN SEED=1987
2530 RANDOMIZE SEED
2540 FOR I=1 TO 7
2550 IF CHIOPT(I,1) >2 THEN GOTO 2600
2560 PRINT "The random value for " CHI$(I) " have been re-
      generated."
2570 FOR J=1 TO CHIOPT(I,2)
2580 CHIVAL(I,J)=RND*(CHIOPT(I,4)-CHIOPT(I,3))+CHIOPT(I,3)
2590 NEXT J
2600 IF CHIOPT(I,1) < 4 GOTO 2660
2610 REM ---- range data setup
2620 CHIVAL(I,1)=CHIOPT(I,3):CHIVAL(I,CHIOPT(I,2))=
      CHIOPT(I,4)
2630 FOR J=2 TO CHIOPT(I,2)-1
2640 CHIVAL(I,J)=CHIVAL(I,J-1)+CHIOPT(I,5)
2650 NEXT J
2660 NEXT I
2690 '
2700 REM --- search
2710 COUNT=0:SN=0
2720 FOR AB=1 TO CHIOPT(1,2)
2730 FOR AC=1 TO CHIOPT(2,2)
2740 FOR AD=1 TO CHIOPT(3,2)
2750 FOR BC=1 TO CHIOPT(4,2)
2760 FOR BD=1 TO CHIOPT(5,2)
2770 FOR CD=1 TO CHIOPT(6,2)
2780 FOR CRIT=1 TO CHIOPT(7,2)

```

```

2800 REM --- function check
2810 COUNT=COUNT+1
2820 FOR I=1 TO NF
2830 X=X(I):Y=Y(I)
2840 IF (1-X)*(1-Y)*CHIVAL(2,AC)+(1-X)*Y*CHIVAL(3,AD)+X*
    (1-Y)*CHIVAL(4,BC)+X*Y*CHIVAL(5,BD)-X*(1-X)*CHIVAL(1,
    AB)-Y*(1-Y)*CHIVAL(6,CD)-CHIVAL(7,CRIT)>0 THEN D=1
    ELSE D=-1
2850 IF D<>F(I) THEN GOTO 3320
2860 NEXT I
2890
2900 REM --- drawing
2910 FOR YINC=0 TO 10
2920 Y=YINC*.1
2930 FOR XINC=0 TO 10
2940 X=XINC*.1
2950 IF (1-X)*(1-Y)*CHIVAL(2,AC)+(1-X)*Y*CHIVAL(3,AD)
    +X*(1-Y)*CHIVAL(4,BC)+X*Y*CHIVAL(5,BD)
    -X*(1-X)*CHIVAL(1,AB)-Y*(1-Y)*CHIVAL(6,CD)
    -CHIVAL(7,CRIT) > 0 THEN P$(XINC+2,YINC+2)="+" ELSE
    P$(XINC+2,YINC+2)="-"
2980 NEXT XINC
2990 NEXT YINC
3000 FOR Y=1 TO 12
3010 P$(1,Y)=" "
3020 NEXT Y
3030 FOR X=1 TO 12
3040 P$(X,1)=" "
3050 NEXT X
3060 P$(1,12)="1 ":P$(1,7)="y ":P$(1,2)="0 "
3070 P$(2,1)="0 ":P$(7,1)="x ":P$(12,1)="1 ":PRINT
3080 FOR Y=12 TO 1 STEP -1
3090 PRINT SPC(10);
3100 FOR X=1 TO 11
3110 PRINT P$(X,Y);
3120 NEXT X
3130 PRINT P$(12,Y)
3140 NEXT Y
3190
3200 REM --- chi value printing
3210 PRINT:PRINT USING"\      \+###.###\      \+###.###\      \
    +###.###\      \+###.###\      \+###.###\      \+###.###";
    "Xab=";CHIVAL(1,AB);" Xac=";CHIVAL(2,AC);" Xad=";
    CHIVAL(3,AD);" Xbc=";CHIVAL(4,BC);" Xbd=";
    CHIVAL(5,BD);" Xcd=";CHIVAL(6,CD)
3220 PRINT USING "\      \+###.###";"Xcrit=";CHIVAL(7,CRIT)
3230 PRINT:INPUT "Do you want to save this chi values? Type
    (y)es or (n)o. ",A$

```

```

3235 IF A$<>"Y" AND A$<>"y" AND A$<>"N" AND A$<>"n" THEN
    GOTO 3230
3240 IF A$<>"Y" AND A$<>"y" THEN GOTO 3290
3250 SN=SN+1
3260 CHIS(SN,1)=CHIVAL(1,AB):CHIS(SN,2)=CHIVAL(2,AC):
    CHIS(SN,3)=CHIVAL(3,AD)
3270 CHIS(SN,4)=CHIVAL(4,BC):CHIS(SN,5)=CHIVAL(5,BD):
    CHIS(SN,6)=CHIVAL(6,CD)
3280 CHIS(SN,7)=CHIVAL(7,CRIT)
3290 PRINT:INPUT "(c)ontinue or (b)ack to main menu? ",A$
3295 IF A$<>"C" AND A$<>"c" AND A$<>"B" AND A$<>"b" THEN
    GOTO 3290
3300 IF A$="B" OR A$="b" THEN GOTO 1300
3310 PRINT "          Option 'continue' chosen."
3320 IF COUNT=5000 OR COUNT=10000 OR COUNT=15000 THEN
    PRINT COUNT "sets of X values have been tested so far."
3400 NEXT CRIT
3410 NEXT CD
3420 NEXT BD
3430 NEXT BC
3440 NEXT AD
3450 NEXT AC
3460 NEXT AB
3500 PRINT "The search is complete."
3510 PRINT "          " COUNT " sets of X values were tested."
3520 GOTO 1300
3980 '
3990 '
4000 REM --- plot option
4005 HOR=1:XSAMP=20:YSAMP=20:P=1:KEY OFF:SCREEN 0
4010 SCREEN 0:PRINT:PRINT X$:PRINT "Main menu -- Do you
    want to:"
4020 PRINT "          (c) change chi values"
4030 PRINT "          (g) change the way of graph look"
4040 PRINT "          (s) see the graphs on your terminal"
4055 PRINT "          * When drawing is finished"
4056 PRINT "          if you want to print it, type
    both 'shift' and 'prtsc' key."
4057 PRINT "          After the printing, type
    'return' key."
4058 PRINT "          if not type 'return' key."
4060 PRINT "          (q) or quit":PRINT X$
4070 INPUT "Type c,g,s,p or q : ",A$
4080 IF A$<>"C" AND A$<>"c" AND A$<>"G" AND A$<>"g" AND
    A$<>"S" AND A$<>"s" AND A$<>"P" AND A$<>"p" AND
    A$<>"Q" AND A$<>"q" THEN GOTO 4070
4090 IF A$="C" OR A$="c" THEN GOTO 4100 ELSE IF A$="G" OR
    A$="g" THEN GOTO 4300 ELSE IF A$="S" OR A$="s" THEN
    GOTO 4600

```

```

4095 SN=0:GOTO 1090
4098 '
4100 REM --- change option
4110 PRINT "      Option 'chis' chosen."
4120 PRINT:PRINT "Number of different settings of X's = "
      SN:PRINT
4130 FOR I=1 TO SN
4140 PRINT USING"###\      \+###.###\      \+###.###\      \+###.###\
      \      \+###.###\      \+###.###\      \+###.###\      \+###.###\
      " Xab= ";CHIS(I,1);" Xac= ";CHIS(I,2);" Xad= ";
      CHIS(I,3);" Xbc= ";CHIS(I,4);" Xbd= ";CHIS(I,5);
      " Xcd= ";CHIS(I,6)
4150 PRINT USING"\      \+###.###";"      Xcrit= ";CHIS(I,7)
4160 NEXT I
4170 INPUT "Do you want to enter more values to plot? (y)es
      or (n)o. ",A$
4175 IF A$<>"Y" AND A$<>"y" AND A$<>"N" AND A$<>"n" THEN
      GOTO 4170
4180 IF A$="N" OR A$="n" THEN GOTO 4000
4190 SN=SN+1
4200 INPUT "Enter new Xab, Xac, Xad, Xbc, Xbd, Xcd and
      Xcrit : ",CHIS(SN,1),CHIS
4210 GOTO 4120
4300 REM --- graph option
4310 PRINT X$:PRINT "      Option 'graph' chosen.":PRINT
4320 PRINT:PRINT "Do you want to change the"
4330 PRINT "      (g) number of graphs horizontally : currently
      " HOR
4340 PRINT "      (s) number of x and y samples : currently "
      XSAMP " and " YSAMP
4350 PRINT "      (b) go back to the main menu":PRINT X$
4360 INPUT "Type g,s or b. : ", A$
4370 IF A$<>"G" AND A$<>"g" AND A$<>"S" AND A$<>"s" AND
      A$<>"B" AND A$<>"b" THEN GOTO 4360
4380 IF A$="S" OR A$="g" THEN GOTO 4500 ELSE IF A$="s" OR
      A$="S" THEN GOTO 4550 ELSE GOTO 4010
4500 REM --- number of graphs
4510 PRINT"      Option 'graphs per page' chosen.":PRINT
4520 INPUT "How many graphs horizontally on a page do you
      want? ",HOR
4530 GOTO 4320
4550 REM --- x,y samples
4560 PRINT "      Option 'samples of x and y' chosen.":PRINT
4570 INPUT "How many samples of x and of y would you like?
      ", XSAMP,YSAMP
4580 GOTO 4320
4590 '
4600 REM --- see graph

```

```

4615 PRINT
4620 PGNUM=INT(SN/HOR)+1:XSTEP=1/XSAMP:YSTEP=1/YSAMP:
    SCREEN 2
4640 FOR I=1 TO PGNUM
4650 CLS:ON HOR GOTO 4660,4700,4800
4660 X1=220:X2=420:Y1=110:Y2=23
4670 XGAP=200/XSAMP:XGO=XGAP*.6:YGAP=87/YSAMP
4680 GOSUB 5000:P=P+1:GOTO 4970
4700 REM --- hor 2
4710 XGAP=200/XSAMP:XGO=XGAP*.6:YGAP=87/YSAMP
4720 Y1=110:Y2=23
4730 X1=380:X2=580:GOSUB 5000
4740 P=P+1:IF P > SN GOTO 4970
4745 X1=60:X2=260:GOSUB 5000
4750 P=P+1:GOTO 4970
4800 REM --- hor 3
4810 XGAP=170/XSAMP:XGO=XGAP*.6:YGAP=75/YSAMP:Y1=110:Y2=35
4820 X1=435:X2=605:GOSUB 5000
4830 P=P+1:IF P > SN GOTO 4970
4835 X1=225:X2=395:GOSUB 5000
4840 P=P+1:IF P > SN THEN GOTO 4970
4845 X1=15:X2=185:GOSUB 5000
4850 P=P+1
4970 LOCATE 24,1:INPUT " ",A$
4980 LOCATE 25,1:PRINT:INPUT "Do you want to (c)ontinue or
    (b)ack to main menu? ",A$
4985 IF A$<>"C" AND A$<>"c" AND A$<>"B" AND A$<>"b" THEN
    GOTO 4980
4990 IF A$="B" OR A$="b" THEN GOTO 4010
4995 NEXT I
4998 '
4999 '
5000 IF P > SN THEN GOTO 4005:REM --- drawing
5010 LINE(X1,Y1)-(X2+XGAP,Y2),,P
5020 XPOS=X1-XGAP
5030 FOR XD=0 TO XSAMP
5040 X=XD*XSTEP:XPOS=XPOS+XGAP:YPOS=Y1+YGAP
5050 FOR YD=0 TO YSAMP
5060 Y=YD*YSTEP:YPOS=YPOS-YGAP
5070 IF (1-X)*(1-Y)*CHIS(P,2)+(1-X)*Y*CHIS(P,3)
    +X*(1-Y)*CHIS(P,4)+X*Y*CHIS(P,5)-X*(1-X)*CHIS(P,1)
    -Y*(1-Y)*CHIS(P,6)-CHIS(P,7) <= 0 THEN
    LINE(XPOS,YPOS)-(XPOS+XGO,YPOS)
5080 NEXT YD
5090 NEXT XD
5200 XLEFT=INT((X1-5)/8):YHALF=INT((Y1+Y2)/2):YUP=INT(Y2/8):
    LOCATE YUP+1,XLEFT:PRINT "1"

```

```

5210 LOCATE YHALF/8,XLEFT:PRINT "y":LINE(X1,YHALF)
      -(X1+XGO*.5,YHALF)
5220 LOCATE INT(Y1/8)+1,1:PRINT TAB(XLEFT) "0"
5230 XCENT=(X1+X2)/16:YLOW=INT((Y1+15)/8):LOCATE YLOW,
      INT(X1/8)+2:PRINT "0":LOCATE YLOW,XCENT+1:PRINT "x":
      LOCATE YLOW,INT(X2/8)+2:PRINT "1"
5310 LINE(XCENT*8,Y1)-(XCENT*8,Y1-XGO*.5)
5320 LOCATE YLOW+2,XLEFT+1:PRINT USING"\      \+###.###\      \
      +###.###"; " Xab= ";CHIS(P,1); " Xac= ";CHIS(P,2)
5330 LOCATE YLOW+3,XLEFT+1:PRINT USING"\      \+###.###\      \
      +###.###"; " Xad= ";CHIS(P,3); " Xbc= ";CHIS(P,4)
5340 LOCATE YLOW+4,XLEFT+1:PRINT USING"\      \+###.###\      \
      +###.###"; " Xbd= ";CHIS(P,5); " Xcd= ";CHIS(P,6)
5350 LOCATE YLOW+5,XLEFT+1:PRINT USING"\      \+###.###";
      " Xcrit= ";CHIS(P,7)
5360 RETURN

```

